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## Piecewise Polynomial Model of the Aerodynamic Coefficients of the *Cumulus One* Unmanned Aircraft

Torbjørn Cunis<sup>1</sup> and Anders La Cour-Harbo<sup>2</sup>

#### Abstract

This document illustrates a piecewise polynomial model for Cumulus One, based on continuous fluid dynamics simulation, derived using the pwpfit toolbox. The model has been developed in a joint project of Sky-Watch and the University of Aalborg.

#### Preliminaries

If not stated otherwise, all variables are in SI units. We will refer to the following axis systems of ISO 1151-1: the *body axis system*  $(x_f, y_f, z_f)$  aligned with the aircraft's fuselage; the *air-path axis system*  $(x_a, y_a, z_a)$  defined by the velocity vector  $\mathbf{V}_A$ ; and the *normal earth-fixed axis system*  $(x_g, y_g, z_g)$ . The orientation of the body axes with respect to the normal earth-fixed system is given by the attitude angles  $\Phi, \Theta, \Psi$  and to the air-path system by angle of attack  $\alpha$  and side-slip  $\beta$ ; the orientation of the air-path axes to the normal earth-fixed system is given by azimuth  $\chi_A$ , inclination  $\gamma_A$ , and bank-angle  $\mu_A$ . (Fig. ??.)



(a) Longitudinal axes ( $\beta = \mu_A = 0$ ).

(b) Horizontal axes ( $\gamma_{\rm A} = 0$ ).

Fig. 1: Axis systems with angles and vectors. Projections into the plane are marked by '.

#### I. Aerodynamic Coefficients

The piece-wise polynomial models of the aerodynamic coefficients are given

$$C_{\odot}(\alpha,\beta,\xi,\eta,\zeta) = \begin{cases} C_{\odot}^{pre}(\alpha,\beta,\dots) & \text{if } \alpha \le \alpha_0, \\ C_{\odot}^{post}(\alpha,\beta,\dots) & \text{else,} \end{cases}$$
(1)

where  $C_{\odot} \in \{C_X, C_Y, C_Z, C_l, C_m, C_n\}$  are polynomials in angle of attack, side-slip, and surface deflections; and the boundary is found at

$$\alpha_0 = 17.949^{\circ}.$$
 (2)

The polynomials in low and high angle of attack,  $C_{\odot}^{pre}$ ,  $C_{\odot}^{post}$ , are sums

$$C_{\odot}^{pre} = C_{\odot\alpha}^{pre}(\alpha) + C_{\odot\xi}(\beta,\xi) + C_{\odot\eta}^{pre}(\alpha,\eta) + C_{\odot\zeta}(\beta,\zeta);$$
(3)

$$C_{\odot}^{post} = C_{\odot\alpha}^{post}(\alpha) + C_{\odot\xi}(\beta,\xi) + C_{\odot\eta}^{post}(\alpha,\eta) + C_{\odot\zeta}(\beta,\zeta).$$

$$\tag{4}$$

In the following subsections, we present the polynomial terms obtained using the pwpfit toolbox. Coefficients of absolute value lower than  $10^{-2}$  have been omitted for readability.

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## A. Domain of low angle of attack

Polynomials in angle of attack:

$$C_{X\alpha}^{pre} = -2.566 \times 10^{-2} + 5.722 \times 10^{-1} \alpha + 1.496 \alpha^2 - 1.148 \times 10^1 \alpha^3;$$
(5)

$$C_{Y\alpha}^{pre} = 5.402 \times 10^{-2} - 2.345 \times 10^{-1} \alpha - 2.001 \alpha^2 + 7.054 \alpha^3;$$
(6)

$$C_{Z\alpha}^{pre} = -3.475 \times 10^{-1} - 5.467\alpha + 1.853\alpha^2 + 2.663 \times 10^1 \alpha^3;$$
<sup>(7)</sup>

$$C_{1\alpha}^{pre} = 4.875 \times 10^{-2} - 2.190 \times 10^{-1} \alpha - 2.004 \alpha^2 + 7.146 \alpha^3;$$
(8)

(9)

$$C_{\rm m\alpha}^{pre} = 6.214 \times 10^{-2} - 1.755\alpha - 3.427\alpha^2 + 1.256 \times 10^1\alpha^3;$$

$$C_{n\alpha}^{pre} = 4.748 \times 10^{-2} - 2.097 \times 10^{-1} \alpha - 2.016 \alpha^2 + 7.171 \alpha^3;$$
<sup>(10)</sup>

Polynomials in angle of attack and elevator deflections:

$$C_{X\eta}^{pre} = 4.327 \times 10^{-2} \eta - 4.458 \times 10^{-1} \alpha \eta + 3.370 \times 10^{-1} \alpha^2 \eta - 4.567 \times 10^{-1} \alpha \eta^2 + 7.331 \times 10^{-2} \eta^3;$$
(11)  
$$C_{X\eta}^{pre} = 1.822 \times 10^{-2} \pi + 7.484 \times 10^{-2} \alpha \pi - 4.284 \times 10^{-1} \alpha^2 \pi - 4.567 \times 10^{-1} \alpha \eta^2 + 7.331 \times 10^{-2} \eta^3;$$
(11)

$$C_{Y\eta}^{pre} = 1.832 \times 10^{-2} \eta + 7.484 \times 10^{-2} \alpha \eta - 4.384 \times 10^{-1} \alpha^2 \eta;$$

$$C_{Z\pi}^{pre} =$$
(12)

$$C_{Z\eta}^{pre} =$$

$$-2.567 \times 10^{-1} \eta + 3.085 \times 10^{-1} \alpha \eta - 5.105 \times 10^{-2} \eta^2 - 7.394 \times 10^{-1} \alpha^2 \eta + 6.936 \times 10^{-1} \alpha \eta^2 + 1.337 \times 10^{-1} \eta^3;$$
(13)  
$$C_{l\eta}^{pre} = 1.699 \times 10^{-2} \eta + 8.936 \times 10^{-2} \alpha \eta - 4.564 \times 10^{-1} \alpha^2 \eta + 1.571 \times 10^{-2} \alpha \eta^2;$$
(14)

$$C_{m\eta}^{pre} = -9.028 \times 10^{-1} \eta + 7.437 \times 10^{-1} \alpha \eta - 4.924 \times 10^{-2} \eta^2 - 8.415 \times 10^{-1} \alpha^2 \eta + 2.210 \alpha \eta^2 + 5.251 \times 10^{-1} \eta^3;$$
(15)

$$C_{n\eta}^{pre} = 1.532 \times 10^{-2} \eta + 8.758 \times 10^{-2} \alpha \eta - 4.513 \times 10^{-1} \alpha^2 \eta + 1.487 \times 10^{-2} \alpha \eta^2.$$
<sup>(16)</sup>

## B. Domain of high angle of attack

Polynomials in angle of attack:

$$C_{X\alpha}^{post} = 1.266 \times 10^{-2} - 3.159 \times 10^{-1} \alpha + 3.832 \times 10^{-1} \alpha^2 - 1.226 \times 10^{-1} \alpha^3;$$
(17)

$$C_{Y\alpha}^{post} = -2.297 \times 10^{-2} \alpha^2 + 1.337 \times 10^{-2} \alpha^3; \tag{18}$$

$$C_{Z\alpha}^{post} = -4.179 \times 10^{-1} - 2.345\alpha + 9.586 \times 10^{-1}\alpha^2 - 3.665 \times 10^{-2}\alpha^3;$$
<sup>(19)</sup>

$$C_{l\alpha}^{post} = 2.006 \times 10^{-2} - 8.200 \times 10^{-2} \alpha + 1.012 \times 10^{-1} \alpha^2 - 3.515 \times 10^{-2} \alpha^3;$$
<sup>(20)</sup>

$$C_{m\alpha}^{post} = -2.552 \times 10^{-1} - 5.131 \times 10^{-1} \alpha - 2.677 \times 10^{-1} \alpha^2 + 1.332 \times 10^{-1} \alpha^3;$$
<sup>(21)</sup>

$$C_{n\alpha}^{post} = 1.159 \times 10^{-2} - 3.062 \times 10^{-2} \alpha + 2.727 \times 10^{-2} \alpha^2;$$
(22)

Polynomials in angle of attack and elevator deflections:

$$C_{X\eta}^{post} = -1.342 \times 10^{-2} \eta - 1.663 \times 10^{-1} \alpha \eta - 1.796 \times 10^{-1} \eta^2 + 2.254 \times 10^{-2} \alpha^2 \eta + 9.274 \times 10^{-2} \alpha \eta^2 + 7.331 \times 10^{-2} \eta^3;$$
(23)

$$C_{Z\eta}^{post} = -2.922 \times 10^{-1} \eta + 1.829 \times 10^{-1} \alpha \eta + 1.277 \times 10^{-1} \eta^2 + 2.284 \times 10^{-2} \alpha^2 \eta + 1.229 \times 10^{-1} \alpha \eta^2 + 1.337 \times 10^{-1} \eta^3;$$
(24)

$$C_{m\eta}^{post} = -9.498 \times 10^{-1} \eta + 6.099 \times 10^{-1} \alpha \eta + 5.093 \times 10^{-1} \eta^2 + 6.456 \times 10^{-2} \alpha^2 \eta + 4.264 \times 10^{-1} \alpha \eta^2 + 5.251 \times 10^{-1} \eta^3;$$
(25)  

$$C_{Y\eta}^{post}, C_{l\eta}^{post}, C_{n\eta}^{post} \text{ are approximately zero.}$$
(26)

### C. Full-envelope polynomials

Polynomials in side-slip and aileron deflections:

$$\begin{split} C_{X\xi} &= \\ 6.557 \times 10^{-2}\beta^{2} + 4.214 \times 10^{-2}\beta\xi - 1.493\xi^{2} + 4.264 \times 10^{-2}\xi^{3} - 1.647 \times 10^{-2}\beta^{4} - 2.321 \times 10^{-2}\beta^{3}\xi + 9.649 \times 10^{-2}\beta^{2}\xi^{2} + 2.859 \times 10^{-2}\beta\xi^{3} + 3.084 \times 10^{1}\xi^{4}, \\ (27) \\ C_{Y\xi} &= \\ -3.697 \times 10^{-1}\beta - 1.570 \times 10^{-1}\xi - 3.231 \times 10^{-2}\beta^{2} - 6.137\xi^{2} + 7.416 \times 10^{-2}\beta^{3} + 1.611 \times 10^{-2}\beta\xi^{2} + 2.214\xi^{3} + 6.487 \times 10^{-1}\beta^{2}\xi^{2} + 5.323 \times 10^{-2}\beta\xi^{3} + 1.456 \times 10^{2}\xi^{4}, \\ (28) \\ C_{Z\xi} &= \\ 3.411 \times 10^{-1}\beta^{2} + 4.141 \times 10^{-1}\beta\xi - 3.717\xi^{2} + 4.234 \times 10^{-2}\xi^{3} - 9.915 \times 10^{-2}\beta^{4} - 1.922 \times 10^{-1}\beta^{3}\xi + 1.945 \times 10^{-1}\beta^{2}\xi^{2} + 9.909 \times 10^{-1}\beta\xi^{3} + 9.856 \times 10^{1}\xi^{4}, \\ (29) \\ C_{I\xi} &= \\ -5.798 \times 10^{-2}\beta - 3.929 \times 10^{-1}\xi - 2.906 \times 10^{-2}\beta^{2} - 5.551\xi^{2} + 1.763 \times 10^{-2}\beta^{3} + 1.722 \times 10^{-1}\beta^{2}\xi + 4.557 \times 10^{-1}\xi^{3} + 5.835 \times 10^{-1}\beta^{2}\xi^{2} + 5.332 \times 10^{-2}\beta\xi^{3} + 1.319 \times 10^{2}\xi^{4}, \\ (30) \\ C_{m\xi} &= \\ -3.978 \times 10^{-2}\beta^{2} + 5.554 \times 10^{-1}\beta\xi - 4.689\xi^{2} + 4.229 \times 10^{-2}\xi^{3} + 2.585 \times 10^{-2}\beta^{4} - 2.309 \times 10^{-1}\beta^{3}\xi + 4.077 \times 10^{-1}\beta^{2}\xi^{2} - 5.068 \times 10^{-1}\beta\xi^{3} + 1.160 \times 10^{2}\xi^{4}, \\ (31) \\ C_{n\xi} &= \\ \end{array}$$

$$3.686 \times 10^{-2}\beta + 1.392 \times 10^{-2}\xi - 2.828 \times 10^{-2}\beta^2 - 5.410\xi^2 - 1.160 \times 10^{-1}\xi^3 + 5.678 \times 10^{-1}\beta^2\xi^2 + 5.334 \times 10^{-2}\beta\xi^3 + 1.286 \times 10^{2}\xi^4.$$
(32)

Polynomials in side-slip and rudder deflections:

$$C_{X\zeta} = -1.031 \times 10^{-2} \beta \zeta - 7.986 \times 10^{-2} \zeta^2 + 1.086 \times 10^{-2} \beta \zeta^3 + 9.739 \times 10^{-2} \zeta^4;$$

$$C_{Y\zeta} =$$
(33)

 $-8.526 \times 10^{-2} \zeta - 2.128 \times 10^{-2} \beta^2 - 3.569 \times 10^{-1} \zeta^2 + 1.049 \times 10^{-2} \beta^2 \zeta + 1.924 \times 10^{-2} \beta \zeta^2 + 7.679 \times 10^{-2} \zeta^3 + 5.663 \times 10^{-2} \beta^2 \zeta^2 + 5.247 \times 10^{-1} \zeta^4;$ (34)

$$C_{Z\zeta} = -2.036 \times 10^{-2} \beta^2 - 1.332 \times 10^{-2} \beta \zeta - 1.743 \times 10^{-1} \zeta^2 + 1.834 \times 10^{-2} \beta^2 \zeta^2 + 3.683 \times 10^{-2} \beta \zeta^3 + 2.631 \times 10^{-1} \zeta^4;$$
(35)

$$C_{l\zeta} = -1.930 \times 10^{-2} \beta^2 - 3.221 \times 10^{-1} \zeta^2 + 5.111 \times 10^{-2} \beta^2 \zeta^2 + 4.735 \times 10^{-1} \zeta^4;$$

$$C_{m\zeta} =$$
(36)

$$-3.231 \times 10^{-2}\beta^{2} - 1.436 \times 10^{-2}\beta\zeta - 2.672 \times 10^{-1}\zeta^{2} + 1.241 \times 10^{-2}\beta^{3}\zeta + 1.472 \times 10^{-2}\beta^{2}\zeta^{2} + 1.051 \times 10^{-2}\beta\zeta^{3} + 4.193 \times 10^{-1}\zeta^{4};$$
(37)
$$C_{n\zeta} = 2.158 \times 10^{-2}\zeta - 1.882 \times 10^{-2}\beta^{2} - 3.137 \times 10^{-1}\zeta^{2} - 1.338 \times 10^{-2}\zeta^{3} + 4.978 \times 10^{-2}\beta^{2}\zeta^{2} + 4.611 \times 10^{-1}\zeta^{4}.$$
(38)

## II. Equations of Motion

We have the aerodynamic forces and moments in body axis system

$$\begin{bmatrix} X^{A} \\ Y^{A} \\ Z^{A} \end{bmatrix}_{f} = \frac{1}{2} \rho S V^{2}_{A} \begin{bmatrix} C_{X} \\ C_{Y} \\ C_{Z} \end{bmatrix}; \qquad \begin{bmatrix} L^{A} \\ M^{A} \\ N^{A} \end{bmatrix}_{f} = \frac{1}{2} \rho S V^{2}_{A} \begin{bmatrix} b C_{1} \\ c_{A} C_{m} \\ b C_{n} \end{bmatrix} + \begin{bmatrix} X^{A} \\ Y^{A} \\ Z^{A} \end{bmatrix}_{f} \times \left( \mathbf{x}_{cg} - \mathbf{x}_{cg}^{ref} \right); \qquad (39)$$

and the weight force by rotation into the body axis system

$$X_{\rm g}^{\rm G} = -g\sin\Theta; \tag{40}$$

$$Y_{\rm g}^{\rm G} = -g\sin\Phi\cos\Theta; \tag{41}$$

$$Z_{\rm g}^{\rm G} = -g\cos\Phi\cos\Theta; \tag{42}$$

The resulting forces lead to changes in the velocity vector, in body axis system, by

$$\dot{\mathbf{V}}_{\mathrm{Af}} = \frac{1}{m} \begin{bmatrix} X^{\mathrm{A}} + X^{\mathrm{G}} + X^{\mathrm{F}} \\ Y^{\mathrm{A}} + Y^{\mathrm{G}} \\ Z^{\mathrm{A}} + Z^{\mathrm{G}} \end{bmatrix}_{\mathrm{f}} + \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times \mathbf{V}_{\mathrm{Af}}.$$
(43)

with the thrust  $X_{\rm f}^{\rm F} = F$  (engines aligned with the  $x_{\rm f}$ -axis). For a symmetric plane  $(I_{xy} = I_{yz} = 0)$ , the resulting moments in body axis are given as

$$L_{\rm f} = L_{\rm f}^{\rm A} - q \, r \, (I_z - I_y) + p \, q \, I_{zx}; \tag{44}$$

$$M_{\rm f} = M_{\rm f}^{\rm A} - p \, r \left( I_x - I_z \right) - \left( p^2 - r^2 \right) I_{zx}; \tag{45}$$

$$N_{\rm f} = N_{\rm f}^{\rm A} - p \, q \, (I_y - I_x) - q \, r \, I_{zx}; \tag{46}$$

with the inertias  $I_x, I_y, I_z, I_{zx}$ . The changes of angular body rates are then given as

$$\dot{p} = \frac{1}{I_x I_z - I_{zx}^2} \left( I_z L_f + I_{zx} N_f \right); \tag{47}$$

$$\dot{q} = \frac{1}{I_y} M_{\rm f};\tag{48}$$

$$\dot{r} = \frac{1}{I_x I_z - I_{zx}^2} \left( I_{zx} L_{\rm f} + I_x N_{\rm f} \right). \tag{49}$$

Here, the normalized body rates have been used with

$$\begin{bmatrix} \hat{p} \\ \hat{q} \\ \hat{r} \end{bmatrix} = \frac{1}{2V_{\mathrm{A}}} \begin{bmatrix} b \ p \\ c_{\mathrm{A}} \ q \\ b \ r \end{bmatrix} \Longleftrightarrow \begin{bmatrix} p \\ q \\ r \end{bmatrix} = 2V_{\mathrm{A}} \begin{bmatrix} b^{-1} \ \hat{p} \\ c_{\mathrm{A}}^{-1} \ \hat{q} \\ b^{-1} \ \hat{r} \end{bmatrix}$$
(50)

and

$$\begin{bmatrix} \dot{\hat{p}} \\ \dot{\hat{q}} \\ \dot{\hat{r}} \end{bmatrix} = \frac{1}{V_{\rm A}} \left( \frac{1}{2} \begin{bmatrix} b \, \dot{p} \\ c_{\rm A} \, \dot{q} \\ b \, \dot{r} \end{bmatrix} - \dot{V}_{\rm A} \begin{bmatrix} \hat{p} \\ \hat{q} \\ \hat{r} \end{bmatrix} \right). \tag{51}$$

The change of attitude is finally obtained by rotation into normal earth-fixed axis system:

$$\Phi = p + q \sin \Phi \tan \Theta + r \cos \Phi \tan \Theta; \tag{52}$$

$$\dot{\Theta} = q\cos\Phi - r\sin\Phi; \tag{53}$$

$$\dot{\Psi} = q\sin\Phi\cos^{-1}\Theta + r\cos\Phi\cos^{-1}\Theta.$$
(54)

#### III. LONGITUDINAL MODEL

The longitudinal model is restricted to the  $x_{\rm a}$ - $z_{\rm a}$ -plane, assuming  $\beta = \mu_{\rm A} = \chi_{\rm A} = 0$ .

#### A. Aerodynamic Coefficients

The longitudinal aerodynamic coefficients,  $C_{\rm L}, C_{\rm D}, C_{\rm m}$ , are obtained as

$$\begin{bmatrix} C_{\rm L} \\ C_{\rm D} \end{bmatrix} = \begin{bmatrix} +\sin\alpha & -\cos\alpha \\ -\cos\alpha & -\sin\alpha \end{bmatrix} \begin{bmatrix} C_{\rm X} \\ C_{\rm Z} \end{bmatrix}.$$
(55)

#### B. Equations of motion

The longitudinal equations of motion are given as

$$\dot{V}_{\rm A} = \frac{1}{m} \left( T \cos \alpha - \frac{1}{2} \rho S V_{\rm A}^2 C_{\rm D}(\alpha, \eta, q) - mg \sin \gamma_{\rm A} \right), \tag{56}$$

$$\dot{\gamma}_{\rm A} = \frac{1}{mV_{\rm A}} \left( T \sin \alpha + \frac{1}{2} \rho S V_{\rm A}^2 C_{\rm L}(\alpha, \eta, q) - mg \cos \gamma_{\rm A} \right),\tag{57}$$

$$\dot{q} = \frac{1}{I_y} \frac{1}{2} \rho S c_{\rm A} V_{\rm A}^2 C_{\rm m}(\alpha, \eta, q); \qquad (58)$$

$$\dot{\Theta} = q; \tag{59}$$

with

$$\Theta = \alpha + \gamma. \tag{60}$$

Nomenclature

α	=	Angle of attack (rad);
$\alpha_0$	=	Low-angle of attack boundary (°);
β	=	Side-slip angle (rad);
$\gamma_{ m A}$	=	Flight-path angle relative to air (rad);
ζ	=	Rudder deflection (rad), negative if leading to positive yaw moment;
$\eta$	=	Elevator deflection (rad), negative if leading to positive pitch moment;
Θ	=	Pitch angle (rad);
$\mu_{\rm A}$	=	Air-path bank angle (rad);
ξ	=	Aileron deflection (rad), negative if leading to positive roll moment;
Q	=	Air density $(\rho = 1.200 \text{ kg m}^{-3});$
$\chi_{ m A}$	=	Air-path azimuth angle (rad);
$\Phi$	=	Bank angle (rad);
$\Psi$	=	Azimuth angle (rad);
$C_1$	=	Aerodynamic coefficient moment body $x_f$ -axis (·);
$C_{\mathrm{m}}$	=	Aerodynamic coefficient moment body $y_f$ -axis (·);
$C_{\rm n}$	=	Aerodynamic coefficient moment body $z_f$ -axis (·);
$C_{\mathrm{D}}$	=	Aerodynamic drag coefficient (·), positive along negative air-path $x_a$ -axis;
$C_{\rm L}$	=	Aerodynamic lift coefficient (·), positive along negative air-path $z_a$ -axis;
$C_{\rm X}$	=	Aerodynamic coefficient force body $x_f$ -axis (·);
$C_{\rm Y}$	=	Aerodynamic coefficient force body $y_f$ -axis (·);
$C_{\rm Z}$	=	Aerodynamic coefficient force body $z_f$ -axis (·);
D	=	Drag force (N), positive along negative air-path $x_a$ -axis;
F	=	Thrust force (N), positive along body $x_f$ -axis;
L	=	Lift force (N), positive along negative air-path $z_a$ -axis;
q	=	Pitch rate $(rad s^{-1})$ ;
b	=	Reference aerodynamic span $(b = 2.088 \text{ m});$
$c_{\mathrm{A}}$	=	Aerodynamic mean chord ( $c_{\rm A} = 2.800 \times 10^{-1} \mathrm{m}$ );
g	=	Standard gravitational acceleration $(g \approx 9.810 \mathrm{m  s^{-2}});$
m	=	Aircraft mass $(m = 2.619 \times 10^1 \text{ kg});$
p	=	Roll rate $(rad s^{-1});$
r	=	Yaw rate $(rad s^{-1});$
$L_{\rm f}$	=	Roll moment (N m), mathematically positive around $x_{\rm f}$ -axis;
$M_{\rm f}$	=	Pitch moment (N m), mathematically positive around $y_{\rm f}$ -axis;
$N_{\mathrm{f}}$	=	Yaw moment (N m), mathematically positive around $z_{\rm f}$ -axis;
S	=	Wing area $(S = 5.500 \times 10^{-1} \mathrm{m}^2);$
$V_{\rm A}, {f V}_{\rm A}$	=	Aircraft speed and velocity relative to air $(V_{\rm A} = \ \mathbf{V}_{\rm A}\ _2, \mathrm{ms^{-1}});$
$X_{\mathrm{f}}^{\mathrm{A}}$	=	Aerodynamic force along body $x_{\rm f}$ -axis (N);
$X_{\rm f}^{\rm F}$	=	Thrust force along body $x_{\rm f}$ -axis (N);
$Y_{\rm f}^{\rm A}$	=	Aerodynamic force along body $y_{f}$ -axis (N);
$Z_{\rm f}^{\rm A}$	=	Aerodynamic force along body $z_{\rm f}$ -axis (N);
$(\cdot)^{post}$	=	Domain of high angle of attack;
$(\cdot)^{pre}$	=	Domain of low angle of attack;
$x_a, y_a, z_a$	=	Air-path axis system;
$x_f, y_f, z_f$	=	Body axis system;
$x_g, y_g, z_g$	=	Normal earth-fixed axis system;