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To cite this version:

Jianzhong Yan, Haoran Hu, Yanjun Wang, Xiaozhen Ma, Minghua Hu, et al.. Robust pre-departure scheduling for a nation-wide air traffic flow management. Chinese Journal of Aeronautics, 2024, 10.1016/j.cja.2024.08.054 . hal-04699251

HAL Id: hal-04699251 <https://enac.hal.science/hal-04699251>

Submitted on 16 Sep 2024

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Chinese Society of Aeronautics and Astronautics & Beihang University

Chinese Journal of Aeronautics

cja@buaa.edu.cn [www.sciencedirect.com](http://www.sciencedirect.com/science/journal/10009361)

FULL LENGTH ARTICLE

⁴ Robust pre-departure scheduling for a nation-wide air traffic flow management

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- 14 Received 29 March 2024; revised 24 April 2024; accepted 6 May 2024

15

17 **KEYWORDS**

- 19 Air traffic flow management;
- 20 Airport and airspace net-
-
- 21 work;
- 22 Capacity uncertainty;
- 23 Chance constraint;
- 24 Stochastic optimization

Abstract Air traffic flow management has been a major means for balancing air traffic demand and airport or airspace capacity to reduce congestion and flight delays. However, unpredictable factors, such as weather and equipment malfunctions, can cause dynamic changes in airport and sector capacity, resulting in significant alterations to optimized flight schedules and the calculated predeparture slots. Therefore, taking into account capacity uncertainties is essential to create a more resilient flight schedule. This paper addresses the flight pre-departure sequencing issue and introduces a capacity uncertainty model for optimizing flight schedule at the airport network level. The goal of the model is to reduce the total cost of flight delays while increasing the robustness of the optimized schedule. A chance-constrained model is developed to address the capacity uncertainty of airports and sectors, and the significance of airports and sectors in the airport network is considered when setting the violation probability. The performance of the model is evaluated using real flight data by comparing them with the results of the deterministic model. The development of the model based on the characteristics of this special optimization mechanism can significantly enhance its performance in addressing the pre-departure flight scheduling problem at the airport network level. ULL LENGTH ARTICLE
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> The 2018 International Civil Aviation Organization (ICAO) 27 statistics showed that 4.3 billion passengers were served by 28 air transport, a 6.1% increase from the previous year. $\frac{1}{2}$ Despite 29

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1. Introduction 26

Peer review under responsibility of Editorial Committee of CJA

<https://doi.org/10.1016/j.cja.2024.08.054>

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Please cite this article in press as: YAN J et al. Robust pre-departure scheduling for a nation-wide air traffic flow management, Chin J Aeronaut (2024), [https://doi.org/](https://doi.org/10.1016/j.cja.2024.08.054) [10.1016/j.cja.2024.08.054](https://doi.org/10.1016/j.cja.2024.08.054)

 the construction of new infrastructure to enhance the capacity and efficiency of air traffic systems, flight delays remain an issue due to unpredictable elements such as extreme weather. In 2018, the flight departure delays within Europe rose to 14.7 min per flight, a 2.3 min increase from 2017.² The imbal- ance between the capacity of the air traffic system and the demand for traffic is still the primary cause of flight delays. Consequently, optimization of air traffic operations is still a major area of research.

 A great deal of research has been conducted to improve the operational effectiveness of air traffic systems since the 1990s. From the investigation of the Ground Holding Problem (GHP) of single airports, multiairports and airport net-43 works, $3,4$ to the examination of the dynamic flow problem of 44 the network and the formulation of the uncertainty problem, $5,6$ researchers from all over the world have made remarkable advances in the air transportation field. Since 2010, researchers have been attempting to optimize the flight schedule in a way that is more beneficial to all parties, taking into account fair- ness.^{7–11} Furthermore, to create a more reliable flight schedule, the uncertainty factor in the airport network has also received attention.^{12–14} As research results continue to be enriched, sys- tematized integrated models have also been featured in many studies.15–17 Some researchers have shifted their focus from 54 the supply side to the demand side of air transport service.^{18,19} The use of mathematics and big data has also been explored to 56 optimize flight schedules.^{20–22} In recent years, a large body of literature has been developed around the topic of airport capacity and demand management.

 Air Traffic Flow Management (ATFM) is a key technique used by traffic management operators to balance the capacity of airports/airspace and air traffic demand. This has been a major area of research for many years. ATFM can be broken down into three stages: strategic ATFM, pre-tactical ATFM and tactical ATFM. Strategic ATFM begins several months before the day of operation and involves slot allocation and airspace organization. Pre-tactical ATFM can start from a week or a day before the day of operation, during which flight schedules may be adjusted. The tactical phase is usually the day of flight operation and the main activities include execut- ing the daily plan developed in the pre-tactical phase, and for- mulating and implementing tactical traffic flow management measures to address unexpected supply–demand imbalances. The implementation of ATFM involves airlines, airports, and air traffic control authority. For more than two decades, the concept of Collaborative Decision Making (CDM) has been explored around the world to enhance the effectiveness of ATFM. This concept has now been widely adopted in major airports and Airport CDM (A-CDM) has become a successful example of its application. A-CDM's operation process helps to reduce delays, improve punctuality, and optimize resource utilization. It provides an information sharing platform and decision-making mechanism for multiple parties in air trans- port, allowing them to optimize resource utilization while still meeting the interests of all parties. The specific process and the 85 16 milestones are illustrated in Fig. 1. 23 All parties involved share their latest information and plan to keep everyone main- taining the same situation awareness. Two important informa- tion provided by air traffic control for departure flights are the Target Take-off Time (TTOT) and the Target Start-up Approval Time (TSAT). More accurate and stable timing

information is vital to the successful implementation of A- 91 $CDM.$ 92

However, insufficient focus has been given to examining the 93 robust optimization of departure slots for all flights within the 94 aviation system. Although current research and decision mak- 95 ing tools can identify the best flight schedule for air traffic 96 management authorities, changes in departure slots may occur 97 due to unexpected events or operational constraints that affect 98 capacity in downstream sectors or airports. Such occurrences 99 are commonly observed in actual operational scenarios. If 100 the actual capacity is lower than the expected capacity, and 101 too many flights were scheduled during the period, then some 102 flights will not be able to take off as planned, resulting in flight 103 delays. On the other hand, if the actual capacity is higher than 104 the predicted capacity, for instance, the capacity of the affected 105 airport or airspace is quickly restored, the preassigned depar- 106 ture slots may have to be changed earlier to avoid wasting 107 capacity and unnecessary flight delays. In such situations, air- 108 lines have to rearrange their resources to facilitate earlier 109 departures, which could result in increased workload and cost. 110 One of the primary obstacles is making departure decisions 111 when faced with capacity uncertainty. There is still a deficiency 112 in methods for accurately forecasting airport and airspace 113 capacity. The second issue lies in the complexity of the air traf- 114 fic management system as a networked system, where modifi- 115 cations in operations at a specific sector or airport can 116 impact the operations of other airports and sectors within 117 the network. In instances where a hub airport's operational 118 capacity falls short of the anticipated level, traffic control 119 restrictions will affect both incoming and outgoing flights at 120 that airport. Over-scheduled flights have to be delayed, leading 121 to delays that will propagate through the entire air transporta- 122 tion network. Conversely, the repercussions of over-scheduling 123 are less significant at smaller airports with lower levels of traf- 124 fic. No research has been conducted to investigate the impact 125 of network effects on the optimized strategies in air traffic flow 126 management problems when using optimization techniques 127 that account for uncertainty in stochastic scenarios. 128 appe area of Gaussia.

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This paper investigates the pre-departure scheduling in the 129 tactical phase of air traffic flow management. Real-time data 130 are used to make optimal adjustments to the flight schedule 131 to enhance airport efficiency and punctuality. The contribu- 132 tions of our work are outlined below. First, a pre-departure 133 scheduling model is proposed which considers uncertain 134 capacity of airport and airspace to minimize the total cost of 135 flight delays. The chance constraint method is used to manage 136 the uncertainty of airport and sector capacity. Second, our 137 model takes the characteristics of air traffic network into 138 account while the computational results are compared with 139 the optimization results of the deterministic capacity model, 140 as well as the superiority of the capacity uncertainty model 141 considering the node importance over the traditional model 142 that only considers capacity uncertainty. This study is valuable 143 for improving the effectiveness of collaborative air traffic flow 144 management, and could have significant implications for 145 designing network control strategies in uncertain conditions. 146

This paper is organized as follows. Section 2 reviews the 147 existing literature on air traffic flow management, uncertainty 148 problems, and the chance constraint method. Section 3 pre- 149 sents a model for allocating uncertainty departure and arrival 150 slots flights at the airport network level and explains the trans- 151 formation of chance constraints. Section 4 examines the struc-
152

Fig. 1 Airport CDM milestones. A total of 16 key events during arrival and departure are marked as milestones.²³ Some critical time events are Calculated Take-off Time (CTOT), Actual Take-off Time (ATOT), Actual Landing Time (ALDT), Actual In-block Time (AIBT), Actual Commencement of Ground Handling Operations Time (ACGHOT), Target Off-block Time (TOBT), Aircraft Ready for Departure Time (ARDT), Aircraft Startup Requested Time (ASRT), Actual Start-up Approval Time (ASAT), Actual Off-block Time (AOBT), Actual Take-off Time (ATOT).

 tural characteristics of the national air traffic network and evaluates the importance of the airport and sector nodes. Sec- tion 5 introduces two methods to set the probability of viola- tion of chance constraints and provides experimental results. Section 6 is the conclusion.

158 2. Literature review

 The majority of the world's busiest airports experience signif- icant issues with traffic congestion and flight delays. Expand- ing airport infrastructure to increase capacity is a potential solution, but it is a lengthy and costly process that makes it dif- ficult to quickly solve the problem. An effective and practical alternative is air traffic flow management. In 1987, Odoni pro- posed a mathematical model for the first time to address the air traffic flow management problem. The model seeks to balance airport capacity and traffic demand, converting air delay into 168 ground delay, thus reducing the cost of flight operations. 24 Sig- nificant attention has been focused on researching air traffic flow management since that time. Comprehensive reviews of air traffic flow management can be found in Ref. 25–27. This section provides an overview of research conducted on pre- tactical and network-level tactical air traffic flow management. The studies can be categorized into deterministic traffic man- agement models and stochastic traffic management models, depending on whether they consider the future impact on air-port or sector capacity as deterministic or uncertain.

178 2.1. Deterministic air traffic flow management models

 The first research on ground holding strategies for air traffic flow management is discussed in Ref. 28, where a deterministic model is introduced for the holding of the ground in a single airport. The model takes into account the airport's capacity, which is determined by factors such as weather conditions (such as wind speed and visibility), to calculate flight departure times and delays. However, this model does not account for the ripple effect of delays spreading between successive flights of the same aircraft. In Ref. 3, a collaborative multi-airport ground delay model is proposed and a heuristic algorithm is developed to find a feasible solution in a reasonable time. This

study examines the ground delay strategies for a network of 190 airports where the impacts of delay propagation over time 191 are carefully considered. To account for both airport capacity 192 and sector capacity constraints, a $0-1$ integer program model is 193 developed.²⁹ Nevertheless, the model does not account for 194 flight rerouting and cancellations. Subsequently, the authors 195 proposed a dynamic network flow method to examine the 196 reroute issue within air traffic flow management. ⁵Lulli argued 197 that the circumstances in Europe are distinct from those in the 198 U.S. and proposed a deterministic dynamic model for Euro- 199 pean air traffic flow management.³⁰ A novel integer program- 200 ming model for solving large-scale air traffic flow problems are 201 presented in. 31 The model covers all the phases of flights, 202 including departure, cruising, and landing, and considers var- 203 ious regulatory actions such as ground delays, route changes, 204 speed adjustments, and airborne holding. It incorporates a 205 multivariable framework with three categories of constraints 206 to enhance relaxation conditions, enabling efficient resolution 207 of air traffic management scenarios comparable in size to the 208 entire United States. In a different research venue, a team of 209 researchers investigates air traffic flow management through 210 the use of Eulerian models. For example, a Eulerian model is 211 proposed in Ref. 32, which is based on the Cell Transmission 212 Model (CTM). This model operates under the assumption that 213 flights between specific Origin-Destination (OD) pairs can be 214 represented as paths, which consist of a sequence of links. 215 Each link corresponds to a sector, and these links are further 216 segmented into cells, where the average flight duration between 217 OD pairs defines the path length and each cell's length is con- 218 sidered as 1 min. In the Cell Transmission Model (CTM), the 219 state variable is the total count of aircraft in each cell during 220 every time interval, and the total aircraft count in a sector is 221 the aggregate of all aircraft across all cells within that sector. 222 This modeling approach pertains to the airway level, and the 223 model's dimensions are dictated by the network structure. 224 Another interesting work is in Ref. 33, where an Eulerian-
225 Lagrangian model is developed by taking into account the 226 departure and arrival fix information of the flights. A Linear 227 Transmission Model (LTM) has been created, and a method 228 for pairwise decomposition is introduced to discover the best 229 global solution (Cao and Sun³⁴). Similar to the CTM, this $\frac{230}{2}$ **Example 11**

Research Towards The media of the system during method of dependent and the media of the system of the system

 model can achieve the optimum outcome, yet it operates approximately six times faster than the CTM. The above men- tioned studies can determine the optimal air traffic flow man- agement strategies assuming that airport and sector capacities are fixed. However, these capacities are subject to change due to stochastic factors, such as weather, equipment malfunc- tions, and air traffic controller's personal capability. Several methods have been suggested to tackle the issue of stochastic air traffic flow management.

240 2.2. Stochastic air traffic flow management models

 In Ref. 35, a dynamic multi-stage stochastic integer program- ming model is introduced for a single airport. This model employs a scenario tree to depict the uncertain capacity, and as time progresses, the decision tree branches out to create numerous scenarios. Hoffman argued that single airport flow management does not take into account the connectivity between flights, which can lead to impractical situation due to the impact of previous flight. To deal with the unpredictabil-249 ity of airport capacity in ground delay programs, Liu et al. 36 developed an airport capacity scenario tree using historical 251 data on airport capacity distribution. Agustin et al.³⁷ devel- oped a multistage hybrid 0–1 programming model to solve the air traffic management problem, taking into account the uncertainty of the capacity of airports and sectors simultane- ously, as well as flight rerouting. Stochastic optimization has become a widely used method for dealing with optimization problems that involve uncertain parameters. The main idea behind is to minimize the risk of exceeding capacity constraints in cases where the probability distributions of the nodes are 260 understood. Bertsimas and Sim⁶ discussed the challenge of dealing with data uncertainty in the context of the network flow optimization problem. They introduced a robust opti- mization approach to tackle this uncertainty, allowing users to manage the level of constraint violation and consequently adjust the model's level of conservatism. However, when cost coefficients contain uncertainties, the 0–1 discrete optimization 267 problem on n variables requires at most $n + 1$ instances of the original problem to solve the robust counterpart, which is 269 computationally intensive. Janak et al.³⁸ proposed a novel robust optimization approach to address planning problems with bounded uncertainty. The model was implemented in real industrial cases to achieve dependable and resilient solutions. 273 Gupta et al.³⁹ proposed a robust optimization approach to tackle the uncertainty in air traffic flow management. How- ever, the model optimized the worst case of uncertain param- eters, resulting in an overly conservative and resource-wasteful allocation scheme. Clare and Richards⁴⁰ proposed a robust optimization method to solve the planning problem with bounded uncertainty, assuming that the future capacity prob- ability distribution information is known. They integrated a deterministic discrete decision mixed integer linear model with sector capacity violation probability constraints to create a chance-constrained model. However, The study employed a brute force algorithm to address the model, leading to compu- tational constraints and challenges in solving large-scale prac-286 tical issues. Chen et al.⁴¹ developed a chance-constrained air traffic flow management model by adding probabilistic con- straints to a deterministic integer programming model. The capacity information of the probabilistic sector is incorporated at traits how management
the concerning condition condition conditions condition and the scalar method of the scalar method in the scalar

within the chance constraints. A polynomial approximation 290 chance constraint optimization algorithm is developed, which 291 is capable of providing optimal traffic management scheme 292 with efficient computational speed. Scenarios generate method 293 is used to reduce the number of possible operation scenarios in 294 order to solve the chance constrained models. $42,43$ These 295 stochastic air traffic flow management models provide mathe- 296 matical frameworks used to optimize the flow of air traffic in 297 uncertain conditions, considering the random nature of factors 298 such as weather, aircraft delays, and airspace congestion. By 299 incorporating probability distributions and stochastic pro- 300 cesses, they aim to find optimal solutions that minimize delays, 301 fuel consumption, and overall system costs while ensuring 302 safety and efficiency. However, most of work consider only 303 one or a few sectors operating under uncertainty. Little atten- 304 tion is given to address the uncertainty of capacity in the whole 305 network. Moreover, no research has been conducted on estab- 306 lishing the thresholds for capacity violations, leaving air traffic 307 flow management staff to rely on their own expertise to make 308 decisions. 309

3. A chance constrained model for air traffic flow management 310

3.1. Model framework and assumptions 3.1

The overall structure of the model is illustrated in Fig. 2. It \qquad 312 takes into account the capacity of airports and sectors, flight 313 plans, and the predetermined probability of violation at the 314 airport/sector. Each flight plan includes the departure airport, 315 destination airport, planned departure time, planned arrival 316 time, list of sectors, and the associated flying time for travers- 317 ing each sector, turnaround time at the airport, etc. The model 318 optimizes the departure time and arrival time for each flight to 319 ensure that the traffic demand and capacity are balanced. We $\frac{320}{2}$ use five-minute intervals as the time unit. Due to the data con- 321 straints, we assume that each flight can pass through the sector 322 with the minimum sector flying time. In future work, we can 323 consider variable flying times for different flights. 324

3.2. Description of notations 325

The sets, parameters and variables used in the model are given 326 in Tables $1-4$. 327

3.3. Objective function 328

The aim of the model is to reduce the total cost of flight delays. 329 Flight delay is defined as the time difference between its sched- 330 uled time of operation and its actual time of operation. It 331 should be noted that the departure displacement includes both 332 ground delays and early departures. The objective function is 333 represented in Eq. (1) :

$$
Q = \min \left(\sum_{f \in F_{\text{wait}}, a = O_f} \beta \left| t - t_f^{\text{dep}} \right| X_{f, a, t} + \sum_{f \in F} \theta y_f Y_f \right) \tag{1}
$$

The cost in the objective function consists of two parts. The 338 first part is the cost of adjusting the departure slot for depar- 339 ture flights as expressed as \sum $\sum_{f \in F_{\text{wait}}, a = O_f} \beta \left| t - t_f^{\text{dep}} \right| X_{f, a, t}$, and the second part, Σ $\theta y_f Y_f$, is the cost of air delays for all flights.

341

340

335

^ð1^Þ ³³⁷

 $f \in F$

Fig. 2 Model framework.

Table 1 Sets of model.

 Operators and managers prefer to keep flights on the ground rather than in the air, as this increases fuel consump- tion and the chances of unsafe events. Based on previous stud-345 ies on the study of Ground Delay Program(GDP),^{44,45} this paper sets the cost ratio of airborne delay to ground delay as 2:1. For simplicity, the cost of one unit of airborne delay is 100, and for ground delay it is 50.

349 3.4. Deterministic model constraints

350 The constraints of the model are capacity constraints, flight 351 connection constraints, and flight time constraints. Eq. (2) to 352 Eq. (21) are the constraints of the model.

353 (1) Constraints for the flights in the air

 (11)

 $40⁵$

$$
\sum_{t \in T} t^* X_{f,a',t} - \sum_{t \in T} X_{f,a,t} - t_f^{\text{fly}} \leq U, \forall f \in F, (a, a') \in A'_f
$$
\n
$$
(12) \qquad \qquad 410
$$

 $W_{f,S_{f,s}^{\text{next}},t+\int_{f,s,\min}^{\text{fly}}}\leqslant W_{f,s,t}, \forall f\in F, s\in S_f', t\in\left[T_{\min}, 287-t_{f,s,\min}^{\text{fly}}\right]$

$$
\sum_{t \in T} t^* X_{f,a',t} - \sum_{t \in T} X_{f,a,t} - t_f^{\text{fly}} = y_f, \forall f \in F, (a, a') \in A'_f
$$
\n(13)

$$
y_f \ge 0.5 - M^*(1 - Y_f), \forall f \in F
$$
 (14) 416

$$
y_f \leqslant 0.5 + M^* Y_f, \forall f \in F \tag{15}
$$

420 (3) Airport and sector capacity constraints 421

422

425

428

434

456

414

417

Eqs. (17) – (21) ensure that traffic at the airport or sector will 423 not exceed its capacity.

$$
W_{f_2, a_2, t+V} \leq W_{f_1, a_1, t}, \forall (f_1, f_2) \in P, (a_1, a_2) \in P', t \in [0, 287 - V]
$$
\n
$$
(16)
$$
\n
$$
427
$$
\n
$$
(16)
$$
\n
$$
427
$$

$$
\sum_{t=3t}^{3t+2} \sum_{f \in F_a^{\text{dep}}} X_{f,a,t} \leq \lambda_{a,t}^{\text{dep}}, \forall a \in A^{\text{dep}}, t \in \left[\frac{T_{\text{min}}}{3}, \frac{T_{\text{max}}}{3} + 12\right] \tag{17}
$$

$$
\sum_{t=3t}^{3t+2} \sum_{f \in P_a^{\text{arr}}} X_{f,a,t} \le \mu_{a,t}^{\text{arr}}, \forall a \in A^{\text{arr}}, t \in \left[\frac{T_{\text{min}}}{3}, \frac{T_{\text{max}}}{3} + 12\right] \tag{18}
$$

$$
\sum_{t=3t}^{3t+2} \left(W_{f,s,t} - W_{f,S_{f,s}^{\text{next}},t} \right) \geqslant 0.5 - M^* \left(1 - b_{f,s,t} \right),
$$
\n
$$
\forall f \in F_s, s \in S, t \in \left[\frac{T_{\text{min}}}{3}, \frac{T_{\text{max}}}{3} + 12 \right] \tag{19}
$$

$$
\sum_{t=3t}^{3t+2} \left(W_{f,s,t} - W_{f,S_{f,s}^{\text{next}},t} \right) \leq 0.5 + M^* b_{f,s,t},
$$
\n
$$
\forall f \in F \quad s \in S \quad t \in [\frac{T_{\text{min}}}{2} \quad \frac{T_{\text{max}}}{2} + 12] \tag{20}
$$

$$
\forall f \in F_s, s \in S, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]
$$
\n
$$
439
$$
\n
$$
440
$$

$$
\sum_{f \in F_s} b_{f,s,t} \leq \varphi_{s,t}, \forall s \in S, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]
$$
\n(21)

3.5. Chance constraints 443

3.5.1. Establishment of chance constraints 444

Chen et al. 41 proposed a chance constrained model to address 445 the problem of Air Traffic Flow Management (ATFM) under 446 uncertainty. The main idea is to replace sector capacity con- 447 straints in the Integer Programming optimization model with 448 probabilistic constraints. That is the capacity of a sector can 449 be exceeded with a given probability. Here, we extend their 450 work to consider both stochastic capacity at airports and sec- 451 tors. Therefore, Eq. (17) , Eq. (18) , and Eq. (21) are replaced by 452 Eq. (22) : 454

$$
P\left(\begin{array}{l}\sum_{t=3t}^{3t+2} \sum_{f\in F_a^{\text{dep}}} X_{f,a,t} \leq \lambda_{a,t}^{\text{dep}}\\ \sum_{t=3t}^{3t+2} \sum_{f\in F_a^{\text{err}}} X_{f,a,t} \leq \mu_{a,t}^{\text{arr}}\\ \sum_{f\in F_s} b_{f,s,t} \leq \varphi_{s,t}\end{array}\right) \geq 1 - \alpha.
$$
\n(22)

Indirect decision	Description
variable	Binary variables, where 1 indicates at slot <i>t</i>
$b_{f,s,t}$	Binary variables, where 1 indicates at slot <i>t</i>
f differ f is in sector <i>s</i> , otherwise	
$0, f \in F, s \in S_f, t \in T_1$	
y_f	integer variables, where positive numbers
indicate flight f occurred air delay, otherwise	
Y_f	Binary variables, where 1 indicates flight f
occurred air delay, otherwise $0, f \in F$	

Table 4 Indirect decision variables of model.

355 Eq. (2) ensures that the decision variable $X_{f,a,t}$ and for 356 flights that are in the air is equal to its actual departure time. 357 Eq. (3) ensures that the decision variable $W_{f,s,t}$ can for flights 358 that are in the air is equal to its actual entry time of each sector 359 it traverses. Eq. (4) ensures that the decision variable $W_{f,s,t}$ is ³⁶⁰ not decreasing. ³⁶¹

363
$$
X_{f,a,t} = 1, \forall f \in F_{\text{fly}}, a = O_f, t = t_f^{\text{dep}}
$$
 (2)

366
$$
W_{f,s,t} = 1, \forall f \in F_{\text{fly}}, s \in S_{f,T_{\text{min}}}^{\text{by}}, t \in \left[t_{f,s}^{\text{in}}, 287 \right]
$$
 (3)

$$
W_{f,s,t-1} \leqslant W_{f,s,t}, \forall f \in F, s \in S_f, t \in [1,287]
$$
\n⁽⁴⁾

372
$$
X_{f,a,t} = W_{f,s,t} - W_{f,s,t-1}, \forall f \in F, a \in A_f, s = a, t \in [1, 287]
$$
 (5)

374 (2) Flight operational constraints

 Eq. (5) expresses the relation between the decision variables $X_{f,a,t}$ and $W_{f,s,t}$. When $X_{f,a,t} = 0$, this means that the flight f has not left the airport a in the slot t. In this case, $W_{f,s,t}$ can be not left the airport a in the slot t. In this case, $W_{f,s,t}$ can be either 0 or 1. If a is an arrival airport, Eq. (6) ensures that all flights have unique departure and arrival slots. Eq. (7) 381 ensures that flights do not arrive earlier than T_{min} . Eq. (8) guar- antees that the maximum departure delay does not exceed 3 h. Eq. (9) ensures that flights arrive no more than 1 h ahead of schedule. Eq. (10) ensures that connecting flights must meet the minimum connection time requirement. Eq. (11) ensures that flights meet the sector minimum flying time. Eqs. (12)– (15) are the air delay of the flight and make sure that the max- imum air delay does not exceed 1 h. Eq. (16) guarantees that transit time for connecting flights is not less than 30 min. ³⁹⁰ Fr. 1987 and Fr. 2 (14 and the decision variable $X_{r,s}$ and K_r and $X_{r,s}$ and K_r and $X_{r,s}$ an

$$
\sum_{t \in T} X_{f,a,t} = 1, \forall f \in F, a \in A_f
$$
\n
$$
393 \tag{6}
$$

395
$$
\sum_{t=T_{\min}}^{287} X_{f,a,t} = 1, \forall f \in F_{\text{fly}}, a \in D_f
$$
 (7)

398
$$
\sum_{t=T_{\min}}^{f_f^{\text{dep}}+L} X_{f,a,t} = 1, \forall f \in F_{\text{wait}}, a \in O_f
$$
 (8)

$$
\sum_{t=\ell_j^{err}-K}^{287} X_{f,a,t} = 1, \forall f \in F, a \in D_f
$$
\n(9)

404
$$
\sum_{t \in T} t^* X_{f,a,t} \leq \sum_{t \in T} t^* X_{f,a',t}, \forall f \in F, (a, a') \in A'_f
$$
 (10)

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 This model enumerates all potential combinations of air- port and sector capacities, and chooses the capacity combina- tion that meets the violation probability. It creates a feasible set of capacity combinations, which is also the feasible set of node traffic allocations. The optimal allocation scheme is the solution in the feasible set that has the best objective function 463 value.

 The most accurate solution to the chance constraint model can be determined by enumerating all possible combinations of capacities. However, as the number of airports and sectors increases, the computational complexity increases drastically. This type of constraint model has difficulty in finding the opti- mal solution for large-scale problems. Therefore, we transfer the joint constraints into individual constraints based on the 471 Bonferroni conservative approximation.⁴⁶ Thus, this article improves the chance constraint method by setting the proba- bility of violation for a single node instead of the joint distri- bution for a number of nodes. Doing so will enhance the computational speed of the model and allow for the cus- tomization of node violation probabilities according to the sig- nificance of nodes in the air traffic network. As a result, this will lead to more beneficial and logically optimized strategies. The capacity constraints in our chance constraint model are 480 expressed in Eqs. (23) – (25) :

$$
P\left(\sum_{t=3t}^{3t+2} \sum_{f \in \mathcal{F}_a^{\text{dep}}} X_{f,a,t} \leq \lambda_{a,t}^{\text{dep}}\right) \geq 1 - \alpha_a, \forall a \in \mathcal{A}^{\text{dep}}, t \in \left[\frac{T_{\min}}{3}, \frac{T_{\max}}{3} + 12\right]
$$
\n483 (23)

$$
^{484}
$$

 $\left(\sum_{t=3t}^{3t+2} \sum_{f \in F_a^{\text{arr}}} X_{f,a,t} \leq \mu_{a,t}^{\text{arr}}\right) \geq 1 - \alpha_a, \forall a \in A^{\text{arr}}, t \in \left[\frac{T_{\text{min}}}{3}, \frac{T_{\text{max}}}{3} + 12\right]$ 486 (24) 487

 $P\Big(\sum_{i=1}^{3t+2}$ $t=3t$ \sum

 $P\vert\sum$ $f \in F_s$

 $\frac{489}{25}$

490 3.5.2. Transformation of chance constraints into deterministic 491 constraints

 $\left(\sum_{f\in F_s}b_{f,s,t}\leqslant \varphi_{s,t}\right)\geqslant 1-\alpha_s, \forall s\in S, t\in \left[\frac{T_{\min}}{3},\frac{T_{\max}}{3}+12\right].$

 In this section, we show how to convert the chance constraints 493 expressed in Eqs. (23) – (25) into deterministic constraints. As an example, the four capacity scenarios of a sector s are pre-sented in Table 5.

496 The first row in Table 5 shows the capacity value $(\varphi_{s,t})$ of 497 the sector s for each scenario; the second row displays the 498 probability $(PC_{s,t})$ of the capacity in each scenario; the third
499 row presents the cumulative probability (PC^{sum}) of the sector. 499 row presents the cumulative probability $(PC_{s,t}^{\text{sum}})$ of the sector. 500 Let n be the scenario number $n \in \{1, 2, 3, 4\}$. The cumulative

probability of scenario n indicates the proportion of scenarios 501 with capacity values less than scenario n . It establishes the con- 502 nection between the chance constraint and the deterministic 503 capacity constraint by considering the probability of violation. 504 The following example demonstrates the specific transforma-

505 tion process. 506

For example, if the probability of violation in sector s is 507 0.05, then it means that the maximum allowable flow is the 508 quantile 5% of all possible capacity scenarios. Since the sce-
509 nario with capacity of 5 is in the quantile 0% to 10% , the 510 probability of violation of 0.05 is within the cumulative prob- 511 ability of Scenario 1 and Scenario 2. Therefore, the chance 512 constraint can be changed into a deterministic constraint that 513 traffic flow is less than or equal to 5. When the probability of 514 violation is 0.95, the maximum allowed traffic is in the 95% 515 quantile of all possible capacity scenarios. Since the capacity 516 in Scenario 4 is in the 80% to 100% quantile, the chance con- 517 straint can be converted into a deterministic constraint with a 518 flow less than or equal to 8. Given the empirical distribution of 519 sector capacity, it is essential to ensure that converting a 520 chance constraint into a deterministic one closely to the origi- 521 nal situation. Thus, for sector s in the time slot t, a chance con-
522 straint with a probability of violation 95% can only be 523 translated into a deterministic constraint where the flow is less 524 than or equal to 8 . In the determinist operator and spin allowsky conducts and spin allowsky scales and the spin allowsky scales and the spin allowsky in the spin allowsky scales and the spin allowsky in the spin allowsky in the spin allowsk

$$
P\left(\sum_{f\in F_s} b_{f,s,t} \leqslant \varphi_{s,t}\right) \geqslant 1 - \alpha_s = \begin{cases} \sum_{f\in F_s} b_{f,s,t} \leqslant 5, & 0 \leqslant \alpha_s \leqslant 0.1\\ \sum_{f\in F_s} b_{f,s,t} \leqslant 6, & 0.1 < \alpha_s \leqslant 0.4\\ \sum_{f\in F_s} b_{f,s,t} \leqslant 7, & 0.4 < \alpha_s \leqslant 0.8\\ \sum_{f\in F_s} b_{f,s,t} \leqslant 8, & 0.8 < \alpha_s \leqslant 1 \end{cases}
$$
(26) 528

4. Characteristics of air traffic flow network 529

Due to its important role in moving passengers and cargo, the 530 properties of the air transportation network have become a 531 significant subject of study within the network science field. 532 Early studies have investigated the structural features of air 533 transport networks. For instance, Guimerà et al. examined 534 the structure of worldwide air transportation network. 47 These 535 networks, whether global or national, exhibit the characteris-
536 tics of scale-free small-world networks. Subsequently, the 537 emphasis of research shifted towards analyzing vital nodes 538 and fundamental characteristics of the network. Given that 539 connectivity patterns influence diffusion phenomena (such as 540) flight delays and epidemics) across the network, understanding 541 the function and essential elements of the network is crucial. 48 $$ 542 Earlier research has demonstrated that reductions in capacity 543 at various airports affect the overall performance of air trans- 544 port systems differently.^{49,50} Motivated by these findings, it is 545 hypothesized that the characteristics of the network play a role 546 in determining probabilistic constraints and optimization 547 approaches. 548

To illustrate how flights operate in the air transportation 549 system, Fig. 3 presents a two-layer air traffic flow network. 550 The bottom layer represents the airport network, where the 551 nodes represent the airports, and the edges represent the sched- 552 uled direct flights connecting the airports. The upper layers are 553

526

8 **S J. YAN** et al.

554 the sector network, where the nodes are the sectors, and the 555 edges represent the flow of flight traffic between the two sec-556 tors. Arrows connect that airport and the sector in the two net-557 works, indicating the traffic flow between the airport and the (3) Betweenness centrality. Betweenness is to measure the 593 influence of the node v over traffic flow between other 594 node. Betweenness centrality is defined as 595

596 597

607

$$
C_{\mathbf{B}}(v) = \sum_{i \neq v \neq j} \frac{\sigma_{ij}(v)}{\sigma'_{ij}} \tag{29}
$$

where σ_{ii} is the total number of shortest path from node i to 600 node *j*, and $\sigma_{ij}(v)$ is the number of those paths that pass 601 through node *v*. through node v .

(4) Closeness centrality. Closeness centrality is a measure 603 that quantifies how close a node is to all other nodes 604 in a network. Mathmatically, closeness centrality is 605 defined as 606

$$
C_{\rm C}(v) = \frac{n-1}{\sum_{u} d(v, u')} \tag{30}
$$

where $d(v, u)$ is the shortest path length from node v to node u. 611
The importance of nodes in a network can be evaluated

The importance of nodes in a network can be evaluated using metrics such as degree, betweenness, and closeness. 613 The degree could reflect the potential for interaction between 614 the node and other nodes in the network. However, we should 615 note that the importance of a node is not solely determined by 616 its degree value, but also by the degree values of its neighbor- 617 ing nodes. Betweenness was originally proposed to measure the 618 social status of a node, as it is determined by the number of 619 shortest paths that pass through it. Closeness is a measure of 620 the proximity of a node to other nodes in the network, with 621 a higher value indicating that the node is closer to other nodes 622 and its information will spread more quickly. When it comes to 623 air traffic, flight delays can spread throughout the system, lead- 624 ing to further delays. To reduce the amount of delays, it is 625 essential to first minimize the initial delays, and then manage 626 the propagation of delays in the network. Therefore, it is 627 important to assess the importance of nodes in sector net- 628 works. Closeness could be a suitable measure for the sector 629 nodes. Nodes with higher closeness should have a lower chance 630 of exceeding capacity, which would control the initial delay 631 generated by important nodes and thus limit the spread of 632 delays in the network. 633 ato different scores cand of which will be manged to one of which will be mainly in the mail of the same structure in the same of the sam

Airports, which are the beginning and end points of the air 634 traffic management system, differ from sectors. Therefore, it is 635 not appropriate to use the same network topology metric to 636 assess their importance. To this end, the airport network G^{\int} 637 is created with all airports as nodes and a link between two air- 638 ports if there is a scheduled traffic flow between them. The 639 degree of the airport node reflects the number of cities served 640 by the airport, but the traffic volume of the airport with high 641 degree is not necessarily large. For example, the node degrees 642 of ZBTJ(Tianjin) and ZLXY(Xi'an) are approximately equal, 643 however, the flight volume of ZLXY is almost twice as much 644 as that of ZBTJ. This means that ZLXY has a higher traffic 645

volume, making it more prone to delays. Furthermore, due 646 to the larger number of flights, ZLXY flight delays are more 647 likely to spread to other airports through the network. More- 648 over, a prior research on the resilience of the airport network 649 has indicated that the traffic volume of airports is the most reli- 650 able indicator of the effect of a disturbance on network effi- 651

sectors. Several studies have investigated the structural charac-
teristics of avation networks. Most networks have airports as
nodes and a link connects two airports if there is a flight oper-
ating between them.⁵¹ In real operation, the airspace is divided
into different sectors, each of which will be managed by one or
two air traffic controllers.⁵¹ To capture the operational charac-
teristics of the air traffic network, the sector network is repre-
sented as a graph
$$
G^{\int} = (N^{\int}, E^{\int})
$$
, where N^{\int} is the set of
nodes and E^{\int} is the set of edges. Nodes *n* (*n* ∈ *N* ^{\int}) of the net-
work G^{\int} are airports and sectors, while an edge *e* (*e* ∈ *E*) is
added between two nodes if there is traffic between them. In
this paper, an edge e represents direct flight connections
between a sector and a sector (or an airport). Let A^{\int} be the
adjacency matrix of the network G^{\int} , with each element a_{ij} rep-
resenting the relationship between node *i* and *j*. For example,
in an undirected, unweighted network, if there is an edge
between *i* and *j*, then $a_{ij} = 1$; otherwise, $a_{ij} = 0$. To measure
the importance of nodes in the network, we introduce the fol-
lowing metrics.

 (1) Degree and degree distribution. The degree of a node v is denoted as k_n , which is defined as the number of edges connected to that node. In an undirected network G, the degree of node v is calculated as

581 582

$$
k_{\nu} = \sum_{u} a_{\nu, u} \tag{27}
$$

585 The degree distribution is often represented as a histogram, 586 showing the count of nodes for each degree.

587 (2) Degree centrality. The degree centrality is defined as

588 589

591 $C_{\text{D}}(v) = \frac{k_v}{\max \text{deg'}}$ (28)

 592 where max_d eg is the maximum degree in the network.

Fig. 3 Air traffic network. The bottom layer is the airport network with the size of node indicating the traffic volume at the airports. The upper layer in the sector network.

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 652 ciency.⁵⁰ Therefore, we use traffic volume as a metric to eval-653 uate the importance of airport nodes.

 To further calculate the importance of the nodes, we use the standard max–min normalization method to transfer the orig- inal node important metric data into the range (0, 1). Fig. 4 plots the importance of sector nodes and airport nodes. The names of sectors are shown in the upper X-axis, while the names of the airports are shown in the bottom X-axis. The sec- tors whose closeness are smaller than 0.209, are assumed to have enough capacity handling additional flights. These sectors are mostly located at the periphery of the network, and the probability of delay caused by these sectors is low. Thirty- eight of these airports have an average daily flights of more than 200, while the remaining airports have a smaller average daily flights and a low probability of traffic exceeding airport capacity. Thus, it is assumed that the capacity of these airports is always enough to meet traffic demand.

669 5. Case study

670 5.1. Experimental setup

671 5.1.1. Data

 We examine the effectiveness and performance of our model by comparing the optimized results with those obtained from the deterministic model. The flight schedule from 9:00 am to 12:00 pm on August 1, 2018 is used as input data for the mod- els. During this period, there were 3435 flights. At 9:00AM, 1156 flights were in the air, while 2279 were still on the ground.

Fig. 4 Importance indicator of sectors and airports. The importance of airports is determined by assessing their significance through traffic volume. Similarly, the importance of sectors is determined by evaluating their significance through closeness centrality.

The air traffic network consists of 195 airport nodes and 188 678 sector nodes. The sector network is formulated based on air-
679 space data from the Air Traffic Management Bureau. Estima- 680 tion of the capacity of an airport or of a sector is a complex 681 task, which is beyond the scope of this study. The airport 682 capacity is provided by the air traffic control authority in the 683 form of declared airport capacity. Statistical results indicate 684 that hourly arrivals/departures of the airport vary between 685 40% and 70% of its declared capacity. Therefore, we use 686 60% of the airport declared capacity as departure capacity 687 and arrival capacity. As there is no data available on the 688 capacity of the sector, the sector capacity is determined as 689 the 50th percentile of the past traffic volume moving through 690 the sector. The primary goal of this study is to investigate 691 the efficiency and benefits of using a chance constrained model 692 in air traffic flow management when faced with uncertainty, 693 taking into account the structural characteristics of the air traf- 694 fic network. It is assumed that the precise determination of air-
695 port and sector capacities does not significantly influence this 696 research. Further validation efforts can be conducted using 697 more realistic capacity data. 698

5.1.2. Optimization schemes 699

We evaluate ten different optimization strategies in addition to 700 the baseline (deterministic) model to compare the performance 701 of our chance-constrained models. These ten optimization 702 schemes are divided into two groups: (A) Method 1: Chance- 703 constrained model with equal probability of violation for all 704 airports and sectors; and (B) Method 2: Chance-constrained 705 model with the probability of violation setting based on the 706 importance of the node. In the base optimization scheme 707 (S_0) , all constraints in the worst-case scenario model must be 708 satisfied. This means that optimized traffic must not exceed 709 airport or sector capacity in all possible scenarios. $\frac{710}{2}$

In fact, the operational capacity of airports or sectors is 711 stochastic, which means that traffic flow may exceed a given 712 capacity limit at some points. To account for this, we allow 713 capacity constraints to be violated with a small probability. 714 To set this probability, we used two different approaches. 715 The first is to set all nodes with the same probability of viola-

⁷¹⁶ tion. If this probability is set too high, it could lead to airport 717 and airspace congestion and large flight delays in actual oper- 718 ations. However, if set too low, the optimized schedule may be 719 more robust to various operating scenarios, but the limited air-
 $\frac{720}{200}$ port capacity may be underused. To balance capacity utiliza- 721 tion and robustness to optimization, we set five schemes 722 $\alpha \in \{0.05, 0.08, 0.11, 0.14, 0.17\}$ which are referred to as S_1 to 723
S₅, respectively. We suggest a second approach that takes into 724 $S₅$, respectively. We suggest a second approach that takes into account the characteristics of the air traffic network. Small dis- 725 turbances that occur at a critical airport or sector can cause 726 long unforeseen delays throughout the network. Therefore, 727 optimized traffic flow must be more resilient to uncertainty 728 in these airports and sectors, and operations strategies should 729 be more conservative. We propose a method to set the proba-

⁷³⁰ bility of violation for airports and sectors, which takes into 731 account the importance of the airport or sector. For simplicity, 732 we use the term "node n" to refer to an airport or a sector. 733

Let H_n be the importance value of node *n*, then 734 $Max_{ix} = max{H_n}$ and $Min_{ix} = min{H_n}$ are the maximum 735 importance value and the minimum importance value of all importance value and the minimum importance value of all

737 nodes. The probability of violation $\alpha_{n,i}$ of the optimization 738 scheme *i*th, $i \in \{6, 7, 8, 9, 10\}$ is calculated as follows:

$$
\alpha_n^i = \alpha_{n,\min}^i + \left(\alpha_{n,\max}^i - \alpha_{n,\min}^i\right) \frac{\max_{x \sim H_n}}{\max_{x \sim \text{Min}_{x\sim}} (31)}
$$

 where $\alpha_{n,\text{max}}^i$ and $\alpha_{n,\text{min}}^i$ are the predetermined violation proba- bilities for the nodes with the maximum importance value and the minimum importance value. Here, $\alpha_{n,\text{max}}^i$ are set to 745 0.20, while $\alpha_{n,\text{min}}^i$ are set to $\{0.05, 0.08, 0.11, 0.14, 0.17\}$, corre-746 sponding to the schemes S_6 to S_{10} respectively. Table 6 pre-747 sents data regarding the probablity of violation α for each optimization scheme. The algorithms are coded in Python and Groubi, and are executed on a computer equipped with a 32 GB RAM and a 12th Gen Intel(R) Core(TM) i7-12700 Cpu (2.10 GHz).

752 5.2. Results

753 5.2.1. The total cost for each optimization scheme

 Table 7 shows the total cost of and the computation time for obtaining the optimal flight schedule under the optimization 756 schemes from S_0 to S_{10} . The total cost of the optimal solution for the base model is 416450, with 13.2% of this cost being attributed to air delay and 86.8% to ground slot displace- ments. In the optimized schedule, 64.9% of the flights are assigned their scheduled departure time, and 35.1% are delayed (98.7%) or depart earlier (1.3%). In contrast, 81.1% of the arrival flights are not assigned their original scheduled arrival slot, with 42.8% being delayed and 57.2% assigned ear- lier slots. This is likely due to the fact that airlines adding buf- fer time to their scheduled blocked time to account for potential flight delays.⁵²

 In uncertainty scenarios, the total delay cost decreases as the probability of violation increases for both the random set- ting and the importance-based node setting. This is because an increase in the capacity chance constraint violation probability enlarges the feasible domain of the model solution, prompting the model to search for a flight schedule with a lower total cost. Since excessive air delay can cause airspace congestion and air traffic safety concerns, the unit cost of air delay is higher than the unit cost of ground delay in the objective function setting of the model. This leads to the ground delay being greater than the air delay. Generally, the optimization results based on Method 2 are better than those of Method 1. The variation is smaller, indicating greater stability. As the probability of violation increases, the percentage of flights experiencing flight delay decreases in all schemes in Method 1. Method 2, how- ever, has a concentration of 6.9%-13.6% of departure flights with delays, and as capacity constraints become more relaxed, the percentage of departure flights delayed decreases. It is evi- dent that the percentage of departure flights that are delayed in U.S. which was the unit qualitation of the determining the state of the Control of the

Method 2 is much lower than that in Method 1. The results 786 show that about 90% of the departure flights depart on time. 787 In comparison, the proportion of flights with delayed arrival 788 flight is higher. Method 1 and Method 2 generally do not have 789 a clear increasing or decreasing pattern but with an overall 790 downward fluctuate. 791

In Fig. 5, we plot the number of slot displacements for arri- 792 val and departure flights in each optimization scheme, while 793 Fig. 6 further shows the ratio of slot forward and slot back- 794 ward displacement. We observe that in the departure flight slot 795 displacement, the slot forward displacement maintaining 796 numerical stability and the slot backward displacement 797 decrease with the increase in violation probability. The back- 798 ward displacement of the departure slot for all scenarios is 799 almost always greater than the forward displacement, and 800 the numerical change in the backward displacement is also sig-
801 nificantly greater than that of the forward displacement. In the 802 flight arrival slot displacement, the slot backward displacement 803 is much smaller than the slot forward displacement, and its 804 proportion is continuously decreasing and approaching zero. 805 The forward displacement of the slot determines the direction 806 of the departure slot for the flight. 807

The runtime of the optimization model using various 808 schemes are displayed in Fig. 7. Our scenario involves 3435 809 flights, 195 airports, and 188 sectors. Traffic characteristics 810 are comparable to those examined in, 41 although our network 811 is substantially larger (up to 20 sectors in their work). Our 812 model was executed using a desktop computer equipped with 813 a single 12th Gen Intel(R) i7-12700 CPU running at 814 2.10 GHz and 32 GB of RAM, whereas the model presented 815 in the study by Chen et al. was run on a Spark Cluster consist- 816 ing of 6 nodes, with each node containing an 8-processor CPU. 817 While it is not possible to directly compare the computational 818 complexities of the two studies, our model can be successfully 819 solved within a 20-minute timeframe for all optimization 820 schemes, with the exception of S_6 and S_7 . 821

5.3. Robustness tests 822

In Section 5.2, we compare and analyze the total cost, the pro- 823 portion of flights that experience slot displacements, and the 824 amount of slot displacement for arrivals and departures. As 825 expected, the total expected cost would decrease as the proba- 826 bility of violation increases. The reason for this is the inclusion 827 of additional "predicted" capacity resources to meet traffic 828 demand. There is a potential risk when expanding capacity, 829 as the actual capacity may be lower than anticipated. Conse- 830 quently, overscheduled flights must be rescheduled for a later 831 departure or arrival time. One advantage of the chance- 832 constrained model is that it helps to ensure that constraints 833 are not violated at a specified probability level. To evaluate 834

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Fig. 5 Number of slot displacements for arrival and departure flights in each scenario.

 the effectiveness of our approach, we use optimized flight schedule as input to the operational air traffic network. How- ever, it is difficult to accurately predict what the future state of airspace will be; therefore, a robust and stable flight schedule in actual operation is more desirable. The term ''robust" is commonly defined to characterize a software, a strategy, or an item that functions effectively and demonstrates minimal failures in various scenarios. In this research, we define the robustness of a flight schedule as the total amount of excess traffic scheduled for all sectors and airports. Here, we con- ducted a total of 20 experiments to compare the robustness of the optimal flight schedule under various schemes. Each experiment generated 50 sets of combinations of capacity based on the empirical distributions of the capacity of airports and sectors. We compare the amount of traffic with the capac- ity for each flight schedule, and calculate the total amount traf-851 fic that exceeds the capacity. Let R_q be the robustness of 852 optimization scheme q , then we have

$$
R_{q} = \frac{1}{N} \sum_{j=1}^{N} \sum_{t \in T'} \left[\sum_{a \in A^{\text{dep}} \cup A^{\text{arr}}} \max(0, (F_{j,a,t}^{q} - C_{j,a,t})) + \sum_{s \in S} \max(0, (F_{j,s,t}^{q} - C_{j,s,t})) \right]
$$
\n
$$
(32)
$$

856 where N represents the total number of simulated operation 857 scenarios, $F j, a, tq$ and $F j, s, tq$ denote 500 the number of

853

flights at airport a and sector s during time period t under opti-
858 mization scheme q, while $C_{j,a,t}$ and $C_{j,s,t}$ are the simulated 859 actual capacities at airport a and sector s during time period 860 t under optimization scheme q . 861

5.3.1. Robustness test results for base model 862

The base model corresponds to the scenario in the uncertainty 863 model where the violation probability is 0. Flight schedule data 864 obtained from its optimization is then compared with the 50 865 sets of capacity combinations generated in each experiment. 866 The robustness R_0 is then calculated and the statistical results 867 are shown in Fig. 8. It is evident that the robust model- 868 optimized flight schedule is more robust than the original flight 869 schedule, as its R is substantially lower. This further confirms 870 that flight schedule optimization is essential to make the air 871 traffic system more stable and improve its resilience to various 872 uncertainties. 873

5.3.2. Robustness test results for uncertainty model 874

The base model is too conservative. Airport and sector capac- 875 ity may be unused due to low scheduled traffic. The more 876 robust a flight schedule is, the higher the total cost. Based on 877 the robustness test, the optimal flight schedule robustness met- 878 ric for Schemes $1-10$ has been calculated. We compare the 879

Fig. 6 Percentage of flights with arrival and departure slot displacement in each scenario.

Fig. 7 Runtime of models under different setting.

 robustness of the uncertainty models with that of the base model based on the robustness metric. Additionally, we also compare the robustness between Method 1 and Method 2, as well as the robustness of the optimal flight schedule for each scheme within Method 1 and Method 2, to analyze the effect of node importance and violation probability on the robust-ness of the models.

887 We can see from Fig. 9 that the optimal flight schedule for all schemes of Method 1 is less robust than the base model. The capacity restriction becomes more stringent as the proba- bility of violation decreases, leading to a decrease in overca- pacity and a more robust flight schedule. The results of the robustness test for each scheme of Method 1 are in line with

the initial hypothesis. This implies that Method 1, which takes 893 into account capacity uncertainty, is less robust than the base 894 model. However, the base model sacrifices the total cost of the 895 flight schedule in order to achieve strong robustness. Fig. 10 896 shows that the total cost of the flight schedule for the robust 897 scheme is approximately 35. 4%, 15. 6%, 9. 49%, 5. 38%, 898 and 4.05% of the base model, respectively. This indicates that 899 the base model incurs a considerable cost in its pursuit of 900 robustness, which may not be desirable to stakeholders. In 901 comparison, Method 1 achieves a significant reduction in the 902 total cost of the flight schedule by sacrificing a bit of robust- 903 ness and appears to be more profitable. However, considering 904 that the optimization objective of the model in this paper is the 905

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Fig. 8 Comparison of robustness metric between original flight schedule and optimal flight schedule of deterministic model.

 flight schedule at the airport network level, it is possible to incorporate the structural characteristics of the network into Method 1. This has the potential to result in obtaining a robust flight schedule and reducing costs, thereby creating a model better suited for optimizing the flight schedule at the airport network level.

 In an airport network, if there is delay or congestion at an airport or sector with high average daily flow or closeness, it can have a ripple effect on other downstream airports and sec- tors. To minimize the likelihood of this occurrence, Method 2 considers the importance of both the airport and the sector nodes. This results in a smaller probability of violations for important airports and sectors, leading to a robust flight schedule with a low total cost sacrifice. The total cost of the optimal flight schedule for all the schemes of Method 2 is sig-

Fig. 9 Comparison of optimal flight schedule robustness metric by scheme.

Fig. 10 Comparison of total cost of optimal flight schedule by scheme.

nificantly lower than that of the robust model and Method 1, 921 as seen in Fig. 10. Additionally, the overcapacity of the opti- 922 mal flight schedule for almost schemes of Method 2 is higher 923 than that of Method 1, as seen in Fig. 9. Considering the 924 importance of the node in the model, incorporating it into 925 the optimization model can result in a flight schedule that 926 demonstrates strong resilience and minimizes overall cost. 927 This, in turn, improves the efficiency of optimizing the flight 928 schedule at the airport network level. 929

Further examination of Fig. 9 reveals two interesting find-
930 ings: (A) we observe that the optimal flight schedule of 931 Scheme 9 in Method 2 performs better in terms of robustness, 932 even though the total cost is lower than that of Scheme 4 and 5 933 of Method 1 by 30.7% and 7.8%, respectively. This clearly 934 shows the robustness and superiority of Method 2 compared 935

 to Method 1. Inclusion of the importance of the nodes in the model has advantages for the optimization performance of the model, making it more suitable for optimizing the flight schedule at the airport network level. The results of the robust- ness metric comparison for the above schemes are shown in Fig. 11. (B) The optimization performance of the model still has room to improve. Fig. 11 shows the robustness metric for each scheme of Method 2. Since Scheme 7 has lower viola- tion probabilities, the optimized schedule should be more robust. However, its robustness metric is not as good as those of Schemes 8 and 9. We hypothesize that this is due to the com- bination of the probability of violation and the structural char- acteristics of the airport network. The importance value cannot fully capture the importance of the sector or airport in the network. To further investigate this, we performed addi- tional experiments by adjusting the values of Eq. (27). The maximum violation probability in Method 2 is set to 0.2, the maximum violation probability ranged from 0.23 to 0.35 with a step change of 0.03. In total, five sets of optimization exper- iments similar to Method 2 were conducted, with the only dif-ference being the combination of violation probability.

 Table 8 presents the total cost and robustness of the flight schedule. The data in the tables show that as the probability of violation increases, the total cost of the optimal flight sched- ule from Scheme 6 to Scheme 10 decreases, but the robustness does not necessarily increase. The results for different values of a demonstrate that the robustness of schemes with a high prob- ability of violation can be lower than that of schemes with a low probability of violation. Method 2 is more suitable for flight schedule optimization at the airport network level than Method 1, however, it does not take into account all the spe- cial points of the airport network. The combination of viola- tion probability calculated by linear interpolation based on node importance is probably not the optimal combination for the corresponding schemes. This is evidenced by the lack of a clear trend in the average robustness in Table 8.

5.4. Comparison with other method of setting violation 972 probability 973

The importance of the sector node was determined using close-
974 ness, while the importance of the airport node was assessed 975 based on the volume of traffic. In this section, we compare 976 the optimal results with an alternative approach that relies 977 on a different network metric to assess the importance of 978 nodes. Specifically, we use the degree of the node as the mea- 979 sure of importance. The total cost and robustness of the results 980 under different optimization schemes are plotted in Fig. 12. 981 There is minimal variation in total cost resulting from two net- 982 work metrics, with only a slight distinction observed in the 983 schemes S_6 and S_7 . However, there are clear discrepancies in 984 the robustness of the optimized schedule when using the two 985 different methods to set the probability of violations. Using 986 traffic and closeness metrics to assess the importance of nodes 987 can lead to a more resilient flight schedule compared to relying 988 solely on the degree of the network. The excess capacity at 989 each airport and sector is determined by employing Eq. (32) 990 In Fig. $13(a)$ and (b), the average number of flights surpassing 991 the capacity of airports or sectors is illustrated for various 992 optimization approaches. Among the airports, only ZBAA, 993 ZGSZ, and ZUCK exhibit more than 3 flights exceeding 994 capacity, while the majority of airports and sectors experience 995 fewer than 2 flights exceeding capacity. Sectors ZHHHAR01 996 and ZBAAAR15 show more than two flights surpassing sector 997 capacity when applying violation probability settings based on 998 closeness. Overall, the optimized flight schedules demonstrate 999 resilience to operational uncertainties. 1000

5.5. Discussion 1001

We identified congested points in the air traffic network by 1002 using flight traffic data and capacity data. The level of conges- 1003 tion was measured with a number in the range of 0 to 1, with 1004

Fig. 11 Comparison of optimal flight schedule robustness metric.

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Fig. 12 Total cost and robustness of results under different optimization scheme.

 higher numerical values indicating more congestion. Similar to R_q , we define $R_{q,w,t}$ as value of the level of congestion for node 1007 w at 15-minutes slot t of optimization scheme $q.R_{q,w,t}$ can be calculated by Eq. (33). The results of Scheme 10 are shown in Fig. 14. We see the optimized flight schedule of Scheme 10 still has some congested airports and sectors. To achieve a flight schedule with fewer congested airports and airspace, increased robustness, and lower total cost, we can modify the probability of a violation of restrictions in airports and sec- tors. However, depending solely on static data such as node importance to set the probability of violation of airports and sectors may not be an optimal strategy. It is challenging to decide on the optimal combination of probability of violation, and congested nodes in the air traffic network should be taken into consideration to dynamically adjust the probability of vio- lation of each chance constraint. To improve the probability of violation and the quality of the solution, it is possible to reduce the probability of violation at congested points and increase the probability of violation at points with a sufficient capacity margin. This can be done by ''cutting the peak and filling the valley'', which can be further studied by monitoring the changes in the probability of the chance of violation of the constraints of each node, thereby exploring the trigger condi- tions and intrinsic mechanisms of the optimization dynamic of the airport network. ¹⁰³⁰

$$
R_{q,w,t} = \frac{1}{N} \sum_{j=1}^{N} \max(0, (F_{j,w,t}^q - C_{j,w,t})), \quad \forall w \in A^{\text{dep}} \cup A^{\text{arr}} \cup S, t \in T'
$$
\n(33)

Our research has practical implications in real-world sce- 1033 narios. Critical sectors and airports can be identified using 1034 existing and predicted air traffic conditions, along with meteo- 1035 rological data. Supported by air traffic flow management sys- 1036 tems, the personnel involved in managing air traffic flow 1037 determines the permissible risk levels for key sectors and air- 1038 ports. Subsequently, our model is capable of assigning the best 1039 departure times for each flight. In the future, the efficacy of the 1040 model could be improved through the application of machine 1041 learning and artificial intelligence technologies. 1042

6. Conclusions 1043

The demand for air transport and the complexity of the air 1044 traffic system have both grown, leading to a number of uncer- 1045 tainties in the implementation of flight schedules. This paper 1046 presents a new capacity uncertainty chance constraint model 1047 to address the flight schedule optimization problem at the air- 1048 port network level. This model takes into account the capacity 1049 uncertainty of airports and sectors in the air traffic system and 1050 also innovatively incorporates the importance of network 1051 nodes into the model. The experimental data show that the tra- 1052

Fig. 13 Robustness of airports and sectors.

Fig. 14 Heatmap of congestion at airports and sectors in Scheme 10. (a) The congestion level of departure airports; (b) The congestion level of arrival airports; (c) The congestion level of sectors.

 ditional capacity uncertainty model is not sufficient to handle the uncertainty problem. The cost of having a reliable flight schedule is high. To address this issue and create a model with better optimization results, this paper takes into account the importance of the nodes in the airport network in the model. Compared to the deterministic model and the traditional capacity uncertainty model, the results show that our model can produce a more robust and lower total cost flight schedule through the appropriate setting of the chance constraint viola-tion probability.

 This study has the following limitations. First, due to the limitations of the current dataset, it is difficult to find the opti- mal combination of probability of violation. This, in turn, reduces the efficiency of the model. To improve the optimiza- tion performance, the dynamic data of the congested points in the airport network should be taken into account when adjust- ing the probability of violation. Second, the length of the slot discussed in this paper is 5 min. Reducing the slot to 1 min could provide more accurate results. However, this would also 1071 significantly increase the computational complexity of the 1072 model. Third, the sector minimum flight time for each flight 1073 should be varied, as this would make the flight schedule more 1074 practical. This is because the performance of the aircraft can 1075 vary greatly depending on the model of the plane being used. 1076 Therefore, the sector minimum flight time should be adjusted 1077 accordingly for each flight. Future research efforts should be 1078 made in two areas: (A) to develop algorithms based on artifi- 1079 cial intelligence to generate representative airspace operation 1080 scenarios; and (B) investigating the unique optimization pro- 1081 cess of the airport network. 1082

CRediT authorship contribution statement 1083

Jianzhong YAN: Writing – original draft, Validation, Investi-
1084 gation, Formal analysis, Conceptualization. Haoran HU: 1085 Writing – original draft, Software, Methodology, Investiga- 1086 Robust pre-departure scheduling for a nation-wide air traffic flow management 17

1087 tion, Formal analysis. Yaniun WANG: Writing – review $\&$ editing, Writing – original draft, Supervision, Project adminis- tration, Methodology, Investigation, Funding acquisition, Formal analysis, Data curation, Conceptualization. Xiaozhen MA: Methodology, Investigation, Formal analysis. Minghua HU: Investigation, Formal analysis. Daniel DELAHAYE: Writing – review & editing, Writing – original draft, Method- ology, Formal analysis. Sameer ALAM: Writing – review & editing, Writing – original draft, Investigation, Formal analysis.

1097 Declaration of competing interest

1098 The authors declare that they have no known competing 1099 financial interests or personal relationships that could have 1100 appeared to influence the work reported in this paper.

1101 Acknowledgements

 This research was supported by the National Natural Science Foundation of China (Grant Nos. U2033203, U1833126, 61773203, 61304190). We thank the anonymous referees and the editors for their constructive comments and suggestions, which have significantly improved this work. Ling., Wi[t](https://www.icao.int/Newsroom/Pages/Solid-passenger-traffic-growth-and-moderate-air-cargo-demand-in-2018.aspx)ting - original draft, Investigation, Formal 2008 manufacture. There are not a few of a manufacture of equal draft interaction of equal draft interaction of equal draft interaction of equal draft interaction of

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Please cite this article in press as: YAN J et al. Robust pre-departure scheduling for a nation-wide air traffic flow management, Chin J Aeronaut (2024), [https://doi.org/](https://doi.org/10.1016/j.cja.2024.08.054) [10.1016/j.cja.2024.08.054](https://doi.org/10.1016/j.cja.2024.08.054)