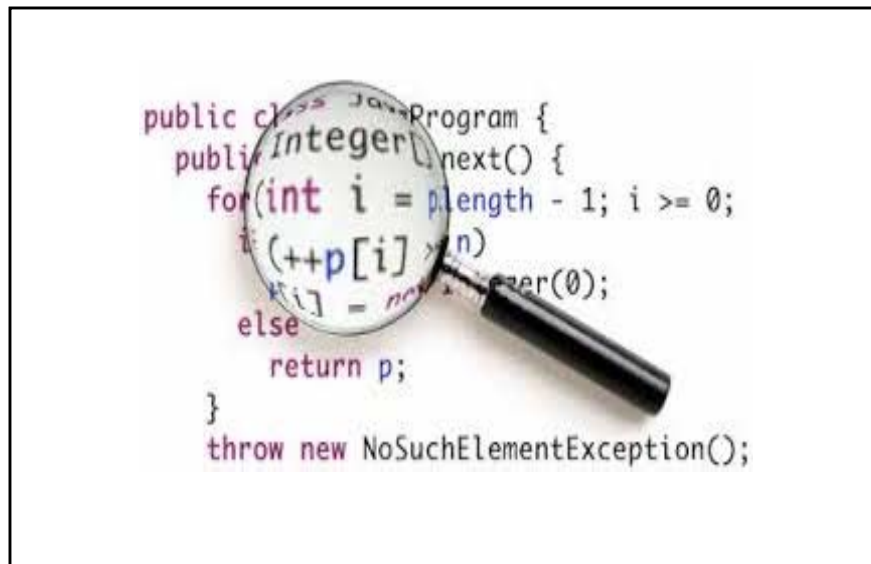


# Software and GNSS Fault-Monitoring for Automated Aircraft



J.H. Rife, H. Huang, S.Z. Guyer  
*Tufts University*

*ION GNSS+ 2018*

November 16, 2018

**Tufts**  
UNIVERSITY

# Key Concepts

- Propose an online **bug-monitoring** approach
  - Use analogy to GNSS augmentation system
- Discuss potential impact for pre-service verification

# Aviation Software at a Crossroads

Augustine's Law: Complexity of flight software grows an order of magnitude/decade

*Will traditional verification approaches (e.g. RTCA DO-178) scale?*

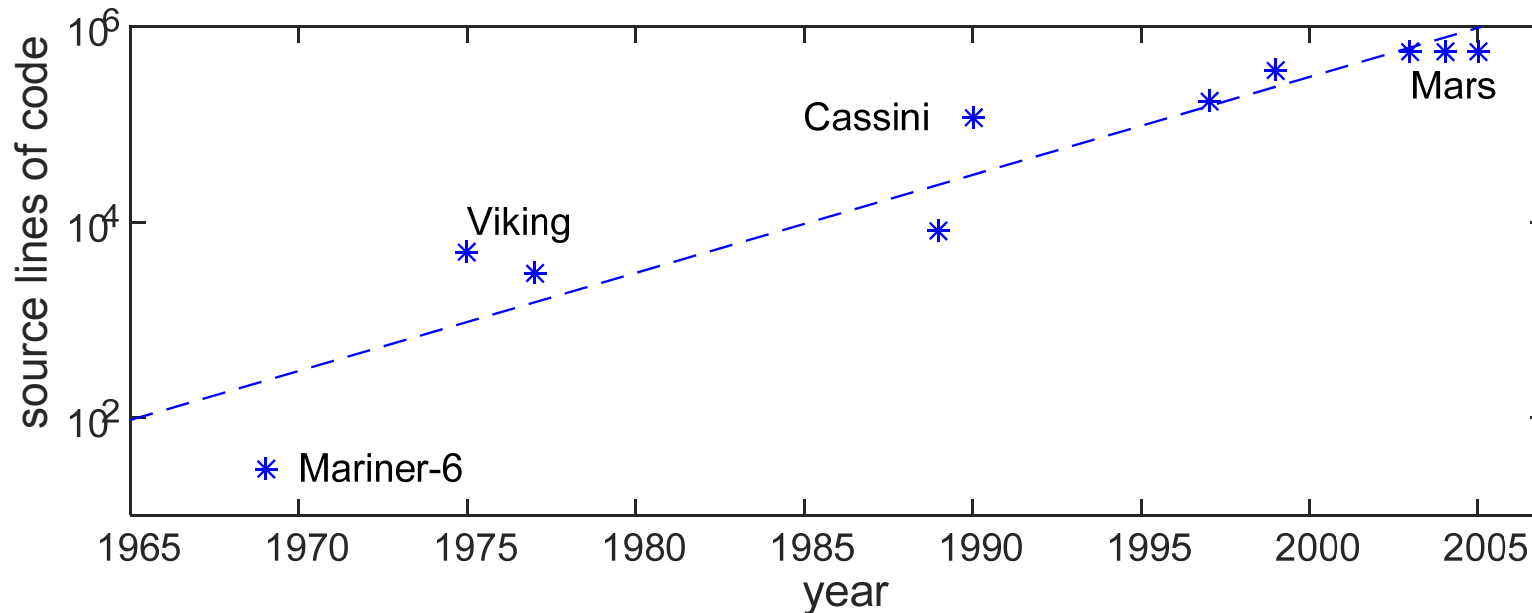


Figure adapted from Dvorak *et al.*,  
NASA study on flight software complexity, 2009

# Aerospace, Meet Internet



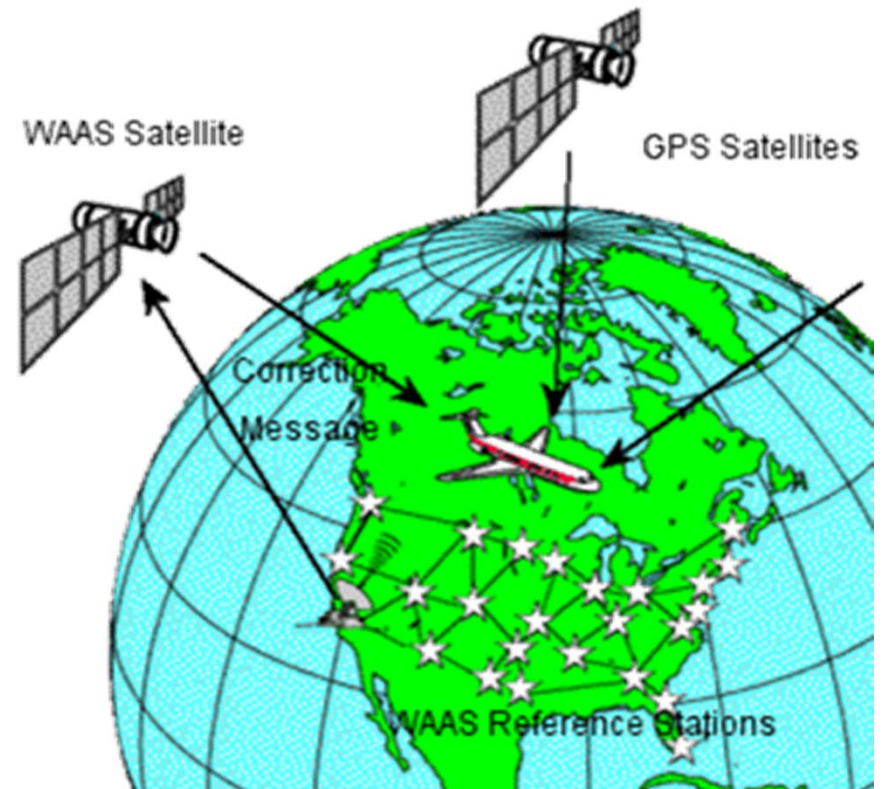
# Continual Validation of Complex Systems

*Inspection,  
Nondestructive Evaluation*



[https://commons.wikimedia.org/wiki/File:Visual\\_inspection\\_of\\_compressor\\_blades-090108-F-9919G-746.jpg](https://commons.wikimedia.org/wiki/File:Visual_inspection_of_compressor_blades-090108-F-9919G-746.jpg)

*Monitoring of Navigation Signals  
(e.g. SBAS)*



<https://commons.wikimedia.org/wiki/File:Waas.png>

# Augmenting the Design Toolbox

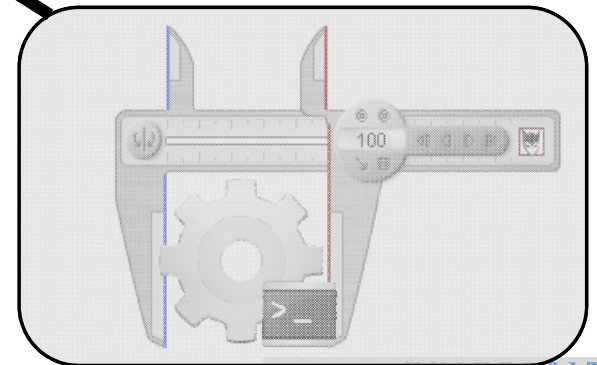


***Language***

```
public class JavaProgram {  
    public Integer next() {  
        for (int i = p.length - 1; i >= 0; i--)  
            if (p[i] > n)  
                return new Integer(0);  
        else  
            return p;  
    }  
    throw new NoSuchElementException();  
}
```

***Compile Time***

***Run-Time***



# An Opportunity Exists

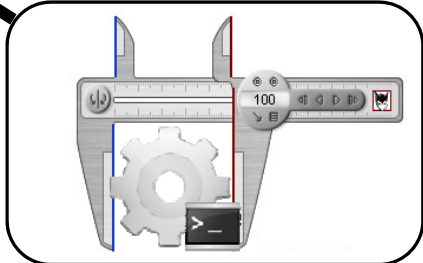


**Language**

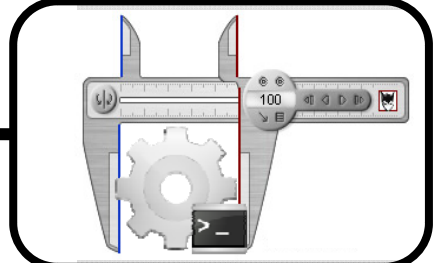
```
public class JavaProgram {  
    public Integer next() {  
        for(int i = length - 1; i >= 0; i--){  
            ++p[i];  
            return p[i];  
        }  
        return p;  
    }  
    throw new NoSuchElementException();  
}
```

**Compile Time**

**Run-Time**



**Pre-operational Testing**



**Operational Testing**



# Open Questions

- How can we *design a bug monitor* analogous to monitors used for mechanical and electrical systems?
- How do we *train a monitor* to recognize what is normal behavior given that our software contains unknown bugs?
- How much can bug monitoring *reduce the burden* of pre-service verification?



Anonymous: <https://pxhere.com/photo/689545>



# Open Questions

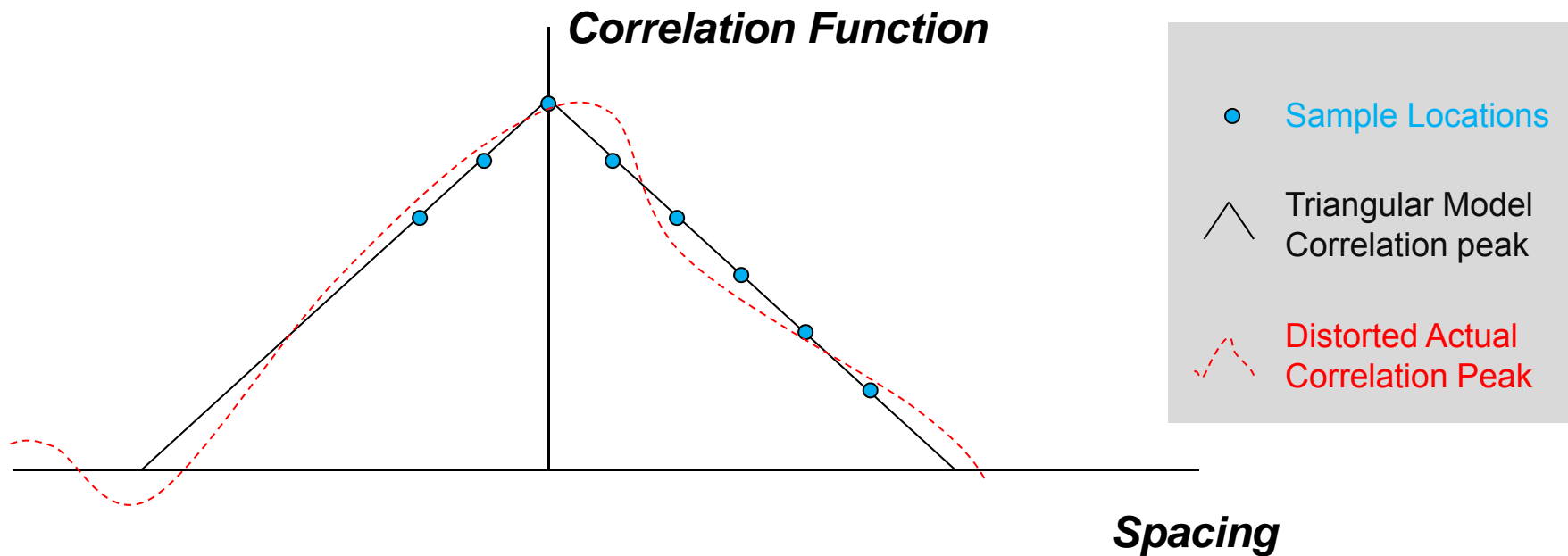
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# Monitor Design



# Signal Deformation Monitoring (SDM)



Sample correlation peak at 8 locations,  
Difference 7 neighboring pairs, and  
Compare to nominal values

## SDM in GBAS

The 7 errors (measured pairs less reference) are normalized and compiled in the vector  $\mathbf{y}$

$$\mathbf{y} \in \mathbb{R}^7$$



*Input signal vector has expected value of zero and unity variance*

$$m = \mathbf{y}^T \mathbf{y}$$



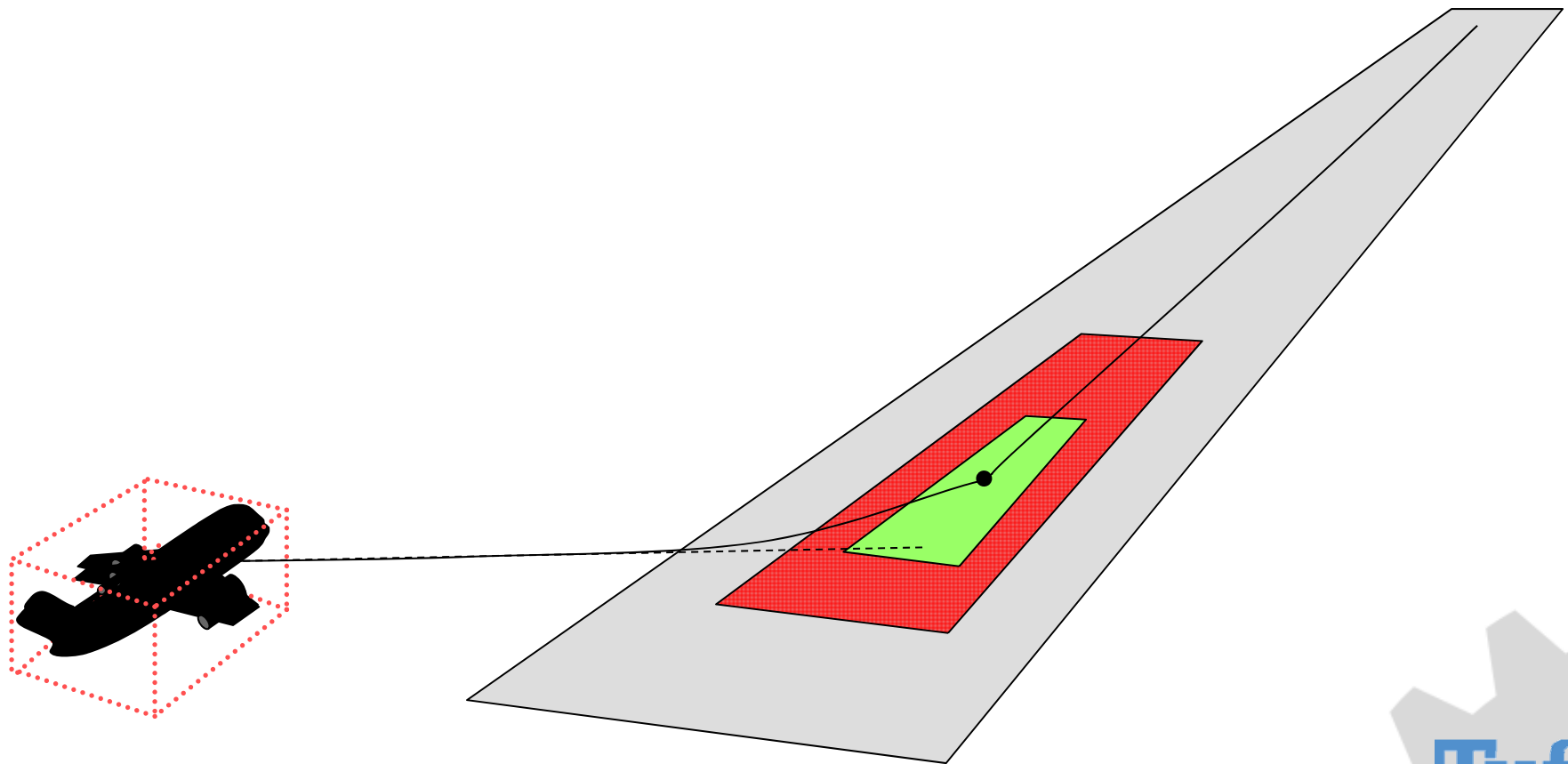
*Test statistic ( $m$ ) fuses input signal values ( $\mathbf{y}$ )*

$$\text{alert if } m > T$$



*Alert issued if test statistic ( $m$ ) exceeds threshold ( $T$ )*

SDM (and other monitors) ensure integrity for safety-critical operations

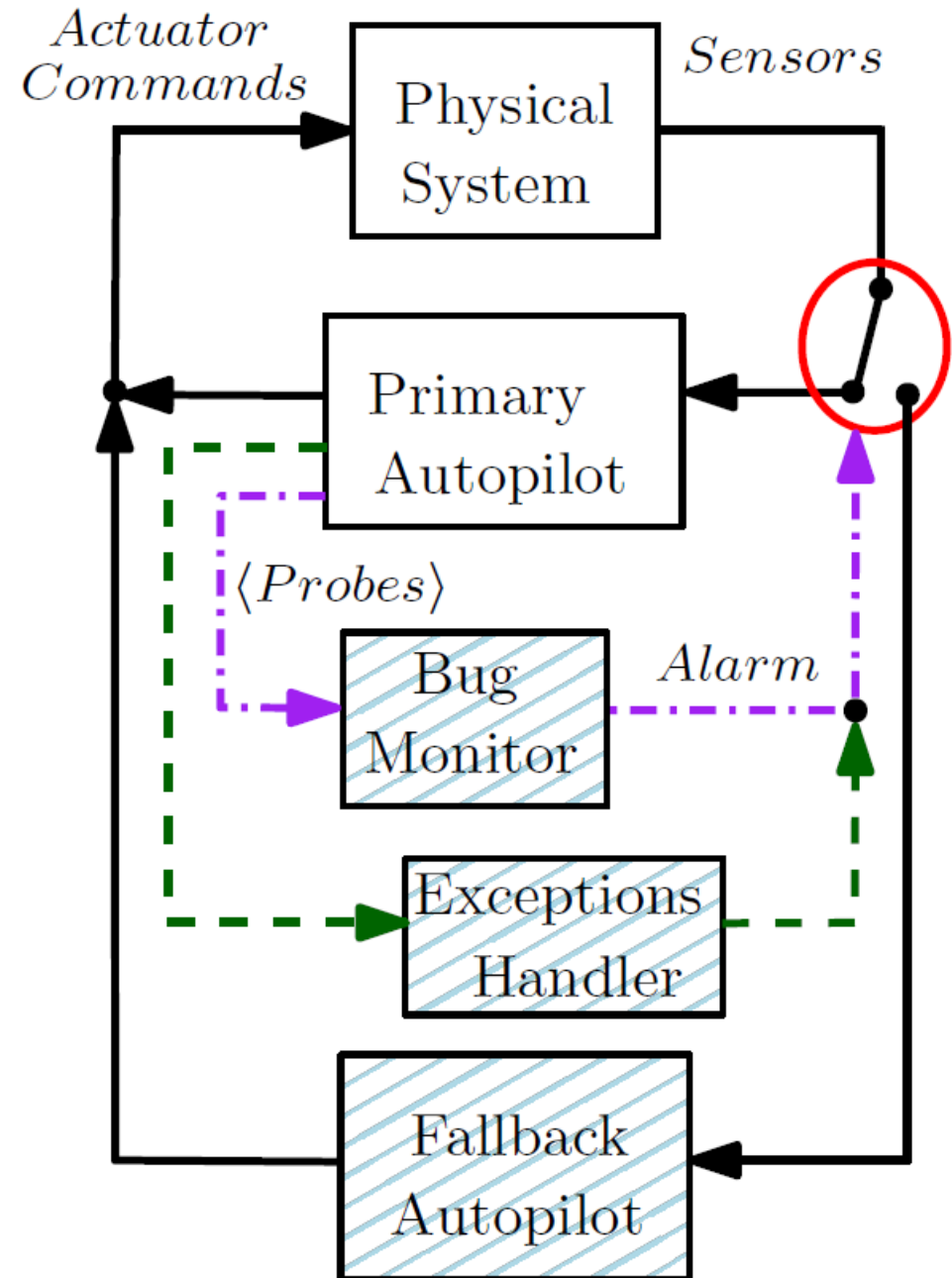


# A Bug Monitor...



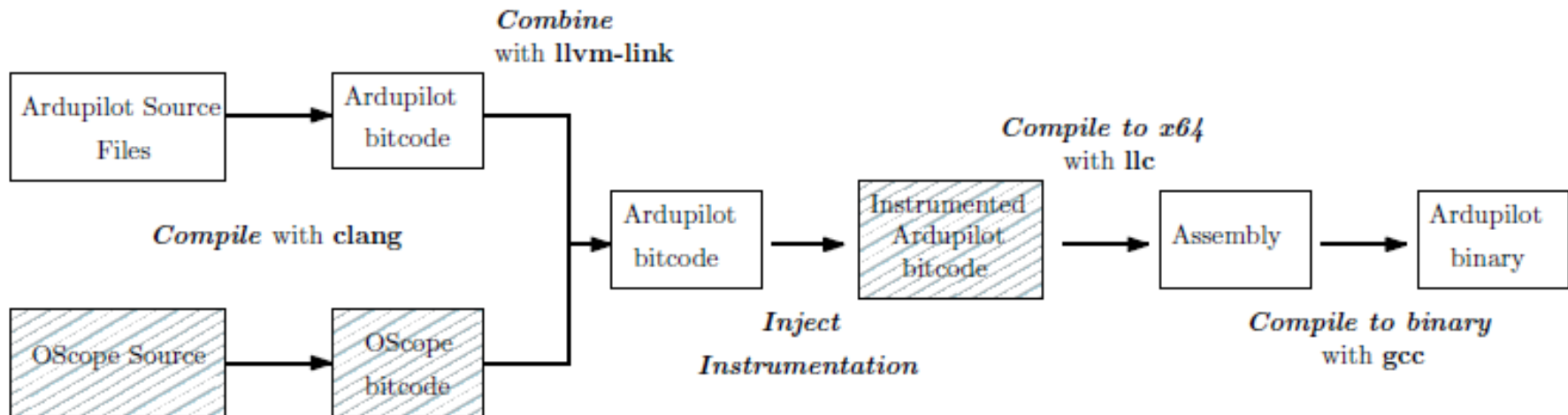
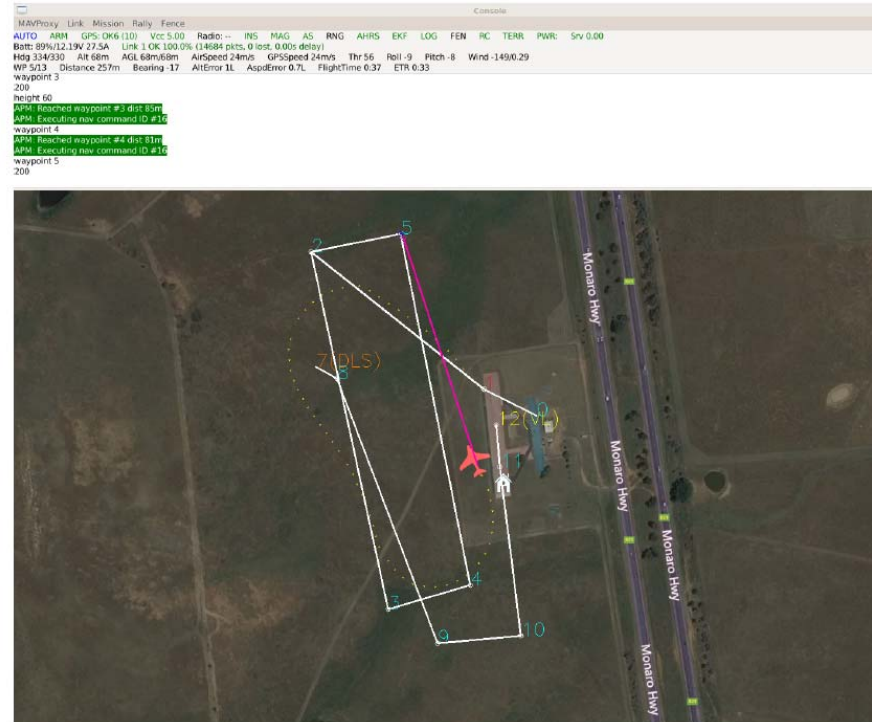
# A Bug Monitor

- Bug monitor looks for anomalous variable values
- Designer chooses a set of variables (or PROBES) to scan
- Choice of probes is critical
  - Maximize sensitivity
  - Minimize overhead



# Implementation

Monitor Ardupilot + JSBSim flight simulator





# Choice of Probes

- In current work, consider two probe choices
  - Random: Sets of 10 variables randomly selected
  - Heuristic: Sensor/actuator interfaces with physical system
- In future work, seek to optimize probe selection

$$\begin{array}{ll} \mathbf{min} & \text{overhead}(P) \\ & P \subset V \\ \text{s. t.} & \text{sensitivity}(P) \\ & \text{specificity}(P) \\ & \text{coverage}(P) \\ & \text{alert\_time}(P) \end{array}$$

# Safety Assurance

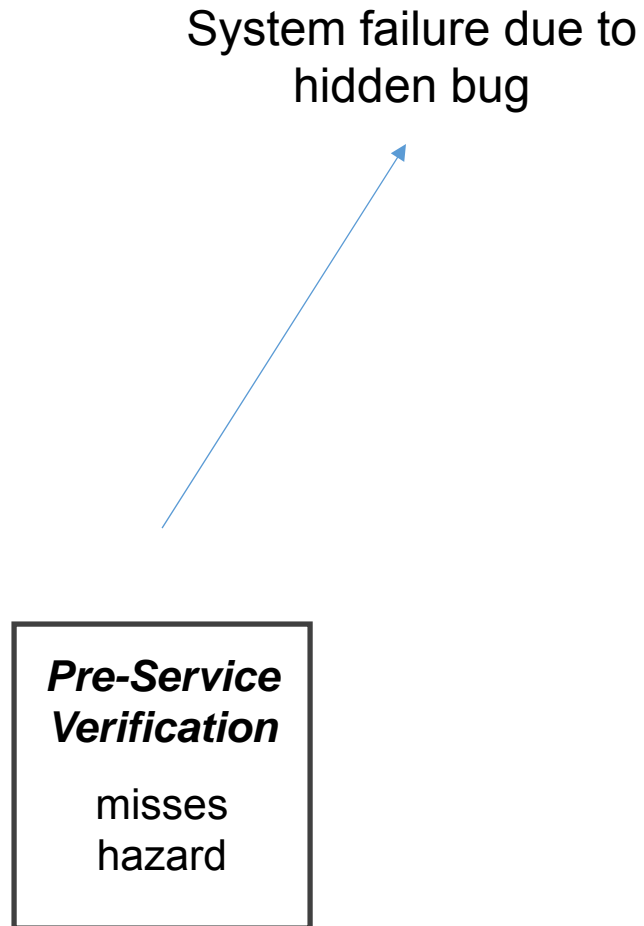


# Open Questions

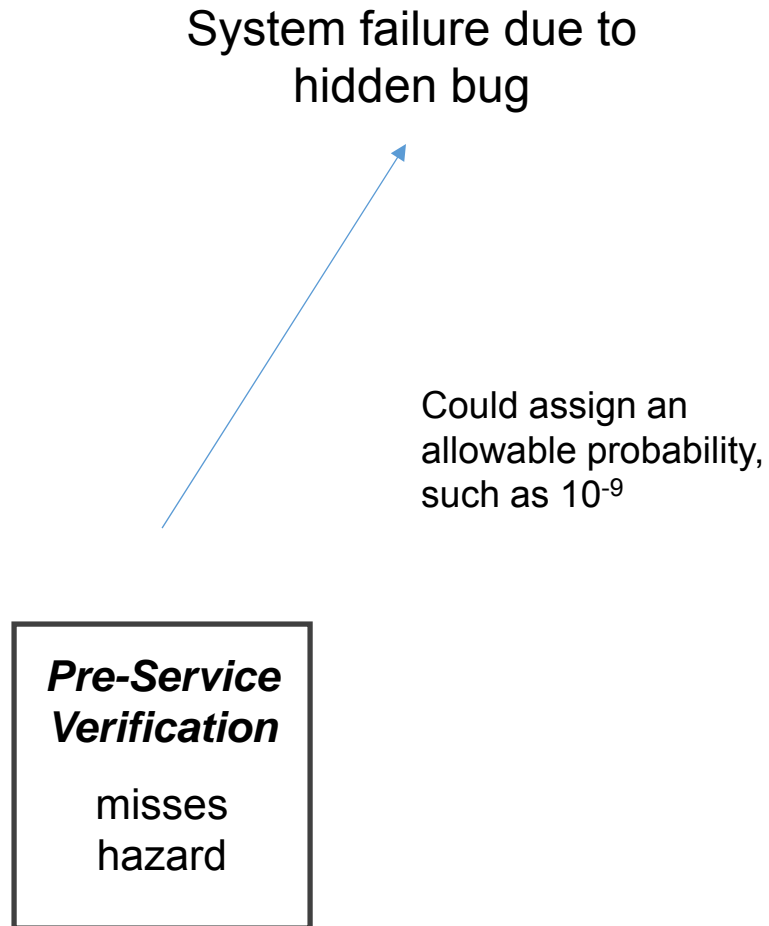
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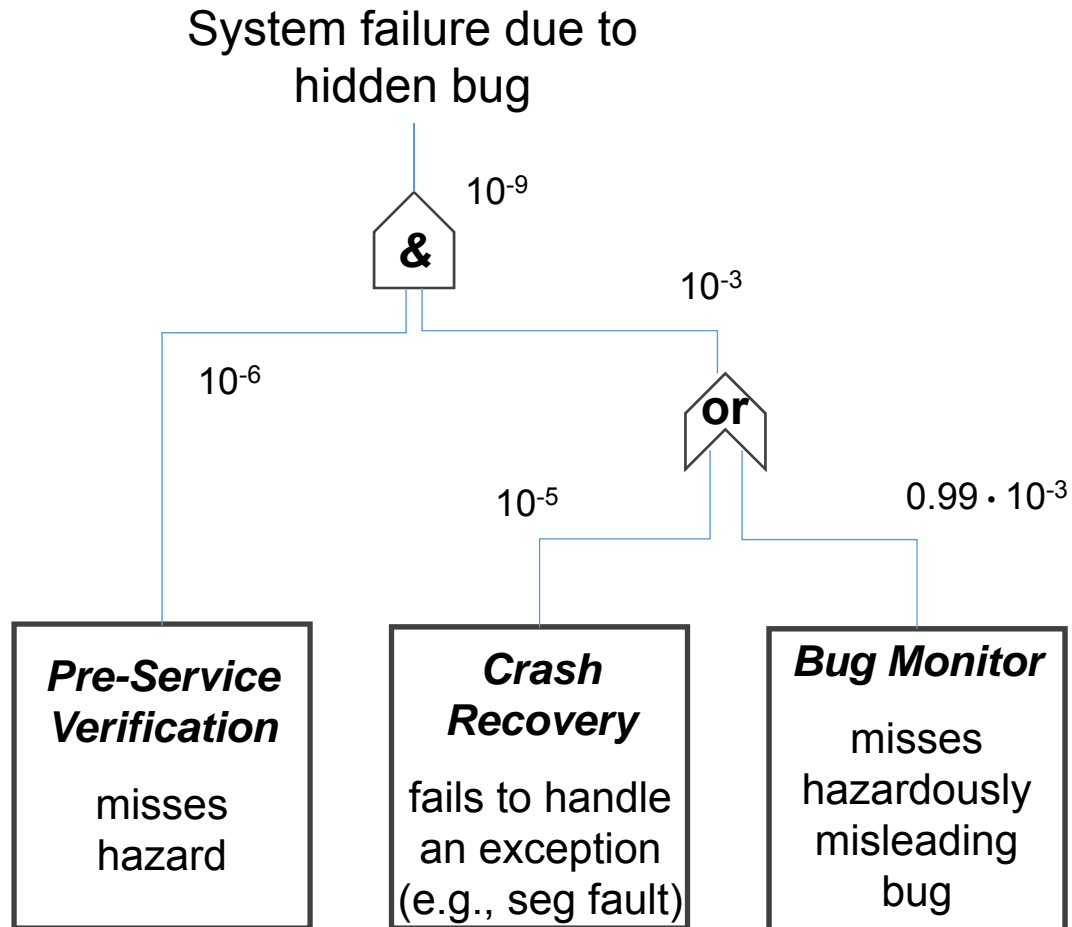
# Fault Tree Concepts: Single point of failure



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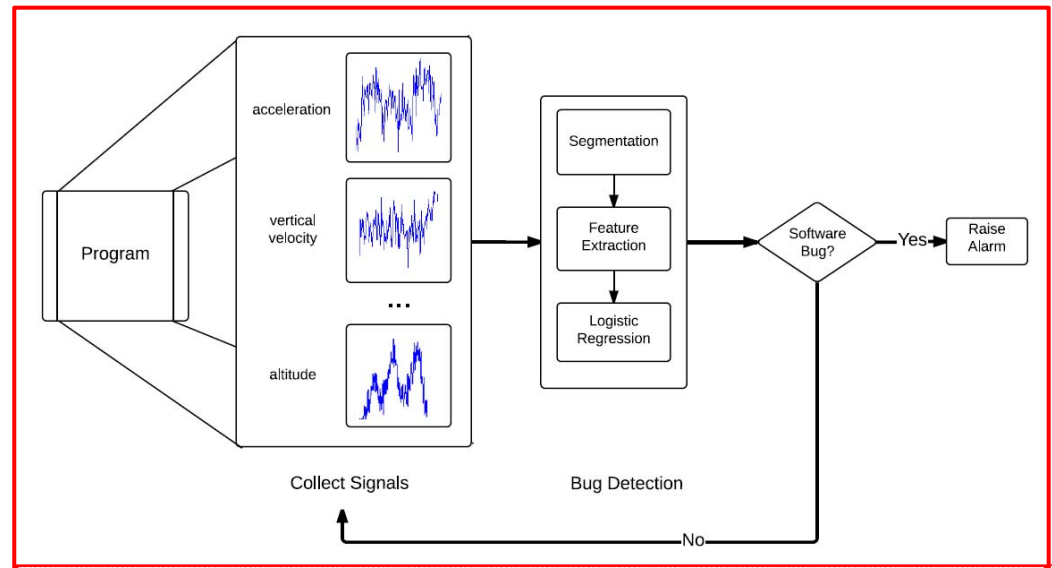
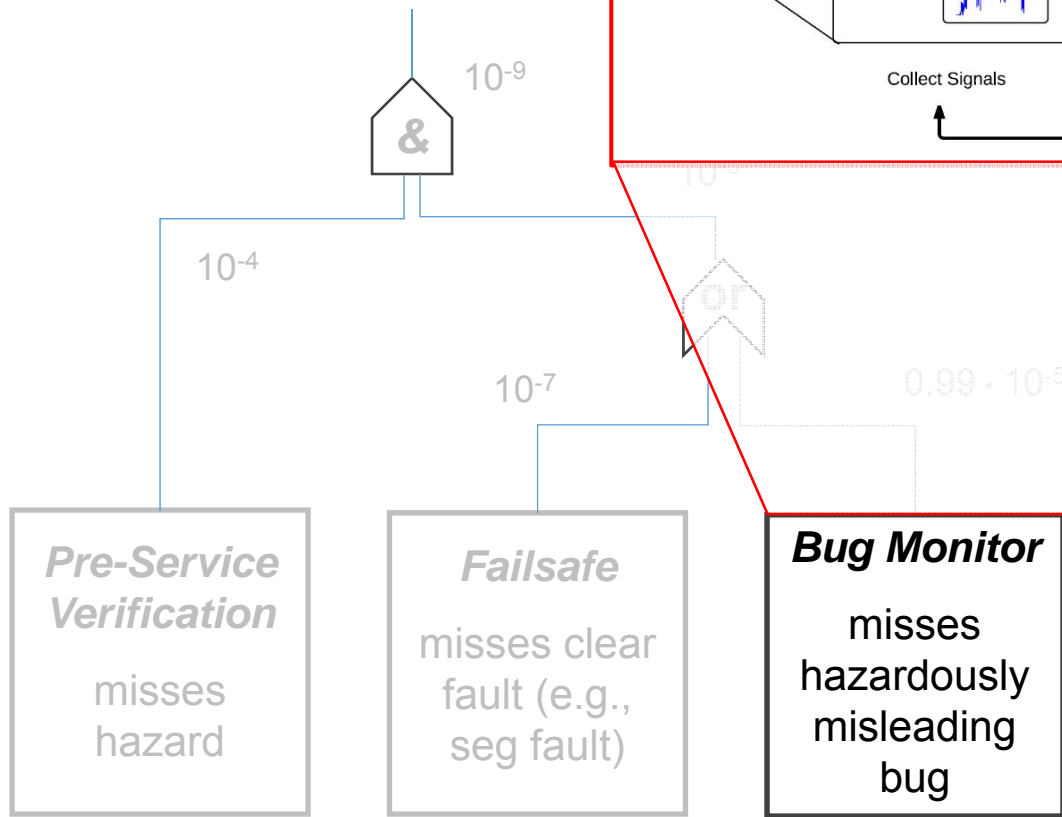


# Fault Tree Concepts: Redundancy



# Context: Monitor Function

System failure due to hidden bug



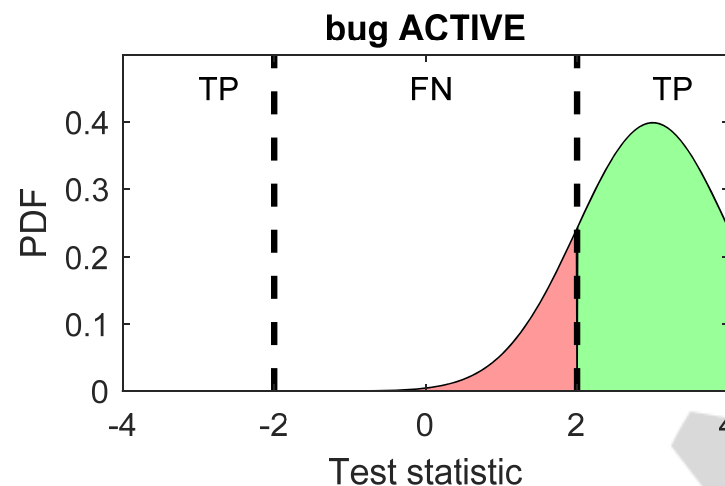
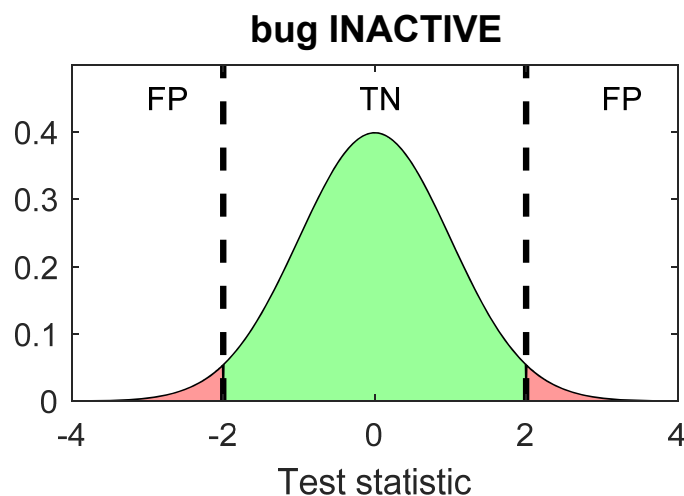
## Monitor Performance

- **Alarm rate:** Rate of both false and true alarms
- **Bug-detection envelope:** Minimum “magnitude” bug that can reliably be detected
- **Loss-of-integrity risk:** Rate of undetected, severe bugs given pre-service verification and monitoring



# Modeling Monitor to Quantify Performance

- Monitor looks for
  - Bugs that appear *infrequently* and are *difficult to find* (“Heisenbugs”)
- Monitor warns of anomalies in real time
  - Test statistic compares machine-learned model to code outputs
  - Alarm occurs if statistic exceeds threshold
- As a starting point, simplify model of test-statistic noise
  - Assume distribution unchanged when bias active, *except* for mean
  - For approximate quantification only, assume a 1D Gaussian distribution



# Performance Characterization

- **Alarm rate:**

$$P_a = P_{vf} (1 - P_{FN}) + (1 - P_{vf}) P_{FP}$$

- **Detection envelope:**

$$\mu = \text{solve} \left[ P_{FN} = \int_{-T}^T p(x - \mu) dx \right]$$

- **Loss-of-integrity risk:**

$$P_{LOI} = P_{vf} P_{FN}$$

$$\text{Threshold: } T = \text{solve} \left[ P_{FP} = 1 - \int_{-T}^T p(x) dx \right]$$

Problem parameterized by

$$P_a = \underline{P_{vf}} (1 - \underline{P_{FN}}) + (1 - \underline{P_{vf}}) \underline{P_{FP}}$$

$$P_{LOI} = \underline{P_{vf}} \underline{P_{FN}}$$

$$\mu = \text{solve} \left[ \underline{P_{FN}} = \int_{-T}^T p(x - \mu) dx \right]$$

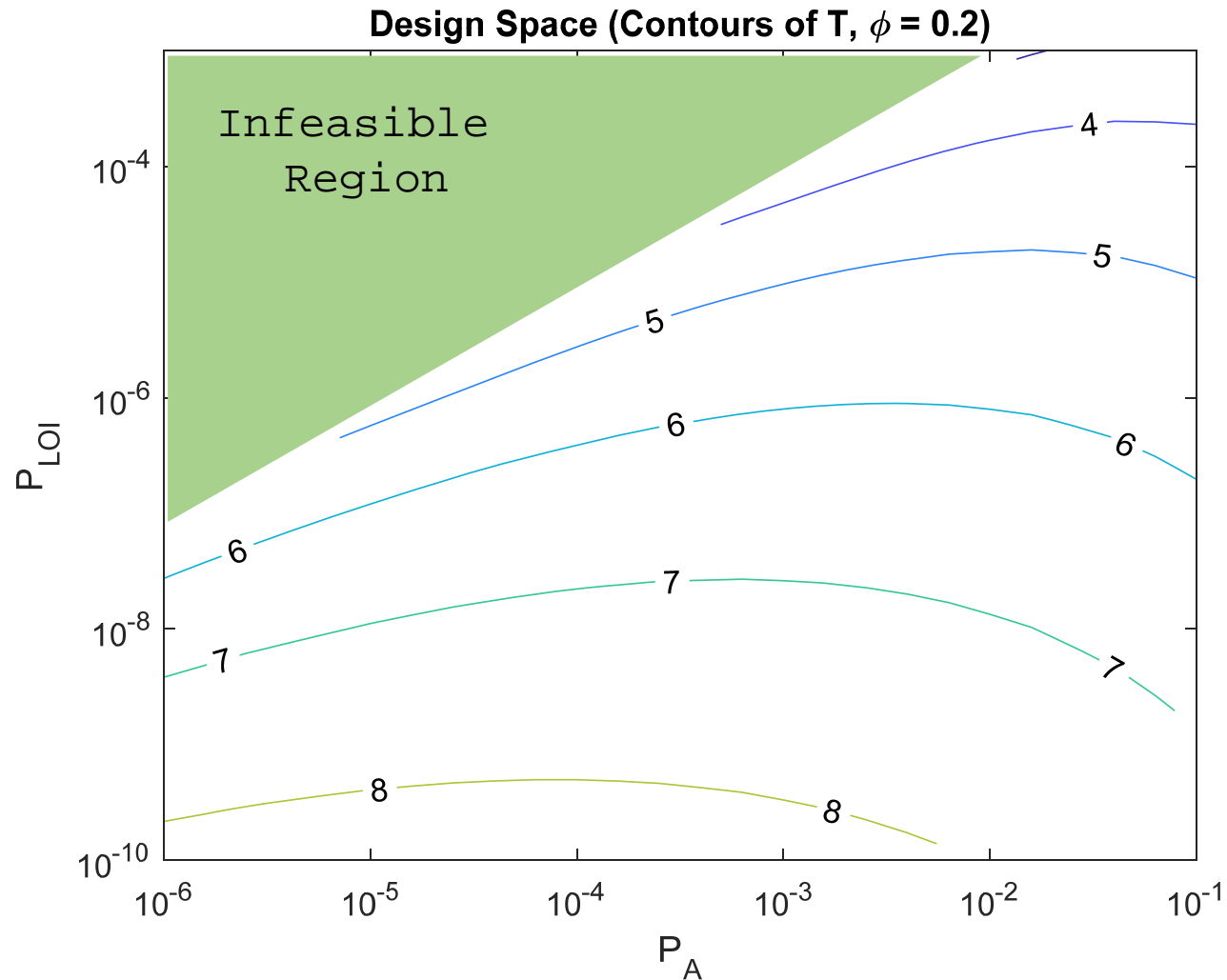
$$T = \text{solve} \left[ \underline{P_{FP}} = 1 - \int_{-T}^T p(x) dx \right]$$

- $P_{FP}$ : False-positive rate
- $P_{FN}$ : False-negative rate
- $P_{vf}$ : Verification fault probability

## Design Problem

- Find an acceptable set of output parameters ( $P_a, \mu, P_{LOI}$ )
- Selecting from space of input parameters ( $P_{FP}, P_{FN}$ ).
  - Note: Low sensitivity to  $P_{vf}$  if  $P_{vf} < 0.8 P_a$

# Achievable Designs



**Contours relate  
three performance  
criteria:**

$$\mu = f(P_a, P_{LOI})$$

For details see: Rife, Hu, and Guyer. ION GNSS+ 2018.

# Summary

- Bug monitoring demonstrated for real bugs in flight software
  - 70% sensitivity demonstrated using snapshot monitor and (!) random probes
  - Reasonable to infer higher sensitivity possible with guided probe selection and/or sequential monitoring
- Relaxing verification seems possible, even with low-sensitivity monitors
  - The Gaussian probability model is clearly very approximate
  - New challenge: Showing software robust to “small bugs”
  - Bottom line: For a given level of safety (e.g. loss-of-integrity probability), pre-service verification can be relaxed by *carefully* introducing bug monitoring

# Acknowledgements



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