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FULL LENGTH ARTICLE 2

Robust pre-departure scheduling for a nation-wide 4 air traffic flow management

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- 19 Air traffic flow management;
- 20 Airport and airspace net-
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- work;
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- Capacity uncertainty; 23 Chance constraint;
- 24 Stochastic optimization



Abstract Air traffic flow management has been a major means for balancing air traffic demand and airport or airspace capacity to reduce congestion and flight delays. However, unpredictable factors, such as weather and equipment malfunctions, can cause dynamic changes in airport and sector capacity, resulting in significant alterations to optimized flight schedules and the calculated predeparture slots. Therefore, taking into account capacity uncertainties is essential to create a more resilient flight schedule. This paper addresses the flight pre-departure sequencing issue and introduces a capacity uncertainty model for optimizing flight schedule at the airport network level. The goal of the model is to reduce the total cost of flight delays while increasing the robustness of the optimized schedule. A chance-constrained model is developed to address the capacity uncertainty of airports and sectors, and the significance of airports and sectors in the airport network is considered when setting the violation probability. The performance of the model is evaluated using real flight data by comparing them with the results of the deterministic model. The development of the model based on the characteristics of this special optimization mechanism can significantly enhance its performance in addressing the pre-departure flight scheduling problem at the airport network level.

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1. Introduction

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The 2018 International Civil Aviation Organization (ICAO) 27 statistics showed that 4.3 billion passengers were served by 28

air transport, a 6.1% increase from the previous year.¹ Despite

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30 the construction of new infrastructure to enhance the capacity 31 and efficiency of air traffic systems, flight delays remain an issue due to unpredictable elements such as extreme weather. 32 In 2018, the flight departure delays within Europe rose to 33 14.7 min per flight, a 2.3 min increase from 2017.² The imbal-34 ance between the capacity of the air traffic system and the 35 demand for traffic is still the primary cause of flight delays. 36 Consequently, optimization of air traffic operations is still a 37 major area of research. 38

A great deal of research has been conducted to improve the 39 40 operational effectiveness of air traffic systems since the 1990s. 41 From the investigation of the Ground Holding Problem 42 (GHP) of single airports, multiairports and airport networks,^{3,4} to the examination of the dynamic flow problem of 43 the network and the formulation of the uncertainty problem,⁵ 44 45 researchers from all over the world have made remarkable advances in the air transportation field. Since 2010, researchers 46 47 have been attempting to optimize the flight schedule in a way that is more beneficial to all parties, taking into account fair-48 ness.^{7–11} Furthermore, to create a more reliable flight schedule, 49 the uncertainty factor in the airport network has also received 50 attention.^{12–14} As research results continue to be enriched, sys-51 tematized integrated models have also been featured in many 52 studies.^{15–17} Some researchers have shifted their focus from 53 the supply side to the demand side of air transport service.^{18,19} 54 55 The use of mathematics and big data has also been explored to optimize flight schedules.²⁰⁻²² In recent years, a large body of 56 literature has been developed around the topic of airport 57 capacity and demand management. 58

Air Traffic Flow Management (ATFM) is a key technique 59 used by traffic management operators to balance the capacity 60 of airports/airspace and air traffic demand. This has been a 61 major area of research for many years. ATFM can be broken 62 down into three stages: strategic ATFM, pre-tactical ATFM 63 64 and tactical ATFM. Strategic ATFM begins several months 65 before the day of operation and involves slot allocation and airspace organization. Pre-tactical ATFM can start from a 66 week or a day before the day of operation, during which flight 67 schedules may be adjusted. The tactical phase is usually the 68 day of flight operation and the main activities include execut-69 70 ing the daily plan developed in the pre-tactical phase, and formulating and implementing tactical traffic flow management 71 measures to address unexpected supply-demand imbalances. 72 The implementation of ATFM involves airlines, airports, 73 and air traffic control authority. For more than two decades, 74 the concept of Collaborative Decision Making (CDM) has 75 76 been explored around the world to enhance the effectiveness of ATFM. This concept has now been widely adopted in major 77 airports and Airport CDM (A-CDM) has become a successful 78 example of its application. A-CDM's operation process helps 79 to reduce delays, improve punctuality, and optimize resource 80 utilization. It provides an information sharing platform and 81 82 decision-making mechanism for multiple parties in air trans-83 port, allowing them to optimize resource utilization while still meeting the interests of all parties. The specific process and the 84 16 milestones are illustrated in Fig. 1.²³ All parties involved 85 share their latest information and plan to keep everyone main-86 taining the same situation awareness. Two important informa-87 tion provided by air traffic control for departure flights are the 88 Target Take-off Time (TTOT) and the Target Start-up 89 Approval Time (TSAT). More accurate and stable timing 90

information is vital to the successful implementation of A-CDM.

However, insufficient focus has been given to examining the 93 robust optimization of departure slots for all flights within the 94 aviation system. Although current research and decision mak-95 ing tools can identify the best flight schedule for air traffic 96 management authorities, changes in departure slots may occur 97 due to unexpected events or operational constraints that affect 98 capacity in downstream sectors or airports. Such occurrences 99 are commonly observed in actual operational scenarios. If 100 the actual capacity is lower than the expected capacity, and 101 too many flights were scheduled during the period, then some flights will not be able to take off as planned, resulting in flight 103 delays. On the other hand, if the actual capacity is higher than the predicted capacity, for instance, the capacity of the affected 105 airport or airspace is quickly restored, the preassigned depar-106 ture slots may have to be changed earlier to avoid wasting 107 capacity and unnecessary flight delays. In such situations, airlines have to rearrange their resources to facilitate earlier departures, which could result in increased workload and cost. 110 One of the primary obstacles is making departure decisions 111 when faced with capacity uncertainty. There is still a deficiency 112 in methods for accurately forecasting airport and airspace 113 capacity. The second issue lies in the complexity of the air traf-114 fic management system as a networked system, where modifi-115 cations in operations at a specific sector or airport can impact the operations of other airports and sectors within 117 the network. In instances where a hub airport's operational 118 capacity falls short of the anticipated level, traffic control 119 restrictions will affect both incoming and outgoing flights at 120 that airport. Over-scheduled flights have to be delayed, leading 121 to delays that will propagate through the entire air transportation network. Conversely, the repercussions of over-scheduling are less significant at smaller airports with lower levels of traffic. No research has been conducted to investigate the impact 125 of network effects on the optimized strategies in air traffic flow 126 management problems when using optimization techniques 127 that account for uncertainty in stochastic scenarios. 128

This paper investigates the pre-departure scheduling in the 129 tactical phase of air traffic flow management. Real-time data are used to make optimal adjustments to the flight schedule 131 to enhance airport efficiency and punctuality. The contribu-132 tions of our work are outlined below. First, a pre-departure 133 scheduling model is proposed which considers uncertain 134 capacity of airport and airspace to minimize the total cost of flight delays. The chance constraint method is used to manage the uncertainty of airport and sector capacity. Second, our model takes the characteristics of air traffic network into 138 account while the computational results are compared with 139 the optimization results of the deterministic capacity model, 140 as well as the superiority of the capacity uncertainty model 141 considering the node importance over the traditional model 142 that only considers capacity uncertainty. This study is valuable for improving the effectiveness of collaborative air traffic flow management, and could have significant implications for designing network control strategies in uncertain conditions.

This paper is organized as follows. Section 2 reviews the 147 existing literature on air traffic flow management, uncertainty 148 problems, and the chance constraint method. Section 3 pre-149 sents a model for allocating uncertainty departure and arrival 150 slots flights at the airport network level and explains the trans-151 formation of chance constraints. Section 4 examines the struc-152

16. ATOT

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7/8. AIBT

AGHT

6. ALDT

Enroute

Fig. 1 Airport CDM milestones. A total of 16 key events during arrival and departure are marked as milestones.²³ Some critical time events are Calculated Take-off Time (CTOT), Actual Take-off Time (ATOT), Actual Landing Time (ALDT), Actual In-block Time (AIBT), Actual Commencement of Ground Handling Operations Time (ACGHOT), Target Off-block Time (TOBT), Aircraft Ready for Departure Time (ARDT), Aircraft Startup Requested Time (ASRT), Actual Start-up Approval Time (ASAT), Actual Off-block Time (AOBT), Actual Take-off Time (ATOT).

tural characteristics of the national air traffic network and
evaluates the importance of the airport and sector nodes. Section 5 introduces two methods to set the probability of violation of chance constraints and provides experimental results.
Section 6 is the conclusion.

2. CTOT allocation

Departure airport

-3 h -2 h

3. Take off (ATOT)

158 **2. Literature review**

The majority of the world's busiest airports experience signif-159 160 icant issues with traffic congestion and flight delays. Expanding airport infrastructure to increase capacity is a potential 161 162 solution, but it is a lengthy and costly process that makes it dif-163 ficult to quickly solve the problem. An effective and practical 164 alternative is air traffic flow management. In 1987, Odoni proposed a mathematical model for the first time to address the air 165 traffic flow management problem. The model seeks to balance 166 airport capacity and traffic demand, converting air delay into 167 ground delay, thus reducing the cost of flight operations.²⁴ Sig-168 nificant attention has been focused on researching air traffic 169 flow management since that time. Comprehensive reviews of 170 air traffic flow management can be found in Ref. 25-27. This 171 section provides an overview of research conducted on pre-172 173 tactical and network-level tactical air traffic flow management. The studies can be categorized into deterministic traffic man-174 agement models and stochastic traffic management models, 175 depending on whether they consider the future impact on air-176 177 port or sector capacity as deterministic or uncertain.

178 2.1. Deterministic air traffic flow management models

The first research on ground holding strategies for air traffic 179 flow management is discussed in Ref. 28, where a deterministic 180 181 model is introduced for the holding of the ground in a single airport. The model takes into account the airport's capacity, 182 183 which is determined by factors such as weather conditions (such as wind speed and visibility), to calculate flight departure 184 times and delays. However, this model does not account for 185 the ripple effect of delays spreading between successive flights 186 of the same aircraft. In Ref. 3, a collaborative multi-airport 187 ground delay model is proposed and a heuristic algorithm is 188 189 developed to find a feasible solution in a reasonable time. This study examines the ground delay strategies for a network of 190 airports where the impacts of delay propagation over time 191 are carefully considered. To account for both airport capacity 192 and sector capacity constraints, a 0-1 integer program model is 193 developed.²⁹ Nevertheless, the model does not account for 194 flight rerouting and cancellations. Subsequently, the authors 195 proposed a dynamic network flow method to examine the 196 reroute issue within air traffic flow management. ⁵Lulli argued 197 that the circumstances in Europe are distinct from those in the 198 U.S. and proposed a deterministic dynamic model for Euro-199 pean air traffic flow management.³⁰ A novel integer program-200 ming model for solving large-scale air traffic flow problems are 201 presented in.³¹ The model covers all the phases of flights, 202 including departure, cruising, and landing, and considers var-203 ious regulatory actions such as ground delays, route changes, 204 speed adjustments, and airborne holding. It incorporates a 205 multivariable framework with three categories of constraints 206 to enhance relaxation conditions, enabling efficient resolution 207 of air traffic management scenarios comparable in size to the 208 entire United States. In a different research venue, a team of 209 researchers investigates air traffic flow management through 210 the use of Eulerian models. For example, a Eulerian model is 211 proposed in Ref. 32, which is based on the Cell Transmission 212 Model (CTM). This model operates under the assumption that 213 flights between specific Origin-Destination (OD) pairs can be 214 represented as paths, which consist of a sequence of links. 215 Each link corresponds to a sector, and these links are further 216 segmented into cells, where the average flight duration between 217 OD pairs defines the path length and each cell's length is con-218 sidered as 1 min. In the Cell Transmission Model (CTM), the 219 state variable is the total count of aircraft in each cell during 220 every time interval, and the total aircraft count in a sector is 221 the aggregate of all aircraft across all cells within that sector. 222 This modeling approach pertains to the airway level, and the 223 model's dimensions are dictated by the network structure. 224 Another interesting work is in Ref. 33, where an Eulerian-225 Lagrangian model is developed by taking into account the 226 departure and arrival fix information of the flights. A Linear 227 Transmission Model (LTM) has been created, and a method 228 for pairwise decomposition is introduced to discover the best 229 global solution (Cao and Sun³⁴). Similar to the CTM, this 230

12. ARDT

14. ASAT

10. ATC issues TSAT

Destination airport

model can achieve the optimum outcome, yet it operates 231 232 approximately six times faster than the CTM. The above men-233 tioned studies can determine the optimal air traffic flow man-234 agement strategies assuming that airport and sector capacities are fixed. However, these capacities are subject to change due 235 to stochastic factors, such as weather, equipment malfunc-236 237 tions, and air traffic controller's personal capability. Several methods have been suggested to tackle the issue of stochastic 238 air traffic flow management. 239

240 2.2. Stochastic air traffic flow management models

In Ref. 35, a dynamic multi-stage stochastic integer program-241 ming model is introduced for a single airport. This model 242 employs a scenario tree to depict the uncertain capacity, and 243 as time progresses, the decision tree branches out to create 244 245 numerous scenarios. Hoffman argued that single airport flow management does not take into account the connectivity 246 between flights, which can lead to impractical situation due 247 248 to the impact of previous flight. To deal with the unpredictability of airport capacity in ground delay programs, Liu et al.³⁶ 249 developed an airport capacity scenario tree using historical 250 data on airport capacity distribution. Agustin et al.³⁷ devel-251 252 oped a multistage hybrid 0-1 programming model to solve 253 the air traffic management problem, taking into account the 254 uncertainty of the capacity of airports and sectors simultane-255 ously, as well as flight rerouting. Stochastic optimization has become a widely used method for dealing with optimization 256 problems that involve uncertain parameters. The main idea 257 behind is to minimize the risk of exceeding capacity constraints 258 259 in cases where the probability distributions of the nodes are understood. Bertsimas and Sim⁶ discussed the challenge of 260 dealing with data uncertainty in the context of the network 261 262 flow optimization problem. They introduced a robust optimization approach to tackle this uncertainty, allowing users 263 to manage the level of constraint violation and consequently 264 adjust the model's level of conservatism. However, when cost 265 266 coefficients contain uncertainties, the 0-1 discrete optimization 267 problem on n variables requires at most n + 1 instances of the original problem to solve the robust counterpart, which is 268 computationally intensive. Janak et al.³⁸ proposed a novel 269 270 robust optimization approach to address planning problems with bounded uncertainty. The model was implemented in real 271 industrial cases to achieve dependable and resilient solutions. 272 Gupta et al.³⁹ proposed a robust optimization approach to 273 274 tackle the uncertainty in air traffic flow management. How-275 ever, the model optimized the worst case of uncertain parameters, resulting in an overly conservative and resource-wasteful 276 allocation scheme. Clare and Richards⁴⁰ proposed a robust 277 optimization method to solve the planning problem with 278 279 bounded uncertainty, assuming that the future capacity prob-280 ability distribution information is known. They integrated a 281 deterministic discrete decision mixed integer linear model with sector capacity violation probability constraints to create a 282 283 chance-constrained model. However, The study employed a 284 brute force algorithm to address the model, leading to computational constraints and challenges in solving large-scale prac-285 tical issues. Chen et al.⁴¹ developed a chance-constrained air 286 traffic flow management model by adding probabilistic con-287 288 straints to a deterministic integer programming model. The capacity information of the probabilistic sector is incorporated 289

within the chance constraints. A polynomial approximation 290 chance constraint optimization algorithm is developed, which 291 is capable of providing optimal traffic management scheme 292 with efficient computational speed. Scenarios generate method 293 is used to reduce the number of possible operation scenarios in 294 order to solve the chance constrained models.42,43 These 295 stochastic air traffic flow management models provide mathe-296 matical frameworks used to optimize the flow of air traffic in 297 uncertain conditions, considering the random nature of factors 298 such as weather, aircraft delays, and airspace congestion. By 299 incorporating probability distributions and stochastic pro-300 cesses, they aim to find optimal solutions that minimize delays, 301 fuel consumption, and overall system costs while ensuring 302 safety and efficiency. However, most of work consider only 303 one or a few sectors operating under uncertainty. Little atten-304 tion is given to address the uncertainty of capacity in the whole 305 network. Moreover, no research has been conducted on estab-306 lishing the thresholds for capacity violations, leaving air traffic 307 flow management staff to rely on their own expertise to make 308 decisions. 309

3. A chance constrained model for air traffic flow management

3.1. Model framework and assumptions

The overall structure of the model is illustrated in Fig. 2. It 312 takes into account the capacity of airports and sectors, flight 313 plans, and the predetermined probability of violation at the 314 airport/sector. Each flight plan includes the departure airport, 315 destination airport, planned departure time, planned arrival 316 time, list of sectors, and the associated flying time for travers-317 ing each sector, turnaround time at the airport, etc. The model 318 optimizes the departure time and arrival time for each flight to 319 ensure that the traffic demand and capacity are balanced. We 320 use five-minute intervals as the time unit. Due to the data con-321 straints, we assume that each flight can pass through the sector 322 with the minimum sector flying time. In future work, we can 323 consider variable flying times for different flights. 324

3.2. Description of notations 325

The sets, parameters and variables used in the model are given in Tables 1–4.

The aim of the model is to reduce the total cost of flight delays. Flight delay is defined as the time difference between its scheduled time of operation and its actual time of operation. It should be noted that the departure displacement includes both ground delays and early departures. The objective function is represented in Eq. (1):

$$Q = \min\left(\sum_{f \in F_{\text{wait}}, a = O_f} \beta \left| t - t_f^{\text{dep}} \right| X_{f, a, t} + \sum_{f \in F} \theta y_f Y_f\right)$$
(1) 337

The cost in the objective function consists of two parts. The first part is the cost of adjusting the departure slot for departure flights as expressed as $\sum_{f \in F_{\text{wait}}, a = O_f} \beta \left| t - t_f^{\text{dep}} \right| X_{f,a,t}$, and the second part, $\sum_{f \in F} \theta y_f Y_f$, is the cost of air delays for all flights.

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Table 2 Parameters of model.

Fig. 2 Model framework.

Table 1 Sets of model. Set Description T/T_{15} Set of 5-minute/15-minute slots in a day Set of flights scheduled to depart at T_{\min} and within 3 h Fwait $F_{\rm fly}$ Set of flights that have not yet arrived at T_{\min} F Set of all flights, $F = F_{wait} \cup F_{fly}$ Set of sectors that flight f has passed through or is in at $S_{f,T_{min}}^{by}$ $T_{\min}, f \in F_{fly}$ Set of all sectors that flight f passes through(include S_f departure and arrival airports), $f \in F$ S'_f Set of sectors that flight f passes through(exclude arrival airport compared to S_f , $f \in F$ S Set of sectors F_s Set of flights passing through sector $s, s \in S$ A_f/A_f' Set of departure and arrival airports/pairs of departure and arrival airports (a, a') for flight $f, f \in F$ $A^{\rm dep}/A^{\rm arr}$ Set of departure/arrival airports $F_a^{\rm dep}/F_a^{\rm arr}$ Set of flights with a as departure/arrival airport, $a \in A^{dep}/A^{arr}$ Set of pairs of connecting flights (f_1, f_2) Р P'Set of airport pairs (a, a') corresponding to the connecting flight pair (f_1, f_2) , where a_1 is the arrival airport of f_1 and a_2 is the departure airport of f_2

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Operators and managers prefer to keep flights on the 2 ground rather than in the air, as this increases fuel consump-43 tion and the chances of unsafe events. Based on previous stud-4 ies on the study of Ground Delay Program(GDP),^{44,45} this 15 paper sets the cost ratio of airborne delay to ground delay as 346 2:1. For simplicity, the cost of one unit of airborne delay is 347 100, and for ground delay it is 50. 348

349 3.4. Deterministic model constraints

The constraints of the model are capacity constraints, flight 350 connection constraints, and flight time constraints. Eq. (2) to 351 Eq. (21) are the constraints of the model. 352

(1) Constraints for the flights in the air 353

Parameter	Description
T_{\min}	The start time of the flight schedule to be optimized
T_{max} $t_f^{\text{dep}}/t_f^{\text{arr}}/t_f^{\text{fly}}$	The end time of the flight schedule to be optimized Original departure/arrival/fly time of flight $f, f \in F$
O_f/D_f	Departure/Arrival airport for flight $f, f \in F$
β/θ	Cost of unit slot displacement of departure/air delay
$S_{f,T_{\min}}$	Sector in which flight <i>f</i> is located at $T_{\min}, f \in F_{\text{fly}}$
$S_{f,s}^{\text{next}}$	Next sector of sector s where flight f is located
2.1	now, $f \in F$, $s \in S'_f$
$t_{f,s}^{\text{in}}$	The slot when flight f enters sector $s, f \in F_{fly}, s \in S_{f,T_{min}}^{by}$
$t_{f,s,\min}^{\mathrm{fly}}$	Minimum fly time of flight f in sector $s, f \in F, s \in S_f$
$\lambda_{a,t}^{\mathrm{dep}}/\mu_{a,t}^{\mathrm{arr}}$	Capacity of airport <i>a</i> at slot $t, a \in A^{dep}/A^{arr}, t \in T_{15}$
$\varphi_{s,t}$	Capacity of sector s at slot $t,s \in S, t \in T_{15}$
U	Maximum air delay for any flight which set to 1 h
L	Maximum delay for departure flight which set to 3 h
Κ	Maximum advanced arrival time for flight which set
	to 1 h
V	Minimum turnaround time for connecting flight
	which set to 30 min
M	A positive number of infinite size
α	Violation probability

 Table 3
 Decision variables of model

Decision variable	Description
$X_{f,a,t}$	Binary variables, where 1 indicates that flight <i>f</i> is assigned to slot <i>t</i> in airport <i>a</i> ,otherwise $0, f \in F, a \in A_f, t \in T$
$W_{f,s,t}$	Binary variables, where 1 indicates at slot t flight f has left or is in sector/airport s,otherwise $0, f \in F, s \in S_f, t \in T$

Table 4 Indirect	t decision variables of model.
Indirect decision variable	Description
$\overline{b_{f,s,t}}$	Binary variables, where 1 indicates at slot t flight f is in sector s,otherwise $0, f \in F, s \in S_t, t \in T_{15}$
y_f	integer variables, where positive numbers indicate flight f occurred air delay, otherwise $0 f \in F$
Y_f	Binary variables, where 1 indicates flight f occurred air delay, otherwise $0, f \in F$

Eq. (2) ensures that the decision variable $X_{f,a,t}$ and for flights that are in the air is equal to its actual departure time. Eq. (3) ensures that the decision variable $W_{f,s,t}$ can for flights that are in the air is equal to its actual entry time of each sector it traverses. Eq. (4) ensures that the decision variable $W_{f,s,t}$ is not decreasing.

$$X_{f,a,t} = 1, \forall f \in F_{\text{fly}}, a = O_f, t = t_f^{\text{dep}}$$

$$\tag{2}$$

$$W_{f,s,t} = 1, \forall f \in F_{\text{fly}}, s \in S_{f,T_{\min}}^{\text{by}}, t \in \left[t_{f,s}^{\text{in}}, 287\right]$$
(3)

$$W_{f,s,t-1} \leqslant W_{f,s,t}, \forall f \in F, s \in S_f, t \in [1, 287]$$

$$\tag{4}$$

$$X_{f,a,t} = W_{f,s,t} - W_{f,s,t-1}, \forall f \in F, a \in A_f, s = a, t \in [1, 287]$$
(5)

(2) Flight operational constraints

Eq. (5) expresses the relation between the decision variables $X_{f,a,t}$ and $W_{f,s,t}$. When $X_{f,a,t} = 0$, this means that the flight f has not left the airport a in the slot t. In this case, $W_{f,s,t}$ can be either 0 or 1. If a is an arrival airport, Eq. (6) ensures that all flights have unique departure and arrival slots. Eq. (7) ensures that flights do not arrive earlier than T_{min} . Eq. (8) guarantees that the maximum departure delay does not exceed 3 h. Eq. (9) ensures that flights arrive no more than 1 h ahead of schedule. Eq. (10) ensures that connecting flights must meet the minimum connection time requirement. Eq. (11) ensures that flights meet the sector minimum flying time. Eqs. (12)–(15) are the air delay of the flight and make sure that the maximum air delay does not exceed 1 h. Eq. (16) guarantees that transit time for connecting flights is not less than 30 min.

$$\sum_{t \in T} X_{f,a,t} = 1, \forall f \in F, a \in A_f$$
(6)

$$\sum_{t=T_{\min}}^{287} X_{f,a,t} = 1, \forall f \in F_{\text{fly}}, a \in D_f$$

$$\tag{7}$$

$$\sum_{t=T_{\min}}^{t_f^{out}+L} X_{f,a,t} = 1, \forall f \in F_{wait}, a \in O_f$$
(8)

$$\sum_{t=t_f^{\text{arr}}-K}^{287} X_{f,a,t} = 1, \forall f \in F, a \in D_f$$

$$\tag{9}$$

$$\sum_{t\in T} t^* X_{f,a,t} \leqslant \sum_{t\in T} t^* X_{f,a',t}, \forall f \in F, (a, a') \in A'_f$$

$$\tag{10}$$

$$W_{f,S_{f,s}^{\text{next}},t+t_{f,s,\min}^{\text{fly}}} \leqslant W_{f,s,t}, \forall f \in F, s \in S'_{f}, t \in \left[T_{\min}, 287 - t_{f,s,\min}^{\text{fly}}\right]$$

$$(11)$$

$$\sum_{t \in T} t^* X_{f,a',t} - \sum_{t \in T} X_{f,a,t} - t_f^{\text{fly}} \leqslant U, \forall f \in F, (a,a') \in A'_f$$
(12)

$$\sum_{t \in T} t^* X_{f,a',t} - \sum_{t \in T} X_{f,a,t} - t_f^{\text{fly}} = y_f, \forall f \in F, (a, a') \in A'_f$$
(13)
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$$y_f \ge 0.5 - M^* (1 - Y_f), \forall f \in F$$
 (14) 416

$$y_f \leq 0.5 + M^* Y_f, \forall f \in F$$

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(15)

Eqs. (17)–(21) ensure that traffic at the airport or sector will

(3) Airport and sector capacity constraints

not exceed its capacity.

$$W_{f_{2},a_{2},t+V} \leq W_{f_{1},a_{1},t}, \forall (f_{1},f_{2}) \in P, (a_{1},a_{2}) \in P', t \in [0,287-V]$$
(16)

$$\sum_{t=3t}^{3t+2} \sum_{f \in F_a^{dep}} X_{f,a,t} \leqslant \lambda_{a,t}^{dep}, \forall a \in A^{dep}, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]$$

$$(17)$$

$$430$$

$$431$$

$$\sum_{t=3t}^{3t+2} \sum_{f \in F_{a}^{\operatorname{arr}}} X_{f,a,t} \leq \mu_{a,t}^{\operatorname{arr}}, \forall a \in A^{\operatorname{arr}}, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]$$
(18)
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$$\sum_{s=3t}^{t+2} \left(W_{f,s,t} - W_{f,S_{f,s}^{\text{next}},t} \right) \ge 0.5 - M^* (1 - b_{f,s,t}),$$

$$\forall f \in F_s, s \in S, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]$$

$$436$$

$$437$$

$$\sum_{t=3t}^{5t+2} \left(W_{f,s,t} - W_{f,S_{f,s}^{\text{next}},t} \right) \leqslant 0.5 + M^* b_{f,s,t},$$

$$\forall f \in F_{t}, s \in S, t \in [\frac{T_{\min}}{2}, \frac{T_{\max}}{2} + 12]$$
(20)

$$\sum b_{fst} \leqslant \varphi_{et}, \forall s \in S, t \in \left[\frac{T_{\min}}{s}, \frac{T_{\max}}{s} + 12\right]$$
(21)

$$f \in F_s \qquad (21) \quad 442$$

3.5. Chance constraints 443

3.5.1. Establishment of chance constraints

Chen et al.⁴¹ proposed a chance constrained model to address the problem of Air Traffic Flow Management (ATFM) under uncertainty. The main idea is to replace sector capacity con-straints in the Integer Programming optimization model with probabilistic constraints. That is the capacity of a sector can be exceeded with a given probability. Here, we extend their work to consider both stochastic capacity at airports and sec-tors. Therefore, Eq. (17), Eq. (18), and Eq. (21) are replaced by Eq. (22): 454

$$P\begin{pmatrix}\sum_{t=3t}^{3t+2}\sum_{f\in F_a^{dep}}X_{f,a,t}\leqslant \lambda_{a,t}^{dep}\\\sum_{t=3t}^{3t+2}\sum_{f\in F_a^{urr}}X_{f,a,t}\leqslant \mu_{a,t}^{arr}\\\sum_{f\in F_s}b_{f,s,t}\leqslant \varphi_{s,t}\end{pmatrix} \ge 1-\alpha.$$
(22)

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This model enumerates all potential combinations of airport and sector capacities, and chooses the capacity combination that meets the violation probability. It creates a feasible set of capacity combinations, which is also the feasible set of node traffic allocations. The optimal allocation scheme is the solution in the feasible set that has the best objective function value.

The most accurate solution to the chance constraint model can be determined by enumerating all possible combinations of capacities. However, as the number of airports and sectors increases, the computational complexity increases drastically. This type of constraint model has difficulty in finding the optimal solution for large-scale problems. Therefore, we transfer the joint constraints into individual constraints based on the Bonferroni conservative approximation.⁴⁶ Thus, this article improves the chance constraint method by setting the probability of violation for a single node instead of the joint distribution for a number of nodes. Doing so will enhance the computational speed of the model and allow for the customization of node violation probabilities according to the significance of nodes in the air traffic network. As a result, this will lead to more beneficial and logically optimized strategies. The capacity constraints in our chance constraint model are expressed in Eqs. (23)-(25):

$$P\left(\sum_{t=3t}^{3t+2}\sum_{f\in F_a^{dep}} X_{f,a,t} \leqslant \lambda_{a,t}^{dep}\right) \ge 1 - \alpha_a, \forall a \in A^{dep}, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]$$
(2)

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$$P\left(\sum_{t=3t}^{3t+2} \sum_{f \in F_a^{\operatorname{arr}}} X_{f,a,t} \leqslant \mu_{a,t}^{\operatorname{arr}}\right) \ge 1 - \alpha_a, \forall a \in A^{\operatorname{arr}}, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]$$

$$P\left(\sum_{f \in F_s} b_{f,s,t} \leqslant \varphi_{s,t}\right) \ge 1 - \alpha_s, \forall s \in S, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right].$$

$$(2)$$

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3.5.2. Transformation of chance constraints into deterministic constraints

In this section, we show how to convert the chance constraints expressed in Eqs. (23)–(25) into deterministic constraints. As an example, the four capacity scenarios of a sector s are presented in Table 5.

The first row in Table 5 shows the capacity value $(\varphi_{s,t})$ of the sector s for each scenario; the second row displays the probability (PC_{s,t}) of the capacity in each scenario; the third row presents the cumulative probability (PC^{sum}_{s,t}) of the sector. Let n be the scenario number $n \in \{1, 2, 3, 4\}$. The cumulative

Table 5	Capacity distr	ibution for se	ctor s at slot	t.
Parameter	Scenario 1	Scenario 2	Scenario 3	Scenario 4
$\varphi_{s,t}$	5	6	7	8
$PC_{s,t}$	0.1	0.3	0.4	0.2
$PC_{s,t}^{sum}$	0	0.1	0.4	0.8

probability of scenario n indicates the proportion of scenarios with capacity values less than scenario n. It establishes the connection between the chance constraint and the deterministic capacity constraint by considering the probability of violation. The following example demonstrates the specific transformation process.

For example, if the probability of violation in sector s is 0.05, then it means that the maximum allowable flow is the quantile 5% of all possible capacity scenarios. Since the scenario with capacity of 5 is in the quantile 0% to 10%, the probability of violation of 0.05 is within the cumulative probability of Scenario 1 and Scenario 2. Therefore, the chance constraint can be changed into a deterministic constraint that traffic flow is less than or equal to 5. When the probability of violation is 0.95, the maximum allowed traffic is in the 95% quantile of all possible capacity scenarios. Since the capacity in Scenario 4 is in the 80% to 100% quantile, the chance constraint can be converted into a deterministic constraint with a flow less than or equal to 8. Given the empirical distribution of sector capacity, it is essential to ensure that converting a chance constraint into a deterministic one closely to the original situation. Thus, for sector s in the time slot t, a chance constraint with a probability of violation 95% can only be translated into a deterministic constraint where the flow is less than or equal to 8.

$$P\left(\sum_{f \in F_s} b_{f,s,t} \leqslant \varphi_{s,t}\right) \ge 1 - \alpha_s = \begin{cases} \sum_{f \in F_s} b_{f,s,t} \leqslant 5, & 0 \leqslant \alpha_s \leqslant 0.1\\ \sum_{f \in F_s} b_{f,s,t} \leqslant 6, & 0.1 < \alpha_s \leqslant 0.4\\ \sum_{f \in F_s} b_{f,s,t} \leqslant 7, & 0.4 < \alpha_s \leqslant 0.8\\ \sum_{f \in F_s} b_{f,s,t} \leqslant 8, & 0.8 < \alpha_s \leqslant 1 \end{cases}$$

$$(26)$$

4. Characteristics of air traffic flow network

Due to its important role in moving passengers and cargo, the 530 properties of the air transportation network have become a 531 significant subject of study within the network science field. 532 Early studies have investigated the structural features of air 533 transport networks. For instance, Guimerà et al. examined 534 the structure of worldwide air transportation network.⁴⁷ These 535 networks, whether global or national, exhibit the characteris-536 tics of scale-free small-world networks. Subsequently, the 537 emphasis of research shifted towards analyzing vital nodes 538 and fundamental characteristics of the network. Given that 539 connectivity patterns influence diffusion phenomena (such as 540 flight delays and epidemics) across the network, understanding 541 the function and essential elements of the network is crucial.⁴ 542 Earlier research has demonstrated that reductions in capacity 543 at various airports affect the overall performance of air trans-544 port systems differently.^{49,50} Motivated by these findings, it is 545 hypothesized that the characteristics of the network play a role 546 in determining probabilistic constraints and optimization 547 approaches. 548

To illustrate how flights operate in the air transportation system, Fig. 3 presents a two-layer air traffic flow network. The bottom layer represents the airport network, where the nodes represent the airports, and the edges represent the scheduled direct flights connecting the airports. The upper layers are

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554 the sector network, where the nodes are the sectors, and the 555 edges represent the flow of flight traffic between the two sec-556 tors. Arrows connect that airport and the sector in the two networks, indicating the traffic flow between the airport and the 557 sectors. Several studies have investigated the structural charac-558 teristics of aviation networks. Most networks have airports as 559 nodes and a link connects two airports if there is a flight oper-560 ating between them.⁵¹ In real operation, the airspace is divided 561 into different sectors, each of which will be managed by one or 562 two air traffic controllers.⁵¹ To capture the operational charac-563 teristics of the air traffic network, the sector network is repre-564 sented as a graph $G^{\int} = (N^{\int}, E^{\int})$, where N^{\int} is the set of 565 nodes and E^{\int} is the set of edges. Nodes $n \ (n \in N^{\int})$ of the net-566 work G^{\int} are airports and sectors, while an edge $e \ (e \in E)$ is 567 added between two nodes if there is traffic between them. In 568 this paper, an edge e represents direct flight connections 569 between a sector and a sector (or an airport). Let A^{\int} be the 570 adjacency matrix of the network G^{\int} , with each element a_{ii} rep-571 572 resenting the relationship between node *i* and *j*. For example, 573 in an undirected, unweighted network, if there is an edge 574 between *i* and *j*, then $a_{ij} = 1$; otherwise, $a_{ij} = 0$. To measure 575 the importance of nodes in the network, we introduce the fol-576 lowing metrics.

577(1) Degree and degree distribution. The degree of a node v578is denoted as k_v , which is defined as the number of edges579connected to that node. In an undirected network G, the580degree of node v is calculated as

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$$k_{v} = \sum_{u} a_{v,u} \tag{27}$$

The degree distribution is often represented as a histogram, showing the count of nodes for each degree.

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$$C_{\rm D}(v) = \frac{k_v}{\max_{\rm deg'}} \tag{28}$$

592 where \max_{d} eg is the maximum degree in the network.



Fig. 3 Air traffic network. The bottom layer is the airport network with the size of node indicating the traffic volume at the airports. The upper layer in the sector network.

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(3) Betweenness centrality. Betweenness is to measure the influence of the node v over traffic flow between other node. Betweenness centrality is defined as

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$$C_{\rm B}(v) = \sum_{i \neq v \neq j} \frac{\sigma_{ij}(v)}{\sigma'_{ij}} \tag{29}$$

where σ_{ij} is the total number of shortest path from node *i* to node *j*, and $\sigma_{ij}(v)$ is the number of those paths that pass through node *v*.

(4) Closeness centrality. Closeness centrality is a measure that quantifies how close a node is to all other nodes in a network. Mathmatically, closeness centrality is defined as

$$C_{\rm C}(v) = \frac{n-1}{\sum_{u} d(v,u)'}$$
(30) 608
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where d(v, u) is the shortest path length from node v to node u.

The importance of nodes in a network can be evaluated using metrics such as degree, betweenness, and closeness. The degree could reflect the potential for interaction between the node and other nodes in the network. However, we should note that the importance of a node is not solely determined by its degree value, but also by the degree values of its neighboring nodes. Betweenness was originally proposed to measure the social status of a node, as it is determined by the number of shortest paths that pass through it. Closeness is a measure of the proximity of a node to other nodes in the network, with a higher value indicating that the node is closer to other nodes and its information will spread more quickly. When it comes to air traffic, flight delays can spread throughout the system, leading to further delays. To reduce the amount of delays, it is essential to first minimize the initial delays, and then manage the propagation of delays in the network. Therefore, it is important to assess the importance of nodes in sector networks. Closeness could be a suitable measure for the sector nodes. Nodes with higher closeness should have a lower chance of exceeding capacity, which would control the initial delay generated by important nodes and thus limit the spread of delays in the network.

Airports, which are the beginning and end points of the air 634 traffic management system, differ from sectors. Therefore, it is 635 not appropriate to use the same network topology metric to 636 assess their importance. To this end, the airport network G^{j} 637 is created with all airports as nodes and a link between two air-638 ports if there is a scheduled traffic flow between them. The 639 degree of the airport node reflects the number of cities served 640 by the airport, but the traffic volume of the airport with high 641 degree is not necessarily large. For example, the node degrees 642 of ZBTJ(Tianjin) and ZLXY(Xi'an) are approximately equal, 643 however, the flight volume of ZLXY is almost twice as much 644 as that of ZBTJ. This means that ZLXY has a higher traffic 645 volume, making it more prone to delays. Furthermore, due 646 to the larger number of flights, ZLXY flight delays are more 647 likely to spread to other airports through the network. More-648 over, a prior research on the resilience of the airport network 649 has indicated that the traffic volume of airports is the most reli-650 able indicator of the effect of a disturbance on network effi-651

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ciency.⁵⁰ Therefore, we use traffic volume as a metric to evaluate the importance of airport nodes.

To further calculate the importance of the nodes, we use the 654 standard max-min normalization method to transfer the orig-655 inal node important metric data into the range (0, 1). Fig. 4 656 plots the importance of sector nodes and airport nodes. The 657 names of sectors are shown in the upper X-axis, while the 658 names of the airports are shown in the bottom X-axis. The sec-659 tors whose closeness are smaller than 0.209, are assumed to 660 have enough capacity handling additional flights. These sectors 661 662 are mostly located at the periphery of the network, and the probability of delay caused by these sectors is low. Thirty-663 eight of these airports have an average daily flights of more 664 665 than 200, while the remaining airports have a smaller average daily flights and a low probability of traffic exceeding airport 666 capacity. Thus, it is assumed that the capacity of these airports 667 is always enough to meet traffic demand. 668

669 5. Case study

670 5.1. Experimental setup

671 5.1.1. Data

We examine the effectiveness and performance of our model by comparing the optimized results with those obtained from the deterministic model. The flight schedule from 9:00 am to 12:00 pm on August 1, 2018 is used as input data for the models. During this period, there were 3435 flights. At 9:00AM, 1156 flights were in the air, while 2279 were still on the ground.



Fig. 4 Importance indicator of sectors and airports. The importance of airports is determined by assessing their significance through traffic volume. Similarly, the importance of sectors is determined by evaluating their significance through closeness centrality.

The air traffic network consists of 195 airport nodes and 188 sector nodes. The sector network is formulated based on airspace data from the Air Traffic Management Bureau. Estimation of the capacity of an airport or of a sector is a complex task, which is beyond the scope of this study. The airport capacity is provided by the air traffic control authority in the form of declared airport capacity. Statistical results indicate that hourly arrivals/departures of the airport vary between 40% and 70% of its declared capacity. Therefore, we use 60% of the airport declared capacity as departure capacity and arrival capacity. As there is no data available on the capacity of the sector, the sector capacity is determined as the 50th percentile of the past traffic volume moving through the sector. The primary goal of this study is to investigate the efficiency and benefits of using a chance constrained model in air traffic flow management when faced with uncertainty, taking into account the structural characteristics of the air traffic network. It is assumed that the precise determination of airport and sector capacities does not significantly influence this research. Further validation efforts can be conducted using more realistic capacity data.

5.1.2. Optimization schemes

We evaluate ten different optimization strategies in addition to the baseline (deterministic) model to compare the performance of our chance-constrained models. These ten optimization schemes are divided into two groups: (A) Method 1: Chanceconstrained model with equal probability of violation for all airports and sectors; and (B) Method 2: Chance-constrained model with the probability of violation setting based on the importance of the node. In the base optimization scheme (S_0) , all constraints in the worst-case scenario model must be satisfied. This means that optimized traffic must not exceed airport or sector capacity in all possible scenarios.

In fact, the operational capacity of airports or sectors is 711 stochastic, which means that traffic flow may exceed a given 712 capacity limit at some points. To account for this, we allow 713 capacity constraints to be violated with a small probability. 714 To set this probability, we used two different approaches. 715 The first is to set all nodes with the same probability of viola-716 tion. If this probability is set too high, it could lead to airport 717 and airspace congestion and large flight delays in actual oper-718 ations. However, if set too low, the optimized schedule may be 719 more robust to various operating scenarios, but the limited air-720 port capacity may be underused. To balance capacity utiliza-721 tion and robustness to optimization, we set five schemes 722 $\alpha \in \{0.05, 0.08, 0.11, 0.14, 0.17\}$ which are referred to as S_1 to 723 S_5 , respectively. We suggest a second approach that takes into 724 account the characteristics of the air traffic network. Small dis-725 turbances that occur at a critical airport or sector can cause 726 long unforeseen delays throughout the network. Therefore, 727 optimized traffic flow must be more resilient to uncertainty 728 in these airports and sectors, and operations strategies should 729 be more conservative. We propose a method to set the proba-730 bility of violation for airports and sectors, which takes into 731 account the importance of the airport or sector. For simplicity, 732 we use the term "node n" to refer to an airport or a sector. 733

Let H_n be the importance value of node n, then 734 Max_{ix} = max{ H_n } and Min_{ix} = min{ H_n } are the maximum 735 importance value and the minimum importance value of all 736

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⁷³⁷ nodes. The probability of violation $\alpha_{n,i}$ of the optimization ⁷³⁸ scheme *i*th, $i \in \{6, 7, 8, 9, 10\}$ is calculated as follows:

$$\gamma_{41} \qquad \alpha_n^i = \alpha_{n,\min}^i + \left(\alpha_{n,\max}^i - \alpha_{n,\min}^i\right) \frac{\operatorname{Max}_{ix} - H_n}{\operatorname{Max}_{ix} - \operatorname{Min}_{ix}}$$
(31)

where $\alpha_{n,\max}^i$ and $\alpha_{n,\min}^i$ are the predetermined violation proba-742 bilities for the nodes with the maximum importance value 743 and the minimum importance value. Here, $\alpha_{n,\max}^i$ are set to 744 0.20, while $\alpha_{n,\min}^i$ are set to {0.05, 0.08, 0.11, 0.14, 0.17}, corre-745 sponding to the schemes S_6 to S_{10} respectively. Table 6 pre-746 sents data regarding the probablity of violation α for each 747 optimization scheme. The algorithms are coded in Python 748 749 and Groubi, and are executed on a computer equipped with a 32 GB RAM and a 12th Gen Intel(R) Core(TM) i7-12700 750 Cpu (2.10 GHz). 751

752 5.2. Results

753 5.2.1. The total cost for each optimization scheme

Table 7 shows the total cost of and the computation time for 754 obtaining the optimal flight schedule under the optimization 755 756 schemes from S_0 to S_{10} . The total cost of the optimal solution 757 for the base model is 416450, with 13.2% of this cost being attributed to air delay and 86.8% to ground slot displace-758 759 ments. In the optimized schedule, 64.9% of the flights are assigned their scheduled departure time, and 35.1% are 760 delayed (98.7%) or depart earlier (1.3%). In contrast, 81.1% 761 762 of the arrival flights are not assigned their original scheduled 763 arrival slot, with 42.8% being delayed and 57.2% assigned ear-764 lier slots. This is likely due to the fact that airlines adding buffer time to their scheduled blocked time to account for 765 potential flight delays.⁵² 766

In uncertainty scenarios, the total delay cost decreases as 767 the probability of violation increases for both the random set-768 ting and the importance-based node setting. This is because an 769 770 increase in the capacity chance constraint violation probability enlarges the feasible domain of the model solution, prompting 771 the model to search for a flight schedule with a lower total cost. 772 773 Since excessive air delay can cause airspace congestion and air traffic safety concerns, the unit cost of air delay is higher than 774 the unit cost of ground delay in the objective function setting 775 of the model. This leads to the ground delay being greater than 776 the air delay. Generally, the optimization results based on 777 778 Method 2 are better than those of Method 1. The variation is smaller, indicating greater stability. As the probability of 779 violation increases, the percentage of flights experiencing flight 780 delay decreases in all schemes in Method 1. Method 2, how-781 ever, has a concentration of 6.9%-13.6% of departure flights 782 783 with delays, and as capacity constraints become more relaxed, 784 the percentage of departure flights delayed decreases. It is evident that the percentage of departure flights that are delayed in 785

Method 2 is much lower than that in Method 1. The results show that about 90% of the departure flights depart on time. In comparison, the proportion of flights with delayed arrival flight is higher. Method 1 and Method 2 generally do not have a clear increasing or decreasing pattern but with an overall downward fluctuate.

In Fig. 5, we plot the number of slot displacements for arrival and departure flights in each optimization scheme, while Fig. 6 further shows the ratio of slot forward and slot backward displacement. We observe that in the departure flight slot displacement, the slot forward displacement maintaining numerical stability and the slot backward displacement decrease with the increase in violation probability. The backward displacement of the departure slot for all scenarios is almost always greater than the forward displacement, and the numerical change in the backward displacement is also significantly greater than that of the forward displacement. In the flight arrival slot displacement, the slot backward displacement is much smaller than the slot forward displacement, and its proportion is continuously decreasing and approaching zero. The forward displacement of the slot determines the direction of the departure slot for the flight.

The runtime of the optimization model using various schemes are displayed in Fig. 7. Our scenario involves 3435 flights, 195 airports, and 188 sectors. Traffic characteristics are comparable to those examined in,⁴¹ although our network is substantially larger (up to 20 sectors in their work). Our model was executed using a desktop computer equipped with a single 12th Gen Intel(R) i7-12700 CPU running at 2,10 GHz and 32 GB of RAM, whereas the model presented in the study by Chen et al. was run on a Spark Cluster consisting of 6 nodes, with each node containing an 8-processor CPU. While it is not possible to directly compare the computational complexities of the two studies, our model can be successfully solved within a 20-minute timeframe for all optimization schemes, with the exception of S_6 and S_7 .

5.3. Robustness tests

In Section 5.2, we compare and analyze the total cost, the pro-823 portion of flights that experience slot displacements, and the 824 amount of slot displacement for arrivals and departures. As 825 expected, the total expected cost would decrease as the proba-826 bility of violation increases. The reason for this is the inclusion 827 of additional "predicted" capacity resources to meet traffic 828 demand. There is a potential risk when expanding capacity, 829 as the actual capacity may be lower than anticipated. Conse-830 quently, overscheduled flights must be rescheduled for a later 831 departure or arrival time. One advantage of the chance-832 constrained model is that it helps to ensure that constraints 833 are not violated at a specified probability level. To evaluate 834

Table 6	Violation probability for eleven optimization schemes.										
Scheme	Base method	Method	Method 1 Method 2								
	S_0	S_1	S_2	S_3	S_4	S_5	S_6	S_7	S_8	S_9	S_{10}
α	0	0.05	0.08	0.11	0.14	0.17					
α_{\min}							0.05	0.08	0.11	0.14	0.17
α _{max}							0.20	0.20	0.20	0.20	0.20

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Robust pre-departure scheduling for a nation-wide air traffic flow management

Table 7	Total cost and	computation time	(in second) for each c	ptimization schem
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Cost	S_0	S_1	S_2	S_3	S_4	S_5	S_6	S_7	S_8	S_9	S_{10}
Total	416,540	146,950	64,750	39,750	22,850	17,250	61,200	27,400	18,600	16,000	13,900
Air	54,900	14,625	6675	4350	3375	2550	8100	4050	3150	2700	2400
Gnd	364,550	132,325	58,075	35,400	19,475	14,700	53,100	23,350	15,450	13,300	11,500
Time	125,624	34,520	24,867	14,684	5324	1387	10,170	5006	1131	1277	1086



Fig. 5 Number of slot displacements for arrival and departure flights in each scenario.

the effectiveness of our approach, we use optimized flight 835 schedule as input to the operational air traffic network. How-836 ever, it is difficult to accurately predict what the future state of 837 airspace will be; therefore, a robust and stable flight schedule 838 in actual operation is more desirable. The term "robust" is 839 840 commonly defined to characterize a software, a strategy, or an item that functions effectively and demonstrates minimal 841 failures in various scenarios. In this research, we define the 842 robustness of a flight schedule as the total amount of excess 843 traffic scheduled for all sectors and airports. Here, we con-844 ducted a total of 20 experiments to compare the robustness 845 846 of the optimal flight schedule under various schemes. Each experiment generated 50 sets of combinations of capacity 847 based on the empirical distributions of the capacity of airports 848 and sectors. We compare the amount of traffic with the capac-849 ity for each flight schedule, and calculate the total amount traf-850 fic that exceeds the capacity. Let R_q be the robustness of 851 optimization scheme q, then we have 852

$$R_{q} = \frac{1}{N} \sum_{j=1}^{N} \sum_{t \in \mathcal{T}'} \left[\sum_{a \in \mathcal{A}^{dep} \cup \mathcal{A}^{arr}} \max\left(0, \left(F_{j,a,t}^{q} - C_{j,a,t}\right)\right) + \sum_{s \in S} \max\left(0, \left(F_{j,s,t}^{q} - C_{j,s,t}\right)\right) \right]$$

$$(32)$$

where N represents the total number of simulated operation 856 scenarios, F j, a, tq and F j, s, tq denote 500 the number of 857

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flights at airport a and sector s during time period t under opti-858 mization scheme q, while $C_{j,a,t}$ and $C_{j,s,t}$ are the simulated 859 actual capacities at airport a and sector s during time period 860 t under optimization scheme q. 861

5.3.1. Robustness test results for base model

The base model corresponds to the scenario in the uncertainty 863 model where the violation probability is 0. Flight schedule data 864 obtained from its optimization is then compared with the 50 865 sets of capacity combinations generated in each experiment. 866 The robustness R_0 is then calculated and the statistical results 867 are shown in Fig. 8. It is evident that the robust model-868 optimized flight schedule is more robust than the original flight 869 schedule, as its R is substantially lower. This further confirms 870 that flight schedule optimization is essential to make the air 871 traffic system more stable and improve its resilience to various 872 uncertainties. 873

5.3.2. Robustness test results for uncertainty model

The base model is too conservative. Airport and sector capac-875 ity may be unused due to low scheduled traffic. The more 876 robust a flight schedule is, the higher the total cost. Based on 877 the robustness test, the optimal flight schedule robustness met-878 ric for Schemes 1-10 has been calculated. We compare the 879

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Fig. 6 Percentage of flights with arrival and departure slot displacement in each scenario.



Fig. 7 Runtime of models under different setting.

robustness of the uncertainty models with that of the base
model based on the robustness metric. Additionally, we also
compare the robustness between Method 1 and Method 2, as
well as the robustness of the optimal flight schedule for each
scheme within Method 1 and Method 2, to analyze the effect
of node importance and violation probability on the robustness of the models.

We can see from Fig. 9 that the optimal flight schedule for all schemes of Method 1 is less robust than the base model. The capacity restriction becomes more stringent as the probability of violation decreases, leading to a decrease in overcapacity and a more robust flight schedule. The results of the robustness test for each scheme of Method 1 are in line with the initial hypothesis. This implies that Method 1, which takes 893 into account capacity uncertainty, is less robust than the base 894 model. However, the base model sacrifices the total cost of the 895 flight schedule in order to achieve strong robustness. Fig. 10 896 897 shows that the total cost of the flight schedule for the robust scheme is approximately 35. 4%, 15. 6%, 9. 49%, 5. 38%, 898 and 4.05% of the base model, respectively. This indicates that 899 the base model incurs a considerable cost in its pursuit of 900 robustness, which may not be desirable to stakeholders. In 901 comparison, Method 1 achieves a significant reduction in the 902 total cost of the flight schedule by sacrificing a bit of robust-903 ness and appears to be more profitable. However, considering 904 that the optimization objective of the model in this paper is the 905

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Fig. 8 Comparison of robustness metric between original flight schedule and optimal flight schedule of deterministic model.

flight schedule at the airport network level, it is possible to
incorporate the structural characteristics of the network into
Method 1. This has the potential to result in obtaining a robust
flight schedule and reducing costs, thereby creating a model
better suited for optimizing the flight schedule at the airport
network level.

In an airport network, if there is delay or congestion at an 912 airport or sector with high average daily flow or closeness, it 913 can have a ripple effect on other downstream airports and sec-914 915 tors. To minimize the likelihood of this occurrence, Method 2 considers the importance of both the airport and the sector 916 nodes. This results in a smaller probability of violations for 917 important airports and sectors, leading to a robust flight 918 schedule with a low total cost sacrifice. The total cost of the 919 optimal flight schedule for all the schemes of Method 2 is sig-920



Fig. 9 Comparison of optimal flight schedule robustness metric by scheme.



Fig. 10 Comparison of total cost of optimal flight schedule by scheme.

nificantly lower than that of the robust model and Method 1, as seen in Fig. 10. Additionally, the overcapacity of the optimal flight schedule for almost schemes of Method 2 is higher than that of Method 1, as seen in Fig. 9. Considering the importance of the node in the model, incorporating it into the optimization model can result in a flight schedule that demonstrates strong resilience and minimizes overall cost. This, in turn, improves the efficiency of optimizing the flight schedule at the airport network level.

Further examination of Fig. 9 reveals two interesting findings: (A) we observe that the optimal flight schedule of Scheme 9 in Method 2 performs better in terms of robustness, even though the total cost is lower than that of Scheme 4 and 5 of Method 1 by 30.7% and 7.8%, respectively. This clearly shows the robustness and superiority of Method 2 compared 935

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to Method 1. Inclusion of the importance of the nodes in the 936 model has advantages for the optimization performance of 937 938 the model, making it more suitable for optimizing the flight 939 schedule at the airport network level. The results of the robustness metric comparison for the above schemes are shown in 940 Fig. 11. (B) The optimization performance of the model still 941 942 has room to improve. Fig. 11 shows the robustness metric for each scheme of Method 2. Since Scheme 7 has lower viola-943 tion probabilities, the optimized schedule should be more 944 robust. However, its robustness metric is not as good as those 945 of Schemes 8 and 9. We hypothesize that this is due to the com-946 bination of the probability of violation and the structural char-947 948 acteristics of the airport network. The importance value 949 cannot fully capture the importance of the sector or airport in the network. To further investigate this, we performed addi-950 tional experiments by adjusting the values of Eq. (27). The 951 maximum violation probability in Method 2 is set to 0.2, the 952 953 maximum violation probability ranged from 0.23 to 0.35 with 954 a step change of 0.03. In total, five sets of optimization experiments similar to Method 2 were conducted, with the only dif-955 ference being the combination of violation probability. 956

Table 8 presents the total cost and robustness of the flight 957 schedule. The data in the tables show that as the probability 958 of violation increases, the total cost of the optimal flight sched-959 960 ule from Scheme 6 to Scheme 10 decreases, but the robustness does not necessarily increase. The results for different values of 961 962 α demonstrate that the robustness of schemes with a high prob-963 ability of violation can be lower than that of schemes with a low probability of violation. Method 2 is more suitable for 964 flight schedule optimization at the airport network level than 965 Method 1, however, it does not take into account all the spe-966 967 cial points of the airport network. The combination of violation probability calculated by linear interpolation based on 968 node importance is probably not the optimal combination 969 970 for the corresponding schemes. This is evidenced by the lack 971 of a clear trend in the average robustness in Table 8.

5.4. Comparison with other method of setting violation probability

The importance of the sector node was determined using close-974 ness, while the importance of the airport node was assessed 975 based on the volume of traffic. In this section, we compare 976 the optimal results with an alternative approach that relies 977 on a different network metric to assess the importance of 978 nodes. Specifically, we use the degree of the node as the mea-979 sure of importance. The total cost and robustness of the results 980 under different optimization schemes are plotted in Fig. 12. 981 There is minimal variation in total cost resulting from two net-982 work metrics, with only a slight distinction observed in the 983 schemes S_6 and S_7 . However, there are clear discrepancies in 984 the robustness of the optimized schedule when using the two 985 different methods to set the probability of violations. Using 986 traffic and closeness metrics to assess the importance of nodes 987 can lead to a more resilient flight schedule compared to relying 988 solely on the degree of the network. The excess capacity at 989 each airport and sector is determined by employing Eq. (32) 990 In Fig. 13(a) and (b), the average number of flights surpassing 991 the capacity of airports or sectors is illustrated for various 992 optimization approaches. Among the airports, only ZBAA, 993 ZGSZ, and ZUCK exhibit more than 3 flights exceeding 994 capacity, while the majority of airports and sectors experience 995 fewer than 2 flights exceeding capacity. Sectors ZHHHAR01 996 and ZBAAAR15 show more than two flights surpassing sector 997 capacity when applying violation probability settings based on 998 closeness. Overall, the optimized flight schedules demonstrate 999 resilience to operational uncertainties. 1000

5.5. Discussion

We identified congested points in the air traffic network by using flight traffic data and capacity data. The level of congestion was measured with a number in the range of 0 to 1, with 1004



Fig. 11 Comparison of optimal flight schedule robustness metric.

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Table 8	Table 6 Total cost (robustness) for schemes in Method 2 with different maximum violation probability.											
α _{max}	S_6	S_7	S_8	S_9	S_{10}							
	$\alpha_{\min} = 0.05$	$\alpha_{min}=0.08$	$\alpha_{\min} = 0.11$	$\alpha_{\min} = 0.14$	$\alpha_{min}=0.17$							
0.20	61,200 (55.5)	27,400 (50.2)	18,600 (49.1)	16,000 (70.2)	13,900 (74.2)							
0.23	51,250 (64.1)	21,750 (54.3)	16,600 (65)	13,300 (74.3)	12,750 (82.8)							
0.26	47,750 (69.5)	19,650 (67.1)	15,100 (68.2)	11,900 (75.6)	10,700 (74)							
0.29	46,550 (73.8)	18,650 (56.9)	12,800 (85.6)	10,600 (78.1)	9650 (92.8)							
0.32	43,950 (90.3)	16,050 (86.8)	10,850 (77.3)	9250 (98.2)	8900 (96.8)							
0.35	41,450 (90.4)	14,750 (81.4)	10,250 (96.4)	8750 (98.1)	7350 (92.1)							



Fig. 12 Total cost and robustness of results under different optimization scheme.

higher numerical values indicating more congestion. Similar to 1005 R_a , we define $R_{a,w,t}$ as value of the level of congestion for node 1006 w at 15-minutes slot t of optimization scheme $q.R_{a,w,t}$ can be 1007 calculated by Eq. (33). The results of Scheme 10 are shown 1008 in Fig. 14. We see the optimized flight schedule of Scheme 10 1009 still has some congested airports and sectors. To achieve a 1010 flight schedule with fewer congested airports and airspace, 1011 increased robustness, and lower total cost, we can modify 1012 the probability of a violation of restrictions in airports and sec-1013 tors. However, depending solely on static data such as node 1014 importance to set the probability of violation of airports and 1015 sectors may not be an optimal strategy. It is challenging to 1016 1017 decide on the optimal combination of probability of violation, 1018 and congested nodes in the air traffic network should be taken 1019 into consideration to dynamically adjust the probability of vio-1020 lation of each chance constraint. To improve the probability of violation and the quality of the solution, it is possible to reduce 1021 the probability of violation at congested points and increase 1022 the probability of violation at points with a sufficient capacity 1023 margin. This can be done by "cutting the peak and filling the 1024 1025 valley", which can be further studied by monitoring the changes in the probability of the chance of violation of the 1026 constraints of each node, thereby exploring the trigger condi-1027 1028 tions and intrinsic mechanisms of the optimization dynamic of the airport network. $1029 \\ 1030$

$$R_{q,w,t} = \frac{1}{N} \sum_{j=1}^{N} \max\left(0, \left(F_{j,w,t}^{q} - C_{j,w,t}\right)\right), \quad \forall w \in A^{\operatorname{dep}} \cup A^{\operatorname{arr}} \cup S, t \in T'$$

(33) 1032

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Our research has practical implications in real-world sce-1033 narios. Critical sectors and airports can be identified using 1034 existing and predicted air traffic conditions, along with meteo-1035 rological data. Supported by air traffic flow management sys-1036 tems, the personnel involved in managing air traffic flow 1037 determines the permissible risk levels for key sectors and air-1038 ports. Subsequently, our model is capable of assigning the best 1039 departure times for each flight. In the future, the efficacy of the 1040 model could be improved through the application of machine 1041 learning and artificial intelligence technologies. 1042

6. Conclusions

The demand for air transport and the complexity of the air 1044 traffic system have both grown, leading to a number of uncer-1045 tainties in the implementation of flight schedules. This paper 1046 presents a new capacity uncertainty chance constraint model 1047 to address the flight schedule optimization problem at the air-1048 port network level. This model takes into account the capacity 1049 uncertainty of airports and sectors in the air traffic system and 1050 also innovatively incorporates the importance of network 1051 nodes into the model. The experimental data show that the tra-1052



Fig. 13 Robustness of airports and sectors.



Heatmap of congestion at airports and sectors in Scheme 10. (a) The congestion level of departure airports; (b) The congestion Fig. 14 level of arrival airports; (c) The congestion level of sectors.

ditional capacity uncertainty model is not sufficient to handle the uncertainty problem. The cost of having a reliable flight schedule is high. To address this issue and create a model with better optimization results, this paper takes into account the importance of the nodes in the airport network in the model. Compared to the deterministic model and the traditional capacity uncertainty model, the results show that our model can produce a more robust and lower total cost flight schedule through the appropriate setting of the chance constraint violation probability.

This study has the following limitations. First, due to the limitations of the current dataset, it is difficult to find the optimal combination of probability of violation. This, in turn, reduces the efficiency of the model. To improve the optimization performance, the dynamic data of the congested points in the airport network should be taken into account when adjusting the probability of violation. Second, the length of the slot discussed in this paper is 5 min. Reducing the slot to 1 min 1070

could provide more accurate results. However, this would also 1071 significantly increase the computational complexity of the 1072 model. Third, the sector minimum flight time for each flight 1073 should be varied, as this would make the flight schedule more 1074 practical. This is because the performance of the aircraft can 1075 vary greatly depending on the model of the plane being used. 1076 Therefore, the sector minimum flight time should be adjusted 1077 accordingly for each flight. Future research efforts should be 1078 made in two areas: (A) to develop algorithms based on artifi-1079 cial intelligence to generate representative airspace operation 1080 scenarios; and (B) investigating the unique optimization pro-1081 cess of the airport network. 1082

CRediT authorship contribution statement

Jianzhong YAN: Writing – original draft, Validation, Investi-1084 gation, Formal analysis, Conceptualization. Haoran HU: 1085 Writing - original draft, Software, Methodology, Investiga-1086

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tion, Formal analysis. Yanjun WANG: Writing - review & 1087 editing, Writing - original draft, Supervision, Project adminis-1088 1089 tration, Methodology, Investigation, Funding acquisition, 1090 Formal analysis, Data curation, Conceptualization. Xiaozhen MA: Methodology, Investigation, Formal analysis. Minghua 1091 HU: Investigation, Formal analysis. Daniel DELAHAYE: 1092 1093 Writing - review & editing, Writing - original draft, Methodology, Formal analysis. Sameer ALAM: Writing - review & 1094 editing, Writing - original draft, Investigation, Formal 1095 analysis. 1096

1097 Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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