

# Dynamic modelling of fares and passenger numbers for major U.S. carriers

Anthony Martin, Maximilian Martin, Steve Lawford

## ▶ To cite this version:

Anthony Martin, Maximilian Martin, Steve Lawford. Dynamic modelling of fares and passenger numbers for major U.S. carriers. 2010. hal-01021531

# HAL Id: hal-01021531 https://enac.hal.science/hal-01021531

Submitted on 11 Jul2014

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Project: Dynamic modelling of fares and passenger numbers for major U.S. carriers \*

ANTHONY MARTIN and MAXIMILIAN MARTIN (supervised by STEVE LAWFORD)<sup>†</sup>

Department of Economics and Econometrics, ENAC, France.

March 13, 2010

#### Abstract

The purpose of this project was to develop econometric models that will enable us to describe and forecast the evolution of air fares and passenger numbers for the 7 largest U.S. carriers. The principal data source was the Department of Transport's DB1B database, which contains extensive information on airline tickets sold in the US. The modelling was first conducted on the basis of pure statistical models, and we later introduced variables with real economic data, such as the air carrier's financial situation and data on the U.S. economy and also information on the individual route characteristics. Among other results, the statistical models reveal a significant drop in fares, and often also passenger numbers, after the September 11 attacks as well as a visible difference between the behaviour of Southwest Airlines , the only low-cost airline under examination, and the other six major carriers. The selection and assessment of the models in this project has been fully automated, using original code developed by the authors in the ecenometric software package EViews6 and with Excel-VBA.

<sup>\*</sup>Journal of Economic Literature (JEL) classification: C01 Econometrics, C13 Estimation, C22 Time-series models, C23 Models with panel data, C51 Model construction and estimation, C53 Forecasting and other model applications, C80 Data collection and data estimation methodology; computer programs - general, L10 Market structure, firm strategy, and market performance, L93 Air transportation (see http://www.aeaweb.org/journal/jel class system.html for classification system). Keywords: airline strategy, ARIMA models, forecasting tools, time series and panel data, U..S. major carriers.

<sup>&</sup>lt;sup>†</sup>Steve Lawford, LH/ECO, ENAC, 7 avenue Edouard Belin, BP 54005, 31055, Toulouse, Cedex 4, France. Email: steve\_lawford (at) yahoo.co.uk.

### 1 Introduction

The aim of this project is to develop econometric models that are capable of describing and forecasting the evolution of air fares and passenger numbers in the U.S. domestic market, for the 7 largest U.S. carriers, American Airlines, Continental Airlines, Delta Airlines, Northwest Airlines, Southwest Airlines, United Airlines and US Airways. The main data source used here is the official DB1B database which holds information on a large representative sample of tickets sold in the U.S. from 1993 to 2009. For certain models we also use data collected from the airlines by the Bureau of Transportation Statistics (the Form 41 Data), and data on the economic situation of the U.S. economy from the Federal Reserve Bank of St. Louis.

The first step is to find the best model that is based purely on statistical data. We examine several auto-regressive (integrated) moving average (AR(I)MA) models for both fares and passenger numbers and identify the best model, which we validate and then use for short-term forecasting. In a second step, we take the best AR(I)MA models and try to improve them by using data on the U.S. economy, that is the GDP and data on the economic situation of the airlines such as fuel expenses and operating profits. We then apply the developed models to illustrate routes, and also examine the airline's behaviour using a panel dataset and additional economic and market/route-specific characteristics.

The structure of this project is as follows. Section 2 provides background information and key features of the seven carriers of interest. Section 3 presents the core Department of Transport datasets, the filtering assumptions that were made, and the method used to deflate nominal in real prices. In section 4, we introduce the Box-Jenkins methodology for building statistical ARIMA time-series models. This is applied to each of the carriers in turn, the models are carefully validated, and used for short-term and dynamic forecasting. Section 5 discusses additional economic variables that are used in an effort to improve the ARIMA models. Section 6 applies the modeling to several illustrative routes. In Section 7, we build a number of purely economic models for fares, which are

used for comparison and to aid intuition. Section 8 concludes the project. The Appendix contains automated model selection output, the EViews 6 and Excel VBA code that was *entirely written by the authors* during the project (for data treatment and analysis), and several Python codes for initial treatment (cleaning, formatting, etc.) of the DB1B and economic data. The report was written and compiled using the typesetting software WinEdt and the LaTeX language.

## Contents

1	Intr	oduction	1
<b>2</b>	Ma	jor U.S. airlines	6
	2.1	American Airlines	6
	2.2	Continental Airlines	7
	2.3	Delta Air Lines	8
	2.4	Northwest Airlines	10
	2.5	United Airlines	11
	2.6	US Airways	12
	2.7	Southwest Airlines	13
3	Dat	a description and preliminary analysis	15
	3.1	Core data	15
		3.1.1 DB1B Ticket data	15
		3.1.2 DB1B Coupon data	22
		3.1.3 Assumptions and inflation data	26
4	Mo	del construction and estimation	32
	4.1	Fares	33
		4.1.1 Simple linear regressions	33
		4.1.2 ARMA models	35
		4.1.3 Selecting the best ARMA model (theory)	37
		4.1.4 Application of ARMA models to 7 U.S. carriers	42
		4.1.5 Summing up	62
		4.1.6 Forecasting	64

	4.2	Passengers
		4.2.1 Summing up
		4.2.2 Forecasting
5	Inse	rtion of economic data 93
0	5.1	
	0.1	
		5.1.1 Form 41 Financial Data
		5.1.2 B-1 Table Data
		5.1.3 P-10 Table Data
		5.1.4 P-12 Table Data
		5.1.5 P-12A Table Data
		5.1.6 GDP
	5.2	Insertion of economic data into ARIMA models for fares
6	Reg	ressions for specific routes 129
	6.1	Chicago (ORD) - Atlanta (ATL)
	6.2	Los Angeles (LAX) - New-York (JFK)
	6.3	Baltimore (BWI) - Seattle (SEA)
7	Pur	ely economic models 149
8	Con	cluding remarks 156
	8.1	Acknowledgements
$\mathbf{A}$	Арр	endix 160
	A.1	ARIMA models (automated outputs)
	A.2	EViews6 Code
		Excel VBA-code for Form 41 data treatment
	11.U	= 1  Add  if  1  for  1  or  1

A.4	Python Code	 	 	 •		•		 •				•				 214

5

### 2 Major U.S. airlines

#### 2.1 American Airlines

American Airlines (IATA code AA) is one of the world's largest airlines (in terms of traffic and operating revenues).<sup>1</sup> Established in 1930 in New York, the airline initially operated scheduled services between Boston, New-York, Chicago, Dallas and Los Angeles. In 1979, one year after the U.S. deregulation of the domestic network, American Airlines moved its headquarters to Fort Worth in Texas.<sup>2</sup> As a major carrier (defined as having more than \$1 billion in annual operating revenues), the airline chose to operate a hub-and-spoke network, with 3 main bases in San Jose (California), Raleigh (North Carolina) and Nashville (Tennessee). During the 1980s and 1990s, American Airlines largely expanded its network, throughout the domestic U.S., and internationally. In 1999, the airline created the OneWorld global airline alliance with British Airways, Canadian, Cathay Pacific and Quantas.<sup>3</sup> In April 2001, American purchased the assets of the near-bankrupt Trans World Airlines (TWA), at the same time acquiring its hub in Saint Louis. The September 11, 2001, terrorist attacks (2 of which involved American Airlines aircraft) had serious consequences on the financial situation of the company.<sup>4</sup> In July 2005, American Airlines announced its first quarterly profit since September 2001. American Airlines is the only legacy carrier to survive bankruptcy-free.

American Airlines is a subsidiary of the AMR corporation. Since 2004, the Chairman, President, and Chief Executive Officer of AA and AMR has been Gerard Arpey. The airline is now based in

<sup>&</sup>lt;sup>1</sup>See the 2009 economic report of the Air Transport Association. Refer to [2].

<sup>&</sup>lt;sup>2</sup>For further information on U.S. deregulation of domestic traffic, refer to [4].

 $<sup>^{3}</sup>$ This alliance was started by 5 of the world's largest airlines at the time, with a driving strategy of expansion of the international network of each of these airlines, through code-sharing and then an immunized alliance. For American Airlines in particular, it was an opportunity for more efficient cooperation on Transatlantic routes with British Airways and on Pacific routes with Quantas and Cathay Pacific.

<sup>&</sup>lt;sup>4</sup>In fact, American airlines managed to reduce the immediate impact of the September 11 attacks. As a consequence the airline did not file for bankruptcy, whereas Delta, Northwest, United and US Airways did and consequently benefited from the help of the federal government. Therefore the airline found itself at a competitive disadvantage compared to these 4 major airlines. See also [3].



Dallas/Fort Worth and has 2 main bases at Chicago O'Hare International and Miami International.

Figure 1: Domestic traffic of American Airlines from Fort Worth International Airport (ENAC Air Transport Data).

#### 2.2 Continental Airlines

Continental Airlines (IATA code CO) is the fourth largest U.S. airline in terms of operating revenues and revenue passenger miles (RPMs). Established in 1934, and based in Houston (Texas), Continental offers domestic, regional and international flights. Created by Walter Varney (who also founded United Airlines), Continental Airlines was originally a regional airline, smaller (in terms of number of routes) than TWA, American Airlines and United. Under its CEO Robert Six, the airline expanded significantly between 1959 and 1978, and was the first carrier to introduce the Boeing 707 and then the Boeing 747 on its domestic routes. Six was also the first to introduce an economy fare on the Chicago-Los Angeles route. Continental offered services from Denver to Chicago, Seattle, Los Angeles and Honolulu. After deregulation, the carrier continued to expand significantly, notably towards the Eastern coast of the U.S., into Miami and New York. However, its acquisition by the airline holding company Texas Air, and a series of reorganizations, led to a first Chapter 11 bankruptcy filing from 1983 to 1986.<sup>5</sup> In 1988, Continental Airlines formed the first international alliance with the Scandinavian airline SAS. From 1990 to 1993, the airline entered its second bankruptcy. Hired in 1993 in order to salvage the company, the new CEO of Continental, Gordon Bethune, began to focus more on customer satisfaction than on fares, and made the airline in 2004 the "most admired global airline" according to Fortune magazine.<sup>6</sup> In the same year, Continental entered the SkyTeam alliance between Air France and Delta Airlines, along with Northwest and KLM. This alliance was initiated by Northwest, which at that moment had the control over all decisions taken by Continental. After the acquisition of Northwest by Delta Air Lines in 2008, Continental Airlines decided to withdraw from the SkyTeam alliance and join the Star Alliance in order to cooperate with United Airlines.<sup>7</sup> This change of alliance was effectively completed in October 2009.

The CEO of Continental Airlines since 2004 has been Larry Kellner, following the retirement of Gordon Bethune. Since the latter was a Boeing executive before managing the airline, from 1994 Continental Airlines has began to renew its fleet only with Boeing aircraft. The three main bases of Continental Airlines are Houston, New York (Newark) and Cleveland.

#### 2.3 Delta Air Lines

Delta Air Lines (IATA code DL), established in 1934, is currently the main U.S. major carrier, in terms of traffic and operating revenues. The airline was created in Macon, Georgia, in 1924, as part of the company Huff Daland Dusters. The headquarters was moved to Atlanta in 1941. Beginning

 $<sup>^{5}</sup>$ Chapter 11 is a section of the United States Bankruptcy Code, which allows a company to reorganize rather than be liquidated. This reorganization is performed by the debtor, to whom the U.S. government provides mechanisms for it to restructure its business, especially the ability to acquire loans and financing from new lenders without clearing its previous debts.

 $<sup>^{6}</sup>$ Refer to [1].

<sup>&</sup>lt;sup>7</sup>Indeed, Continental had several merger discussions with United Airlines between 2006 and 2008, and the CEO of Continental stated on November 2009 that "We are watching Delta to see whether Delta outperforms us financially" before reconsidering the merger with United [7].



Figure 2: Domestic traffic of Continental Airlines from George Bush Intercontinental Airport (ENAC Air Transport Data).

its passenger services on the West coast, the acquisition of Northeast Airlines in 1972 greatly helped the expansion of the carrier in the Eastern U.S. In 1955, it was the first airline to implement the hub-and-spoke system. In 1987, Delta merged with Western Airlines, acquiring the hubs of Salt Lake City and Los Angeles (Los Angeles International Airport). However, the main acquisition of Delta Airlines was its absorption of the bankrupt airline PanAm in 1991. In 2000, the carrier founded the SkyTeam alliance with Air France, Aeromexico and Korean Air. Four years later, Delta began an important restructuration of its services in an effort to improve profitability and avoid bankruptcy. Despite these measures, the airline filed for Chapter 11 bankruptcy protection in September 2005, and returned as an independent carrier in April 2007. In October 2008, Delta Air Lines and Northwest Airlines (which was part of the SkyTeam alliance since 2004) merged under the Delta identity.

The CEO of Delta is Richard Anderson. As for Continental Airlines, Delta only operates with

Boeing aircraft.<sup>8</sup> The carrier, based in Atlanta, has 3 main U.S. bases: Cincinnati, New York (JFK Airport) and Salt Lake City.

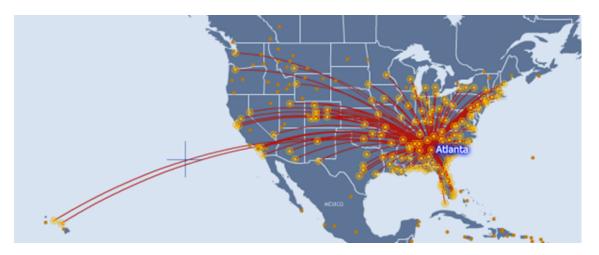


Figure 3: Domestic traffic of Delta Air Lines from Hartsfield-Jackson Atlanta International Airport (ENAC Air Transport Data).

#### 2.4 Northwest Airlines

At the time of writing, Northwest Airlines (IATA code NW, established 1926) no longer exists and the Northwest brand name will be phased out by 2010. However, as its merger with Delta Airlines only took place in 2008, for the largest part of the time-frame in this study Northwest Airlines existed as an independent carrier. As for most U.S. majors, Northwest has more than 50 years of history, that began at its present headquarter city Minneapolis/St.Paul. Besides Minneapolis/St.Paul, Northwest operates two other U.S. hubs in Detroit and Memphis. Outside of the U.S., Northwest has a strong presence at Tokyo Narita and Amsterdam. Amsterdam is the hub airport for KLM Royal Dutch Airlines, with which Northwest pioneered the field of airline alliances/cooperations by entering a joint-venture that includes revenue sharing and Frequent Flyer

<sup>&</sup>lt;sup>8</sup>In 1997, Delta announced that the airline would buy only Boeing aircraft for the next 20 years, in order to strengthen cooperation and as a consequence the flexibility and price advantages following from this [5].

Program cooperation. Today, Northwest is, as its "predator" Delta, member of the SkyTeam alliance. Northwest's fleet ranges from DC9-30s with 100 seats to 747-400s with 403 seats. All the aircraft are operated in a 2-class configuration with Economy and Business or First class. In 2008 it transported 65.5 million passengers and employed 34,400 people. Its net loss lay at \$6.2 billion.

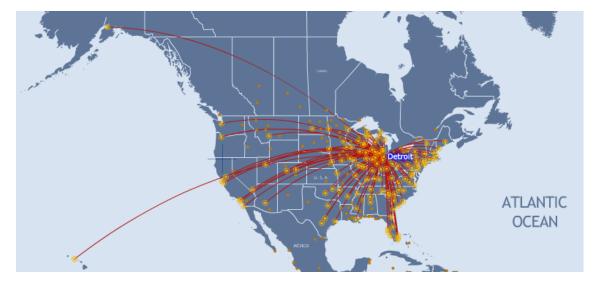


Figure 4: Domestic traffic of Northwest Airlines from Detroit Metro Airport (ENAC Air Transport Data).

#### 2.5 United Airlines

United Airlines (IATA code UA, established 1931) has developed to become one of the largest airlines in the U.S. and also worldwide. In 1997 United was, together with Air Canada, Lufthansa, SAS Scandinavian Airlines and Thai Airways, a founding member of Star Alliance, which is now the world's largest airline alliance. According to the Air Transport Association of America's 2008 Annual Report, United Airlines was third largest carrier by revenue passenger miles (RPM). At 109.8 billion RPM it was about 20 billion RPM behind American Airlines and 30 billion ahead of Continental Airlines. The airline is headquartered in Chicago, and operates hubs at Chicago O'Hare, Washington Dulles, San Francisco and Denver (the latter is purely domestic). From its hubs it serves destinations on all continents except Africa. The first African destinations will be Accra and Lagos in 2010. United operates 360 aircraft (2008) ranging from the Airbus A319 to the Boeing 747-400 in a 3- or 4-class-layout. Its Economy product has recently been supplemented at the top end and below Business/First Class with the introduction of the so-called "Economy Plus" class which is available on all United aircraft. Several smaller airlines fly under the United Express brand name to supplement United's domestic network.



Figure 5: Domestic traffic of United Airlines from Chicago O'Hare International Airport (ENAC Air Transport Data).

#### 2.6 US Airways

US Airways (IATA code US, established 1939) is the smallest of the airlines we will look at in this project. In 2008, its transport performance lay at 60.5 million RPM, trailing Southwest, and it employed 32,700 people while posting a loss of \$2.2 billion. Before its merger with America West in 2005, US Airways mainly served the eastern part of the U.S. from its hubs in Philadelphia and Charlotte. The 2005 merger with America West added America West's Phoenix hub to the network.

Since 2004, US Airways has been a member of Star Alliance and operates 349 aircraft (296 aircraft fly with other airlines such as Mesa Air and PSA Airlines under the US Airways Express brand). All aircraft are equipped with an Economy and Business or First class, the latter called "Envoy" class. The airline is headquartered in Phoenix and mainly serves destinations in North America and Europe.



Figure 6: Domestic traffic of US Airways from Charlotte Douglas International Airport (ENAC Air Transport Data).

#### 2.7 Southwest Airlines

Southwest (IATA code WN, established 1967) is the only low-cost carrier considered in this project. However, even though it is low-cost and also the youngest among the carriers we examine, Southwest is the largest by number of passengers transported (88.5 million in 2008). It is quite different compared to the other large U.S. carriers. For example, Southwest Airlines posted a net profit (\$0.18 billion) in 2008. The other main differences apart from its age and low-cost/low fare concept are that it has a single-class 737-only fleet (namely 181 737-300 and 338 737-700 with 137 seats each and 25 737-500 with 122 seats) and operates exclusively on U.S. domestic routes. Southwest is not part of any larger alliance, and only has agreements with Canadian carrier Westjet and Mexico's Volaris. Southwest is headquartered in Dallas. Its main bases are Las Vegas, Chicago, Phoenix, Baltimore/Washington, Houston, Dallas, Denver, Oakland, Los Angeles and Orlando.

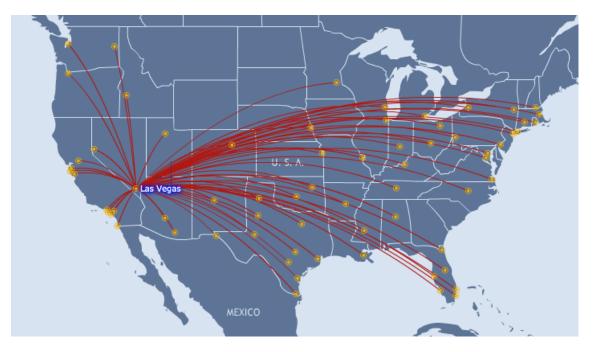


Figure 7: Domestic traffic of Southwest Airlines from Las Vegas McCarran International Airport (ENAC Air Transport Data).

### **3** Data description and preliminary analysis

#### 3.1 Core data

In this project, we will make use of a number of rich statistical data sets from the American Bureau of Transportation Statistics (BTS).<sup>9</sup> We are particularly interested in the BTS Airline Origin and Destination Survey (DB1B). This dataset is a 10% random sample of scheduled airline tickets from reporting carriers. It gives information on domestic itineraries within the U.S. domestic market. The data has been reported quarterly from 1993 to 2009 (we have access to reliable data until the first quarter of 2009), giving us data over 65 quarterly time periods.

The survey is divided into 3 related databases: Market, Coupon, and Ticket. We will only use the second and third for this project. In fact, the Market database mostly uses the data contained in the Coupon and Ticket databases to report a new presentation of itineraries, displaying the number of passengers, the fares, the time period, the ticketing, operating and reporting carriers and the origin and destination airport for each segment of the flight.

#### 3.1.1 DB1B Ticket data

This database gives, for each domestic itinerary reported by a reporting carrier, the origin and destination of the flight, the nominal itinerary fare, the number of passengers per ticket, and the length of the trip, among other variables. Figure 8 presents a small excerpt from this database, highlighting the main variables that are of use to us.

• ItineraryID (ItinID): This variable links the DB1B databases Coupon and Ticket, and allows us to compare and merge the data. One ticket has a unique "ItinID", and it can contain several coupons (segments) with that same ID.

<sup>&</sup>lt;sup>9</sup>This agency, created in 1992, has been collecting data from any mode of transportation for more than 15 years, creating huge microeconomic and other databases in many areas (infrastructure, economic, financial, social, demographic, energy, freight or passenger travel). Much data is freely available online.

ItineraryID	Number of Coupons	Year	Quarter	Origin Airport	Origin state	Reporting Carrier	Passengers	Itinerary Fare	Distance
200912901646	1	2009	1	FLL	FL	WN	2.00	215.00	793.00
200912901647	1	2009	1	FLL	FL	WN	1.00	218.00	793.00
200912901648	1	2009	1	FLL	FL	WN	2.00	221.00	793.00
200912901649	1	2009	1	FLL	FL	WN	6.00	227.00	793.00
200912901650	1	2009	1	FLL	FL	WN	3.00	248.00	793.00
200912901651	1	2009	1	FLL	FL	WN	1.00	250.00	793.00
200912901652	1	2009	1	FLL	FL	WN	2.00	258.00	793.00
200912901653	1	2009	1	FLL	FL	WN	3.00	260.00	793.00
200912901654	1	2009	1	FLL	FL	WN	1.00	272.00	793.00
200912901655	1	2009	1	FLL	FL	WN	1.00	31.00	793.00
200912901656	2	2009	1	FLL	FL	WN	1.00	117.00	1916.00
200912901657	2	2009	1	FLL	FL	WN	1.00	148.00	1645.00
200912901658	2	2009	1	FLL	FL	WN	2.00	272.00	970.00
200912901659	2	2009	1	FLL	FL	WN	1.00	287.00	970.00
200912901660	4	2009	1	FLL	FL	WN	1.00	267.00	1627.00
200912901661	4	2009	1	FLL	FL	WN	1.00	302.00	4980.00
200912901662	2	2009	1	FLL	FL	WN	1.00	5.00	1381.00
200912901663	2	2009	1	FLL	FL	WN	1.00	88.00	1381.00
200912901664	2	2009	1	FLL	FL	WN	2.00	151.00	1381.00
200912901665	2	2009	1	FLL	FL	WN	1.00	164.00	1381.00
200912901666	2	2009	1	FLL	FL	WN	1.00	173.00	1381.00
200912901667	2	2009	1	FLL	FL	WN	1.00	214.00	1381.00

Figure 8: Excerpt from the DB1B Ticket database for 2009Q1, where FLL is Fort Lauderdale Airport (IATA airport code), FL is Florida, WN is Southwest (IATA airline code), the itinerary Fare is nominal (in U.S.\$), and distance is measured in miles. In the text, we take a closer look at the 3 highlighted itineraries.

- Number of Coupons: It is essential to know, for a given itinerary, the number of segments contained in the itinerary. The minimal number of coupons is 1, and reaches 23. Figure 9 shows, for example, the distribution of the number of coupons bought by passengers on an itinerary in 2008. We can see that the proportion of tickets with 7 coupons or more seems negligible (it represents, in 2008, 0.25% of all tickets sold).
- Year and Quarter: Tickets are reported every quarter, and it would be very difficult to obtain the exact date of the flight for each ticket (this is not available through DB1B), which would add considerable complexity to the databases, although it would enable us to model for example intraweek, weekly and monthly effects. From 1993Q1 to 2009Q2, there are consequently 65 different periods in the database.

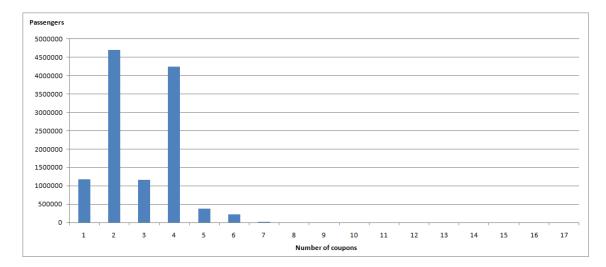


Figure 9: Coupons bought by passengers on an itinerary in 2008, for all U.S. reporting carriers. We observe that the proportion of tickets with 2 or 4 itineraries represents more than 66% of all tickets sold. In fact, this graph does not give us the proportion of round trips or changes of planes, so we cannot state whether the 4,250,000 4-coupon itineraries are one-stop returns or one-way trips with 4 successive changes of plane.

Consider the number of passengers who took a flight during the year 2008 (Figure 10). We can observe that the quarter when people travelled the most was the second quarter, with 500,000 more travellers than during the first quarter of 2008. About 2,800,000 passengers travelled during 2008Q1 and a similar number during 2008Q4.

• Origin airport and state: We have the origin airport for each ticket. The DB1B Coupon dataset will later provide the entire route followed by each passenger. Figure 11 shows, for example, the distribution of the passengers having a trip in 2008 from a given state of origin. We can see that the outgoing traffic comes mostly from California, Texas, New York, Florida, Illinois and Pennsylvania, which are also the most populous U.S. states.<sup>10</sup> As a consequence, we could try to avoid this effect of the most populous states on the traffic results, by dividing the number of passengers for a given state by the population of this state (Figure 12). We

<sup>&</sup>lt;sup>10</sup>2007 population estimates from the U.S. Census Bureau. See http://www.census.gov/.

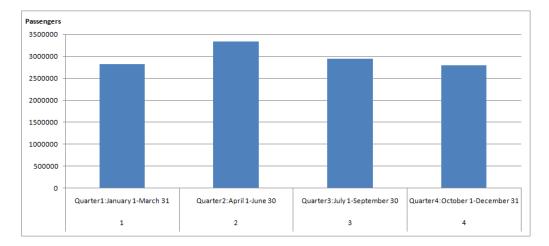


Figure 10: Number of passengers per quarter in 2008.

can see from this graph that this kind of concentration of the traffic is very high for the less populous U.S. states, especially for the District of Columbia. In 2008, a number of passengers equivalent to half the population of Washington D.C. left the capital of the United States for domestic travel. We can also note the high percentage for Alaska, which can be explained by the low population of the state and the difficulty for the inhabitants to make domestic trips in the U.S. with other means of transportation than aircraft. The same arguments and the high level of tourism for Hawaii can explain the high percentage calculated for the island. For Nevada, the low population compared to the high traffic from Las Vegas and Reno also explains the high percentage for the state. Returning to the first graph, we can also note the very low outgoing traffic in Dakota, Wyoming and West Virginia, which are also among the less populated U.S. states.

• **Reporting carrier:** The reporting carrier is the airline reporting the data of tickets and coupons to the Bureau of Transportation. We can examine the distribution of the passengers in 2008 by respective reporting carrier (Figure 13). We note that the largest reporting airlines (in terms of number of passengers) are the 6 legacy carriers presented in the first part of this

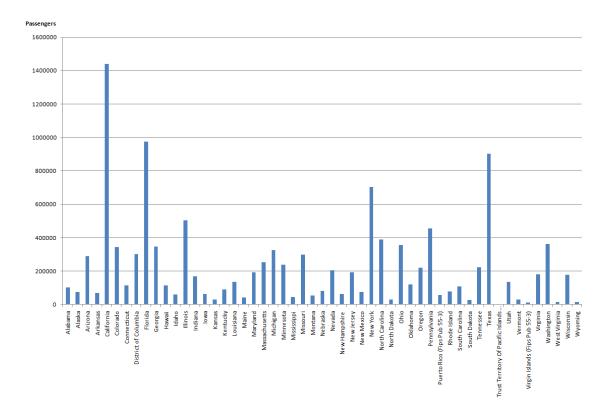


Figure 11: State of departure for 2008 itineraries.

project, and the low-cost carrier Southwest. These airlines are major carriers (as defined above), and reported the tickets of more than 600,000 passengers in 2008. The largest carrier on this graph is Southwest: we could consequently tend to think that the low-cost carrier was the most important (reporting) carrier for domestic travel in the U.S. in 2008. Nevertheless we have to keep in mind that the reporting carrier may not be the operating carrier, especially when a carrier like the 6 other legacy carriers uses code-sharing to develop its hub-and-spoke network. The code-sharing effects are very difficult to capture here, as the different alliances between airlines can change over time.

We also observe that there are other significant reporting carriers in the U.S.: SkyWest,

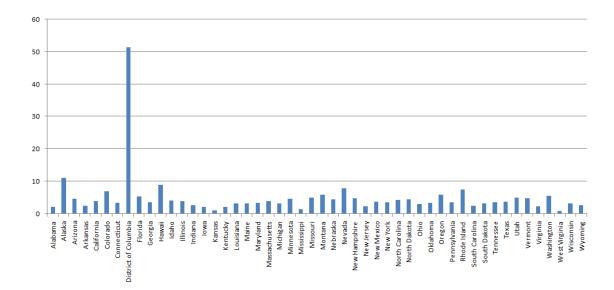


Figure 12: Number of passengers for 2008 itineraries as a percentage of the population estimates by U.S. state.

AirTran and American Eagle. SkyWest is a regional airline headquartered in Utah, and has recently secured a partnership with the low-cost carrier AirTran. This partnership will be effective in February 2010, and may strengthen the position of these 2 airlines in the U.S. domestic market. American Eagle is a subsidiary of American Airlines.

- **Passengers:** The number of passengers buying a ticket for a given route at a given price with a given reporting carrier. This number can be sometimes very high (up to 1000 passengers with the same ItinID: it does not mean that all these passengers know each other and bought one ticket for 1000 individuals, but instead that 1000 passengers bought a similar ticket during the quarter (the same route, with the same carrier(s), and at the same price), which enables the DOT to compress the dataset to some extent.
- Itinerary fare: This is the nominal U.S.\$ fare paid for the ticket. We saw, looking at the database, that some fares appear unusual, as they seem to be very high for domestic travel, or

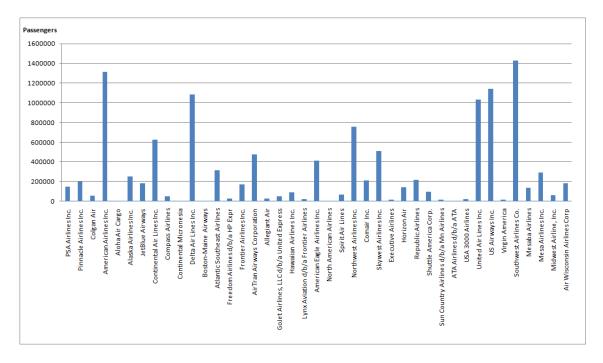


Figure 13: Carrier reporting 2008 itineraries.

very low (for example, 7 euros for a 3-coupons itinerary from Texas with Southwest). Indeed a passenger, even flying with a low-cost carrier such as Southwest, must pay some fees, charges and taxes: in order to remove possible errors from the database, we decided to impose upper and lower bounds on the fare data. We develop the computation of these bounds in section 3.1.3 below (Assumptions).

• **Distance:** The length of the route is expressed in miles. It may be interesting to see whether we can relate this distance to the fares proposed by the airlines on specific routes.

We now take a general look at 3 illustrative itinerary IDs (highlighted in red on Figure 8).

• ItinID 200912901650: This line represents one ticket, an itinerary of 1 (number of coupons) flight which took place during the first quarter of 2009. This itinerary began at Fort Lauderdale Hollywood International Airport (FLL), in Dania Beach, in the South of Florida (FL). This

ticket was reported by Southwest to the Bureau of Transportation. On this itinerary, 3 passengers bought a ticket at a nominal fare of \$248 per passenger, and we see that they covered 793 miles.

- Itin 200912901658: Starting from the same airport (FLL), in the same quarter, two other passengers performed 2 flights (perhaps a round trip), covering an itinerary of 970 miles which cost nominal \$272 per passenger. This ticket was also reported by Southwest.
- Itin 200912901660: Another passenger, with the same initial conditions of time and place, covered 1627 miles with 4 successive flights (perhaps a non-direct round trip). According to the reporting carrier Southwest, this passenger paid a nominal fare \$267 for this ticket.

#### 3.1.2 DB1B Coupon data

We now consider the Coupon database. A small excerpt from the database (Figure 14) follows. As for the Ticket database, we are particularly interested in the following variables:

- ItineraryID: See Ticket data description above.
- Sequence number and Coupons: For a given ticket, there can be several coupons, which specify the number of separate flights in an itinerary.
- Year and quarter: See Ticket data description above.
- Origin/Destination airport and state: In the Coupon database, we again find the initial airport of departure for the first coupon of an ItinID, which must be the same as the Origin airport for the respective ticket. We can also see all the airports where the passenger landed, and can therefore reconstitute the whole route.
- Break: This variable indicates whether the passenger stopped at a given airport (if the variable is checked "x") for a few hours or days. Thus if there is no break at a given destination

Itinerary ID	Sequence number	Coupons	Year	Quarter	Origin Airport	Origin State	Destination Airport	Destination State	Break	Ticketing carrier	Operating carrier	Reporting carrier	Passengers	Fare Class	Distance
200912901648	1	1	2009	1	FLL	FL	BNA	TN	Х	WN	WN	WN	2.00	G	793.00
200912901649	1	1	2009	1	FLL	FL	BNA	TN	X	WN	WN	WN	6.00	G	793.00
200912901650	1	1	2009	1	FLL	FL	BNA	TN	Х	WN	WN	WN	3.00	G	793.00
200912901651	1	1	2009	1	FLL	FL	BNA	TN	Х	WN	WN	WN	1.00	G	793.00
200912901652	1	1	2009	1	FLL	FL	BNA	TN	X	WN	WN	WN	2.00	G	793.00
200912901653	1	1	2009	1	FLL	FL	BNA	TN	X	WN	WN	WN	3.00	G	793.00
200912901654	1	1	2009	1	FLL	FL	BNA	TN	X	WN	WN	WN	1.00	G	793.00
200912901655	1	1	2009	1	FLL	FL	BNA	TN	Х	WN	WN	WN	1.00	Х	793.00
200912901656	1	2	2009	1	FLL	FL	BNA	TN		WN	WN	WN	1.00	G	793.00
200912901656	2	2	2009	1	BNA	TN	ABQ	NM	X	WN	WN	WN	1.00	G	1123.00
200912901657	1	2	2009	1	FLL	FL	BNA	TN		WN	WN	WN	1.00	G	793.00
200912901657	2	2	2009	1	BNA	TN	BDL	СТ	Х	WN	WN	WN	1.00	G	852.00
200912901658	1	2	2009	1	FLL	FL	BNA	TN		WN	WN	WN	2.00	F	793.00
200912901658	2	2	2009	1	BNA	TN	BHM	AL	X	WN	WN	WN	2.00	F	177.00
200912901659	1	2	2009	1	FLL	FL	BNA	TN		WN	WN	WN	1.00	F	793.00
200912901659	2	2	2009	1	BNA	TN	BHM	AL	х	WN	WN	WN	1.00	F	177.00
200912901660	1	4	2009	1	FLL	FL	BNA	TN	Х	WN	WN	WN	1.00	G	793.00
200912901660	2	4	2009	1	BNA	TN	BHM	AL		WN	WN	WN	1.00	G	177.00
200912901660	3	4	2009	1	BHM	AL	TPA	FL		WN	WN	WN	1.00	G	460.00
200912901660	4	4	2009	1	TPA	FL	FLL	FL	х	WN	WN	WN	1.00	G	197.00
200912901661	1	4	2009	1	FLL	FL	BNA	TN		WN	WN	WN	1.00	G	793.00
200912901661	2	4	2009	1	BNA	TN	BUR	CA	X	WN	WN	WN	1.00	G	1790.00
200912901661	3	4	2009	1	BUR	CA	LAS	NV		WN	WN	WN	1.00	G	223.00

Figure 14: Excerpt from the DB1B Coupon database for 2009Q1. As for the Ticket database, the itinerary fare is nominal, in U.S.\$, and distance is measured in miles. We will later take a closer look at the 3 highlighted itineraries.

airport it means that it is only a short-stop for the passenger.

- Ticketing/Operating/Reporting carrier: The ticketing system can sometimes be very complex, and the carrier which sells a flight is not necessarily the carrier which will operate it, nor will it necessarily be the carrier that reports the ticket to the Bureau of Transportation. Indeed, an itinerary containing several different coupons can be operated and sold by as many different carriers. In order to make our future analysis easier, we chose to retain only the operating carrier.
- **Passengers:** As for the Ticket database, we can see for a given coupon how many passengers bought a similar ticket. As a consequence, there is always a unique number of passengers for a given ItinID, in both databases. As for the Ticket database, this number can be very high, as the DOT prefers to combine similar tickets (same itineraries, same fares, same carriers,...)

in the quarter.

• Fare class: There are 6 different type of fare class defined by the DOT: split into restricted and unrestricted, there are first (unrestricted: code F; restricted: code G), business (respectively codes C and D) or coach class (Y or X) coupons. The DOT stresses that these classes are defined by carriers and can differ from one airline to another. Consequently any analysis of these fare classes should be interpreted with caution. For example, we can observe the distribution of the passengers in 2008 by fare class (Figure 15): a first remark is that this graph represents the fare class by coupons, and not by ticket, so the column axis represents number of passengers multiplied by the number of coupons bought by each passenger. Nevertheless, we can note that the proportion of passengers in the Business fare class only represents 1.13% of all coupons bought in 2008, whereas the coach class tickets represents more than 84% of all these coupons! This statistic shows in fact a characteristic of the U.S. domestic market, where the business fare class is not proposed by carriers as often as it is in Europe. The passenger discrimination is focused between 2 fare classes: the first class and coach class.

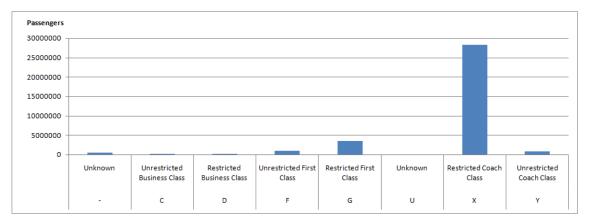


Figure 15: Fare class for coupons purchased in 2008. These fare class are defined by reporting carriers.

• Distance: We also know the length of each flight operated, in miles, which we could

also compute from the exact location of the airports of origin and destination (latitudes, longitudes, giving the great-circle distance).

We selected 3 itineraries to illustrate this database (the 3 ItinId match the 3 examples taken above for the Ticket database). As a consequence, the data contained in the coupons with a specific ItinID should completely match the data for the corresponding ticket (that is indeed the case for the number of coupons in the itinerary, the period of time, the origin airport, the reporting carrier, the number of passengers and the distance). What can we learn from this database for our 3 examples?

- ItinID 200912901650: We learn from this ticket that the 3 passengers taking off from Fort Lauderdale in Florida went with their single flight to Nashville International Airport, in Tennessee, and that they chose to fly in the restricted first class.
- ItinID 200912901658: We also know that these passengers took a similar flight (as for the passengers with the Ticket 200912901650), but instead of staying in Tennessee, their second flight carried them to Birmingham-Shuttlesworth International Airport, in Alabama, 177 miles from Nashville. They flew in the unrestricted first class for the entire itinerary.
- Itin 200912901660: This last passenger also landed at Nashville airport with a similar flight. He stayed there for an unknown period, after which he took his return flight to Fort Lauderdale. This return flight unfolded with three legs, and this passenger landed successively at Birmingham-Shuttlesworth International Airport and at Tampa International Airport (in Florida) before reaching Fort Lauderdale.

To sum up, we can see that we are able to get considerable data about each ticket from the Coupon database. Nevertheless, the likely most important and interesting information about the itinerary, the fare of the ticket, is given only in the database Ticket (because we cannot of course give a fare for each of the coupons bought by the passengers).

#### 3.1.3 Assumptions and inflation data

In order to obtain a reliable sample of data, and to avoid possible erroneous values in the Ticket and Coupon databases, we need to make some additional assumptions:

- **Passengers:** We observed that on some itineraries there were fewer than 90 passengers during a quarter. Given that the database represents 10% of all tickets sold in the U.S., there were less than 900 passengers for some itineraries during a quarter, which is equivalent to 75 passengers per week. There may be some flights operated with these 75 passengers per week; nevertheless, in order to delete what could be erroneous values in the database, we decided to fix 90 passengers as a lower bound.
- Fares: Another possible source of erroneous values in the Coupon and Ticket databases can be the fares. We make 2 additional assumptions:
  - 1. Inflation: The tickets reported by the carriers to the DOT in 1993 have been reported with the value of the dollar in 1993. Nevertheless, one dollar spent in 1993 does not offer the same purchasing power for the U.S. citizens as one dollar spent today. We consequently need to take into account the general rise in the level of prices (i.e. the inflation rate), in order to be able to compare the fare of a ticket bought in 1993 with the fare of a ticket bought in 2009. The usual method used to deal with this problem is the Consumer Price Index (CPI).<sup>11</sup> Below (Figure 16), we can see the monthly U.S. Consumer Price Index between 1993 and 2009 (available on the BLS website), which represents the increase in average prices over time. We note the sudden global decrease of prices in 2008, a clear sign of the recent economic and financial global crisis. We also observe that the Consumer Price Index is remarkably linear over the entire period.

A simple regression (using least squares estimation) gives an estimated coefficient of

<sup>&</sup>lt;sup>11</sup>See the U.S. Bureau of Labor Statistics website for more details on the CPI (http://www.bls.gov/cpi/).

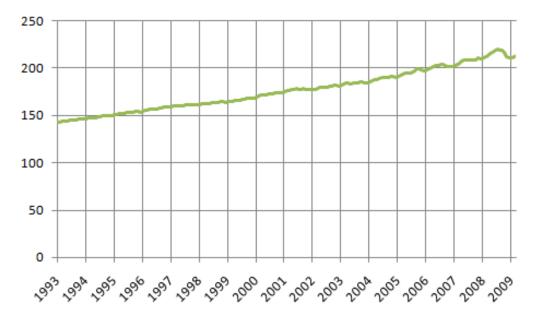


Figure 16: U.S. Consumer Price Index between 1993 and 2009.

1.126, meaning that there is an average increase of 1.126 in CPI per quarter, that is to say an average increase of 45 in the CPI index over 10 years. The econometric software EViews6 gives us a coefficient of  $R^2$  (which represents the "quality" of fit for the regression) of 0.986, which is very high.

From these values, we can compute a "CPI deflator" value for each quarter, which will be a multiplying factor between the fares reported by the carriers in a given quarter and the real fares, taking into account the inflation of the prices between this quarter and today. The last quarter in our database is the first quarter in 2009 (afterwards this period will be written as 2009Q1), and our "original" value of the dollar will be the value for the quarter 2009Q1. The "CPI deflator" for this period (CPIdef(2009Q1)) is set at 1. The CPI deflator for the quarter 2008Q4 (CPIdef(2008Q4)) can be computed as the ratio between the quarterly average CPI of 2009Q1 (CPI(2009Q1)) and the quarterly average CPI of 2008Q4 (CPI(2008Q4)):

$$CPIdef(2008Q4) = CPIdef(2009Q1) \times \frac{CPI(2009Q1)}{CPI(2008Q4)}.$$
 (1)

As a consequence, the CPI deflator for a given quarter t is:

$$CPIdef(t) = CPIdef(t+1) \times \frac{CPI(t+1)}{CPI(t)}.$$
(2)

Below (Figure 17), we see the Consumer Price Index deflators between 1993 and 2009 (dashed line), and the curve of the inflation of the quarterly average CPI (defined as the ratio between successive quarterly average CPI). As the CPI is almost a linear curve, therefore the CPI deflator curve is also approximately linear. On the other hand, the inflation of the quarterly average CPI is highly variable, especially for the past 10 years, reflecting the disturbance of the actual economy. We can note 3 major drops in quarterly inflation after 1993, leading to a quarterly deflation of the U.S. economy: the first one happened during 2001Q4, and is most likely to be a consequence of the September 11 attacks. The second one, which took place during 2006Q4, matches the beginning of the subprime mortgage financial crisis, with the end of the U.S. housing bubble. Finally, the third quarter of U.S. deflation, in 2008Q4, corresponded to the beginning of the current global economic crisis. We can check that the CPI deflator is a decreasing curve, with a minimum of 1 in the first quarter of 2009. The maximum value, 1.48, means as a consequence that we need to multiply all fares reported in the first quarter of 1993 by 1.48 to get the real value of fare which would be sold today (and a value we can therefore compare with the values of fares reported in the first quarter of 2009).

2. Zero-fare award coupons: Many U.S. airlines, and in our case each of the 7 carriers we are interested in, have put in place "frequent flyer programs": AAdvantage for American

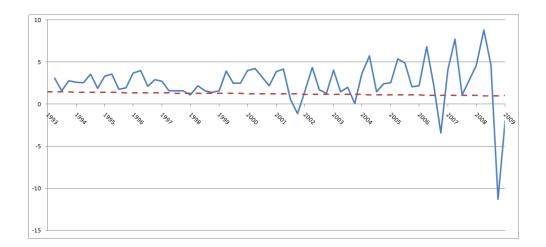


Figure 17: CPI deflators (dashed) and inflation estimates between 1993 and 2009.

Airlines, OnePass for Continental, SkyMiles for Delta and Northwest, Mileage Plus for United, Dividend Miles for US Airways and Rapid Rewards for Southwest. Due to these programs, some passengers can obtain tickets with zero-fare award coupons and pay nothing else but some taxes. Other passengers may also "fly for free": the carrier employees. As we are not able to distinguish them from full-fare passengers in the databases, we must fix a lower bound for the fares in order to be able to correctly assess the real fares. This bound can also enable us to delete some other erroneous values. Which bound should we fix? We need to fix a bound that will not delete true low-fare tickets (offered by Southwest, for instance), but at the same time if this bound is too low, we may probably keep frequent flyer award coupon without any monetary payment but the air transport taxes.

3. Air transport taxes: All U.S. carriers are subject to taxes for each flight operated, most of which are reflected in the passenger's ticket fare. What are the usual taxes paid by the passengers? The current aviation excise tax structure from the Federal Aviation Authorities (FAA) is attached in the Appendix.<sup>12</sup> Nevertheless, the easiest way to find the additional taxes contained in a ticket is to look at the carriers' websites. Searching for the cheapest ticket sold by Southwest (on 29 November 2009) we found the following itinerary (Figure 18), from Kansas City to Milwaukee, at \$59.60. According

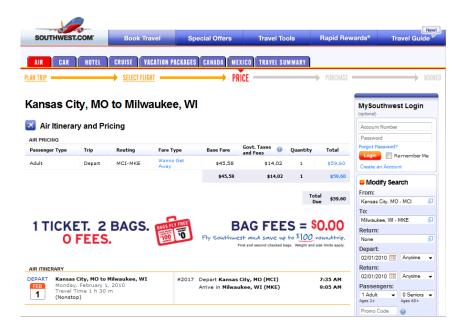


Figure 18: Illustrative Southwest ticket from Kansas City to Milwaukee.

to Southwest, about \$14.02 on the \$59.60 of the ticket are Government Taxes and Fees, made up with 7.5% (of the initial fare) for the Federal Excise Tax, accounting here for \$3.42 (most of time, especially for the 6 other carriers, this tax is included in the initial fare proposed on the first booking screen), plus \$3.60 of Federal segment fee (for each flight segment of the itinerary), plus \$2.5 of "Government-imposed September 11th Security Fee" per segment (up to \$5 for a one-way travel), and finally \$4.5 of "Airport assessed Passenger Facility Charge" (PFC) per landing (up to \$18 for a round trip, but

<sup>&</sup>lt;sup>12</sup>A good report on usual aviation taxes and fees is also available at http://assets.opencrs.com/rpts/RL33913\_ 20080421.pdf [8]

the PFC can be lower than \$4.5 for each segment, depending of the airport of origin on this segment). Checking the websites of the 6 other major carriers of interest, we observe that the additional taxes are the same as for Southwest.

As a consequence, we can assume that the minimal taxes paid for a one-way ticket (between big airports for which the PFC costs \$4.5) are \$10.6. On the other hand, the highest taxes, paid for a round trip with 4 successive segments, are up to \$42.4! It appears difficult to fix a reliable lower bound for fares, without losing some useful data on low-fare travels. In order to try to remove a large number of erroneous values, but without losing too much data, we decided to fix this **lower bound at \$20**.

4. Very high fares: A final source of error can be some high fare values. We saw in the database that some tickets are very expensive, and seem too expensive for domestic travel. As a consequence we decided to fix a higher bound at \$10,000 for the fares.

Once the lower and higher bounds for fares have been fixed, we can check in the database created with these assumptions whether these bounds are correctly fixed. We chose to gather all tickets bought by passengers in the same quarter for a round trip between the same airports and operated by the same carrier. We also create a fare for this round trip, fixed as the passenger-weighted average between all of the fares for this round trip during this quarter.

Do the assumptions for fares hold for this database?

We can see that our assumptions are quite realistic: we observe that the lowest real average fare in this database is \$60, and the highest fare is \$1801 (for round trips to the Island of Guam, in the western Pacific Ocean, i.e. more than 6000 miles from Los Angeles, compared to less than 3000 miles maximum for travel between the Pacific coast and the Atlantic cost of the U.S.!). These limits are easily contained in the interval fixed with the previous assumptions for fares.

### 4 Model construction and estimation

Here (Figure 19) we can see the quarterly average fares for round trips for the 7 carriers we are interested in, followed (Figure 20) by the quarterly number of passengers carried by these airlines for round trips between 1993 and 2009. We observe from these two figures a clear difference between

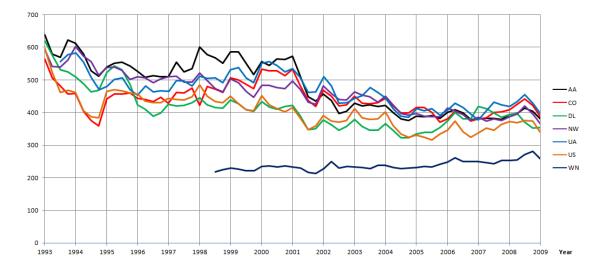


Figure 19: Quarterly average fares for round trips (unit: real 2009 US\$). The data for the airline Southwest in the DB1B database, for round trips, is given by the DOT only from the third quarter of 1998. Before this quarter Southwest did not report round trips.

the low-cost model and the model for state airlines. Indeed, Southwest clearly has the lowest average fares, and is the largest airline in terms of passengers. In this section, we attempt to build rigorous forecasting models for the series displayed in these figures, from the simplest univariate time series models to more complicated regressions including both statistical and economic data.

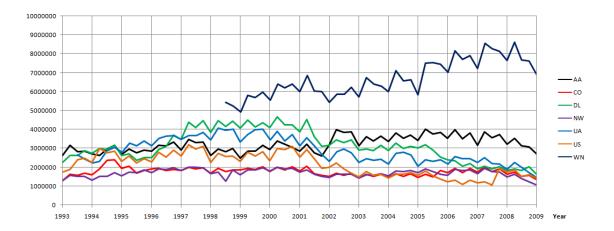


Figure 20: Number of passengers carried per quarter (round trips). As for the fares, data from Southwest is only available from the third quarter of 2008.

#### 4.1 Fares

#### 4.1.1 Simple linear regressions

One of the most straightforward ways to develop a model for the quarterly average fares, between 1993 and 2009, for a given carrier, is by a linear regression:

$$Fare(t) = \alpha_0 + \alpha_1 \times t, \tag{3}$$

where t is time. The limit of the fitted fares will be either  $-\infty$ ,  $+\infty$  or  $\alpha_0$  if  $\alpha_1 = 0$ , which is obviously very restrictive for any analysis and forecasting. In Table 1 we can see the estimated coefficients  $\widehat{\alpha_0}$  and  $\widehat{\alpha_1}$ . First, we can observe that the Student's t-statistics are all greater (in absolute value) than 1.96, which means that we reject at the 95% level of confidence the hypothesis that a coefficient would be individually equal to 0.

It is interesting to see that the trend for all carriers is to decrease their fares, except for Southwest (this is apparent in the sign of the coefficient  $\widehat{\alpha_1}$ , which is positive only for the low-cost carrier).

Carriers	$\mathbf{A}\mathbf{A}$	CO	$\mathbf{DL}$	$\mathbf{NW}$	$\mathbf{U}\mathbf{A}$	$\mathbf{US}$	WN
$\widehat{lpha_0}$	602.86	479.13	493.94	559.32	540.30	476.91	198.28
$\widehat{lpha_1}$	-3.769	-1.144	-2.567	-3.010	-2.123	-2.319	0.919
$\widehat{se}(\widehat{lpha_0})$	9.678	9.761	10.166	4.816	9.241	7.767	5.017
$\widehat{se}(\widehat{lpha_1})$	0.261	0.263	0.274	0.130	0.245	0.209	0.112
$t - stat(\widehat{\alpha_0})$	62.29	49.084	49.586	116.13	58.466	61.399	39.521
$t - stat(\widehat{\alpha_1})$	-14.45	-4.349	-9.365	-23.178	-8.656	-11.076	8.196
$R^2$	0.768	0.231	0.582	0.895	0.551	0.661	0.621

Table 1: The carriers are denoted by their IATA airline codes. " $se(\alpha_i)$ " stands for the standard error of the coefficient  $\alpha_i$ , and " $t - stat(\alpha_i)$ " stands for the Student's t-statistic, which asymptotically follows a standard normal distribution. " $R^2$ " is the coefficient of determination of the regression, which is a measure of the global fit of the model.

Nevertheless, in absolute value, Southwest is the most "stable" carrier in terms of variability of average fares.

Another interesting feature is the coefficient of determination of the regression, which appears to be very high for American Airlines and even moreso for Northwest Airlines. These coefficients can be interpreted as significant evidence for these two carriers to decrease their fares since 1993. It could be related to the difficult financial situation of the two airlines, since we know that Northwest airlines was forced to merge with Delta Airlines in 2008. For American Airlines, we can observe (see Figure 19) that the carrier was the "most expensive" after 2001. Following the successive political and economic crisis since 2001, a strategy to align the fares with the other airlines in a more competitive market may explain (more than the financial situation of the carrier) this decreasing trend for the fares of American Airlines since 1993.

### 4.1.2 ARMA models

Even if the linear model can explain a trend in the fares, it remains a very simple model and does not catch all the variations of fares since 1993. As a consequence, we could try a different approach to model the fare: the autoregressive moving average (ARMA) models. These models are often used for the analysis of statistical data. The main idea is to assume that the fare today will depend on the fares in previous periods (this is the autoregressive part of the model, also called the AR component), and on the shocks in these past fares altering the "average" value of the model (the moving average (MA) component of the model). An ARMA(p,q) model (combining AR(p) and MA(q) terms) can be written as follows:

$$Fare(t) = \alpha_0 + \alpha_1 \times Fare(t-1) + \alpha_2 \times Fare(t-2) + \dots + \alpha_p \times Fare(t-p)$$

$$+\varepsilon(t) + \beta_1 \times \varepsilon(t-1) + \beta_2 \times \varepsilon(t-2) + \dots + \beta_q \times \varepsilon(t-q).$$
(4)

We could imagine that the higher are p and q, the better the model could match reality. Nevertheless, by increasing the number of variables p and q, we decrease the number of available observations for our model and risk "overfitting". Given that our databases only have 65 quarterly observations from 1993 to 2009, we decided to limit p and q to 4, which correspond to one year of information for fares. These 4 past data also allow us to ignore for the moment possible seasonality effects on fares. As a consequence, we obtain for each carrier 25 new models (p and q = 0,1,2,3,4).

We can also assume that the fares of these 7 carriers may also depend on the time period, and that there may be a trend in the fares to decrease or increase over time. In order to model this trend, we can add a variable of time in the regression of the fares. This new variable leads to 50 possible models of regression for the fares.

Moreover, another interesting variable to include in these regressions is a variable that could take into account what we can call a shock for the fares of the carrier (as a sudden and unexpected variation of the fares), caused by a major major external event such as an economic or political crisis, or an event such as the U.S. terrorist attacks of September 11, 2001. For example, looking at the curve of the fares for American Airlines (Figure 21), we can see that there is a visible gap between the average fares before and after the quarter 35, i.e. between July 2001 and September 2001 (included). This gap was the most important decrease of in average fares for American Airlines since 1993 (a drop of more than \$64 between the second and the third quarter of 2001), and was very likely caused by the terrorist attacks in New-York and the 3 days of non-activity imposed by the U.S. government after these events. Consequently, we can assume that we may need to take

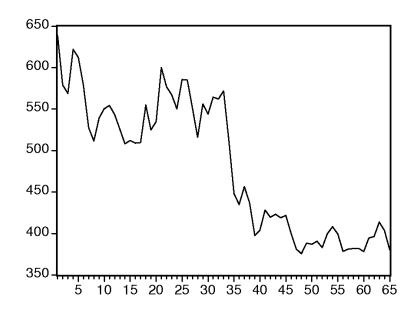


Figure 21: Quarterly average fares for American Airlines (\$ against time).

this shock into account in our model for fares. We chose to try to see the impact of this drop with the insertion of a dummy variable in our regression. How can we choose this dummy variable? In order to observe the change in the regression, we can insert a variable that takes value of 0 before the quarter 35, 0.22 for this quarter and 1 thereafter.<sup>13</sup> This dummy variable DummyD(t) can be

 $<sup>^{13}</sup>$ The coefficient 0.22 was also used by Guzhva and Pagiavlas (2004) [9]. It represents the ratio 20/92 (20 days in the quarter 35 after 9/11 and 92 days total in this quarter).

expressed as follows :

$$DummyD(t) = 0 \text{ for } t < 35; \ 0.22 \text{ for } t = 35; \ 1 \text{ for } t \ge 35.$$
(5)

Thus we obtain 100 possible models for each airline.

# 4.1.3 Selecting the best ARMA model (theory)

So how can we choose the best among all these models? (that is, a reliable statistical and forecasting model which can also provide some interesting insights into the airlines' fare setting behaviour?) Many studies have been written on this subject, and methods have been proposed to find the best possible model for ARMA regressions. The classic approach is the Box-Jenkins methodology.<sup>14</sup> According to this procedure, one of the most important features to consider is the stationarity (stability) of a model. A model is said to be covariance-stationary if the mean, variance and covariance are finite and are invariant with respect to time. We can observe that some of the fares seem to decrease over time, and due to this "trend" we created models including a time variable. This variable can be a solution to "detrend" the regression and make this model trend-stationary. Nevertheless, even if we include a variable of time in the equation, the model can still be nonstationary. We can have a look, for example, at the following model AR(1) :

$$Fare(t) = \alpha_0 + \alpha_1 \times Fare(t-1) + \varepsilon(t).$$
(6)

We can easily infer from this equation that if we know  $Fare(t_0)$ , we get for all  $t \ge t_0$ :

$$\operatorname{Fare}(t) = \alpha_0 \times (1 + \alpha_1) + \alpha_1^2 \times \operatorname{Fare}(t - 2) + \alpha_1 \times \varepsilon(t - 1) + \varepsilon(t), \tag{7}$$

<sup>&</sup>lt;sup>14</sup>See for example http://economics.uwaterloo.ca/2007-Winter/603notes3.pdf for more information about this methodology, and Hamilton (1994) [10].

and so

$$Fare(t) = \alpha_0 \times (1 + \alpha_1 + \alpha_1^2 + \dots + \alpha_1^{t-1}) + \alpha_1^t \times Fare(t_0)$$
$$+ \alpha_1^{t-1} \times \varepsilon(t_0) + \dots + \alpha_1 \times \varepsilon(t-1) + \varepsilon(t)$$
(8)

$$\Rightarrow \operatorname{Fare}(t) = \alpha_0 \times \sum_{i=t_0}^{t-1} (\alpha_1^i) + \alpha_1^t \times \operatorname{Fare}(t_0) + \sum_{i=t_0}^{t-1} (\alpha_1^i \times \varepsilon(t-i)).$$
(9)

What is the expected limiting behavior of  $\operatorname{Fare}(t)$  as  $t \to +\infty$ ? If we assume that  $\varepsilon_t \sim D(0, \sigma^2)$ , then  $\lim_{t\to\infty} E[\sum_{i=t_0}^{t-1} (\alpha_1^i \times \varepsilon(t-i))] = 0$ , where E[.] is the expectation operator, D(.) is some distribution and  $\operatorname{Fare}(t_0) = 0$  is assumed. and we can observe that:

- if  $|\alpha_1| < 1$ :  $\lim_{t\to\infty} E[\operatorname{Fare}(t)] = \frac{\alpha_0}{1-\alpha_1}$
- if  $|\alpha_1| = 1$ :  $\lim_{t\to\infty} \operatorname{Fare}(t) = \infty$  if  $\alpha_0 \neq 0$ ,  $\lim_{t\to\infty} \operatorname{Fare}(t) = 0$  if  $\alpha_0 = 0$
- if  $|\alpha_1| > 1$ :  $\lim_{t\to\infty} \operatorname{Fare}(t) = \infty$ ,

and so the AR(1) model is not explosive if and only if  $|\alpha_1| < 1$ . In fact, we can find a general rule for all ARMA models, which determines a condition in the  $\alpha$  terms to get a finite limit for a model and because of that the stationarity (stability) of this model. To establish this condition, we need to rewrite the ARMA(p,q) models as:

$$Fare(t) = \alpha_0 + \alpha_1 \times Fare(t-1) + \alpha_2 \times Fare(t-2) + \dots + \alpha_p \times Fare(t-p) + \beta_1 \times \varepsilon(t-1) + \beta_2 \times \varepsilon(t-2) + \dots + \beta_q \times \varepsilon(t-q).$$
(10)

Let  $L^i$  be the lag operator, which transforms Fare(t) into Fare(t-i). Then we can write the model ARMA(p,q) as follows:

$$\operatorname{Fare}(t) = \sum_{i=0}^{p} (\alpha_i \times \mathbf{L}^p) \times \operatorname{Fare}(t) + \sum_{i=1}^{q} (\beta_i \times \mathbf{L}^q) \times \varepsilon(t)$$
(11)

or

$$(1 - \sum_{i=1}^{p} (\alpha_i \times \mathbf{L}^p)) \times \operatorname{Fare}(t) = \alpha_0 + \sum_{i=1}^{q} (\beta_i \times \mathbf{L}^q) \times \varepsilon(t),$$
(12)

and if we denote

$$A(L) := 1 - \sum_{i=1}^{p} (\alpha_i \times L^p)$$
(13)

$$B(L) := \sum_{i=1}^{q} (\beta_i \times L^q) \tag{14}$$

then

$$A(L) \times \text{Fare}(t) = \alpha_0 + B(L) \times \varepsilon(t).$$
(15)

The stability condition for the ARMA(p,q) model is the following: under the assumption that  $\varepsilon(t) \sim D(0, \sigma^2)$  (meaning that  $\varepsilon$  follows an independent, identically distributed, or White Noise distribution), a model is stationary if all the roots of the real polynomial  $\alpha_Z = 1 - \sum_{i=1}^{p} (\alpha_i \times Z^p)$  are greater than 1 in absolute value (or in norm for complex roots).

If this stability condition holds, then we can invert the polynomial  $\alpha_Z$  (which can be done thanks to the convolution formula), and in the same way we get the inverse of the polynomial A(L),  $A(L)^{-1}$ , and thus we can "solve" the equation Fare(t):

$$Fare(t) = \alpha_0 \times A(L)^{-1} + A(L)^{-1} \times B(L) \times \varepsilon(t).$$
(16)

As  $\alpha_0$  is a constant, in fact we can prove that  $\alpha_0 \times A(L)^{-1} = \alpha_0 \times A(1)^{-1}$ , so the limit of the fares is:

$$\lim_{t \to \infty} \operatorname{Fare}(t) = \alpha_0 \times A(1)^{-1}.$$
(17)

The model is therefore stationary, as we know that the limit of the fares is finite.

EViews6 can provide us with the "inverted" roots of the AR polynomial A(L), in the estimation output of an ARMA model. These roots are in fact the inverted roots of the polynomial  $\alpha_Z$ . Indeed, we can prove that the stability conditions is equivalent to having these inverted roots lower in absolute value (or in norm) than 1. So we can check, for each model, whether the stability condition holds. However, we can observe that in some cases the roots are below (but very close to) 1. This proximity to the limit value of stability can be a problem as it makes it very difficult to find  $A(L)^{-1}$ , and such values can be a sign that the model is not as stable as we would wish. Some tests can allow us to solve this problem and determine a critical value under which we may expect to have stationarity with a certain amount of confidence. One of the tests we can perform with EViews6 is the Augmented Dickey-Fuller (ADF) test, which checks whether a unit root is present or not in the model. The ADF test uses the following regression, with the difference operator notation  $\Delta Fare(t - p) := Fare(t - p) - Fare(t - p - 1)$ :

$$\Delta \operatorname{Fare}(t) = \alpha_0 \times \operatorname{Fare}(t-1) + \alpha_1 \times \Delta \operatorname{Fare}(t-1) + \alpha_2 \times \Delta \operatorname{Fare}(t-2) + \dots + \alpha_p \times \Delta \operatorname{Fare}(t-p) + \varepsilon(t)$$
(18)

We can add to this equation a constant term, and a time trend, to check the stationarity of these models too. Then what we want to test is whether  $\alpha_0 = 0$ . The other  $\Delta \text{Fare}(t - i)$  terms behind are used to avoid possible autocorrelation effects of the residuals in the regression. This regression allow us to compute the t-statistic for the coefficient  $\alpha_0$ . Then we reject the hypothesis of the null for this coefficient (and so we reject the nonstationarity hypothesis for the model) if this computed t-statistic is greater than the critical value at a certain level of confidence.

If we find, thanks to the ADF test, that a model is still nonstationary, then there is a common tool used in econometrics, which is to apply an initial differencing step to the model, and to transform the ARMA model into an autoregressive integrated moving average (ARIMA) model. In this ARIMA model we consequently do not estimate Fare(t) but  $\Delta Fare(t - 1)$ , which may "stationarize" the regression.<sup>15</sup> We may need to difference the data several times (using  $\Delta \text{Fare}(t-2)$  or  $\Delta \text{Fare}(t-3)$  as the dependent variable for the regression) to get stationarity, but this method can sometimes create additional problems if the differencing is taken "too far", and so we will try to stay at the first-order of differencing. We can also evaluate, with the Dickey-Fuller test, whether the ARIMA models have unit roots or not, and thus we can check the stationarity of these models too.

Once we obtain a stationary model, we also need to perform other tests on the regression output to select the best one. We first need to check that all the coefficients of the regression are significant (considering the Student's t-statistics of all coefficients). Then we need to check that the residuals have nice distributional properties (checking that they follow a White Noise distribution), and that they are not autocorrelated (the Durbin-Watson statistic must be close to 2).<sup>16</sup> The autocorrelation of the residuals can also be checked using the correlograms and the Ljung-Box Q-statistic. Indeed, we can observe on the correlograms the (partial) autocorrelation functions of the residuals, which represent the dependence between a value of the fares at the time period t (Fare(t)), and the value of these fares s periods before t (Fare(t - s)). If the value of this dependence is too high, it means that there is a strong dependence between the fares at these two periods of time, and therefore our model may have missed an important correlation in the regression. Thus we need to check whether there is a spike in the correlograms, and if such a spike exists what is the probability of dependence between the two fares (thanks to the Q-statistic).

Finally, how can we choose, among these good models, the best one? The Schwarz Information Criterion (SIC) can be a solution to select the model which best fits the model. The SIC is asymptotically consistent for ARMA(p,q) models, i.e. given a "large enough" sample and a set of p and q that includes the true p,q, the SIC will select the correct lag-order. The criterion is given

<sup>&</sup>lt;sup>15</sup>See http://www.duke.edu/~rnau/411arim.htm#les for details.

<sup>&</sup>lt;sup>16</sup>See http://en.wikipedia.org/wiki/Durbin-Watson\_statistic for further information on the Durbin-Watson statistic.

by

$$SIC = \frac{-2 * \ln L}{T} + \frac{k * \ln T}{T},$$
(19)

where L is the maximized log-likelihood (estimated), T is the effective sample size, and k is the number of estimated parameters. The best ARMA model is chosen by minimizing the SIC across various ARMA(p,q) models, e.g. p, q = 0, 1, 2, 3, 4.

# 4.1.4 Application of ARMA models to 7 U.S. carriers

If we run a first series of regressions for the seven carriers, and keep the best model among these regressions according the Schwarz Information Criterion, we get the following results:

• American: The best ARMA model for American Airlines seems to be an ARMA(3,0), that is to say an AR(3). It would mean that the best ARMA regression for the airline would be:

$$\operatorname{Fare}(t) = \alpha_0 + \alpha_1 \times \operatorname{Fare}(t-1) + \alpha_2 \times \operatorname{Fare}(t-2) + \alpha_3 \times \operatorname{Fare}(t-3) + \varepsilon(t).$$
(20)

The Student's t-statistics for the coefficients of the regression are greater (in absolute value) than 1.96, so they are individually significant. The coefficient  $R^2$  is equal to 0.918, which is very high. The Durbin-Watson statistic is equal to 2.015, close to 2, meaning that the residuals of the regression do not appear to be autocorrelated. The Jarque Bera statistic is quite low (1.390), so we can assume that these residuals are approximately normally distributed.

However, the very high coefficient of determination  $R^2$  is a sign that there may be a problem hidden behind these apparently good results. Looking at the inverse roots of the AR polynomial, we see that one root is equal to 0.968, which is very close to 1. There may consequently be a problem of nonstationarity for this model (the model is unstable). This hypothesis is confirmed by the unit root test.

Thus, we can try to difference this equation to remove this nonstationarity: the ARMA model

ARMA(3,0) with first-order differencing leads to an ARIMA(3,1,0):

$$\operatorname{Fare}(t) - \operatorname{Fare}(t-1) = \alpha_0 + \alpha_1 \times (\operatorname{Fare}(t-1) - \operatorname{Fare}(t-2))$$

$$+ \alpha_2 \times (\operatorname{Fare}(t-2) - \operatorname{Fare}(t-3)) + \alpha_3 \times (\operatorname{Fare}(t-3) - \operatorname{Fare}(t-4)) + \varepsilon(t).$$
(21)

In order to get the best differenced models for our regressions, we consequently keep the ARIMA model minimizing the Schwarz criterion.

For American Airlines, the result of this differencing appears to be the ARIMA(2,1,0) model (i.e. ARMA(2,0) with first-order differencing). Nevertheless, we can observe that, even though the inverted roots of the AR polynomials are here far from 1 in absolute value, the other statistics are worsened by the differencing. The  $R^2$  coefficient is only equal to 0.11 (meaning that the model would explain roughly 11% of the data for fares), and, for one coefficient, we do not reject at the 95% level of confidence the hypothesis that it is equal to 0. These results tend to say we may have missed an important characteristic in our model for this airline.

We can first try to see if there is a change in the trend of the airline for its average fares after September 11, 2001. We run the following regression:

$$Fare(t) = \alpha_0 + \alpha_1 \times D(t) + \alpha_2 \times t + \alpha_3 \times D(t) \times t + \varepsilon(t).$$
(22)

From the results of this regression (Figure 22), we can see that the intercept dummy variable appears to be very important and reveals a drop of about \$100 in the average fares for the airline during the September 11 attacks. We can also observe that there is a trend in the fares (we reject the hypothesis of the null for the time trend variable), but this trend does not seem to change after 2001, as the variation of this coefficient is very low (\$0.37, with a standard error of 0.75, hence we do not reject the null hypothesis for this coefficient at the

Dependent Variable: FARE1 Method: Least Squares Date: 12/30/09 Time: 17:24 Sample: 1 65 Included observations: 65					
Variable	Coefficient	Std. Error	t-Statistic	Prob.	
C	569.8331	9.291963	61.32537	0.0000	
DUMMY	-99.50148	30.86451	-3.223815	0.0020	
@TREND	-1.023797	0.475261	-2.154177	0.0352	
@TREND*DUMMY	-0.372762	0.749828	-0.497130	0.6209	
R-squared	0.887526	Mean dependent var		482.2520	
Adjusted R-squared	0.881995	S.D. dependent var		81.31382	
S.E. of regression	27.93281	Akaike info criterion		9.557045	
Sum squared resid	47594.76	Schwarz criterion		9.690853	
Log likelihood	-306.6040	F-statistic		160.4499	
Durbin-Watson stat	0.904774	Prob(F-statistic)		0.000000	

95% level of confidence). So maybe we could include this dummy variable, with a trend, in a

Figure 22: American Airlines - regression on quarterly average fares: @trend stands for the regression of the results over time, and dummy stands for the dummy variable previously presented.

ARMA model, and get the best ARMA model according to the Schwarz criterion. Here is the result of this new regression: EViews6 indicates that the best model with these requirements is an ARMA(0,2) (Figure 23), which can be written:

$$\operatorname{Fare}(t) = \alpha_0 + \alpha_1 \times t + \alpha_2 \times \mathrm{D}(t) + \varepsilon(t) + \beta_1 \times \varepsilon(t-1) + \beta_2 \times \varepsilon(t-2).$$
(23)

Indeed we can see that this model is much better than the previous ones: all coefficients are individually significant, and jointly significant (the F-statistic is very high). The inverted MA roots are lower than 1 in absolute value, so the model is invertible, and also stationary (confirmed by the unit root test). The Jarque-Bera statistic is equal to 6.68 (not present in the Figure), so we reject the normality of the residuals. The Durbin-Watson statistic is equal to 2.176 so there is no autocorrelation either in these residuals, and there are no significant spikes in the autocorrelation function (ACF) or the partial autocorrelation function (PACF), so the residuals of this regression are similar to White Noise, and there seem to be no other significant patterns left in the data. To sum up, we can notice that the quarterly average

> Dependent Variable: FARE1 Method: Least Squares Date: 12/30/09 Time: 16:44 Sample: 1.65 Included observations: 65 Convergence achieved after 11 iterations Backcast: -1.0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C @TREND DUMMY MA(1) MA(2)	574.6830 -1.640269 -88.83975 0.882115 0.385701	13.56196 0.589527 21.54177 0.095828 0.093419	42.37462 -2.782348 -4.124070 9.205166 4.128723	0.0000 0.00 <b>72</b> 0.0001 0.0000 0.0001
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.934305 0.929926 21.52502 27799.59 -289.1287 2.176079	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		482.2520 81.31382 9.050112 9.217373 213.3293 0.000000
Inverted MA Roots	4444i	44+.44i		

Figure 23: American Airlines - final regression on quarterly average fares.

fares for American Airlines (for round trips) fell substantially after the September 11 terrorist attacks, by about \$90 on average. There is also a trend for these fares to decrease over time, by about \$1.64 per quarter.

**Remark**: these regressions were executed with a lower bound in the database. Indeed, we decided to keep only the flights with more than 90 passengers. Nevertheless, we observe that the results are the same if we consider the non-filtered data, and the model ARMA(0,2), with a dummy variable and a trend in the fares, remains the best model for this carrier. We can also observe that the Schwarz criterion is lower for the non-filtered data, so the use of this bound may not be that relevant for American Airlines. Thus we choose to work with the regression output of the non-filtered data (Figure 24).

Convergence achieved after 12 iterations Backcast: -1 0					
Variable	Coefficient	Std. Error	t-Statistic	Prob.	
C DUMMY @TREND MA(1) MA(2)	580.3625 -87.85106 -1.650983 0.860514 0.370623	13.18745 21.04902 0.574834 0.094353 0.092009	44.00870 -4.173642 -2.872104 9.120151 4.028100	0.0000 0.0001 0.0056 0.0000 0.0002	
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.934410 0.930037 21.28624 27186.24 -288.4036 2.220186	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		488.0287 80.47577 9.027802 9.195063 213.6928 0.000000	
Inverted MA Roots	43+.43i	4343i			

Dependent Variable: FARE1 Method: Least Squares Date: 01/08/10 Time: 16:38

Included observations: 65

Sample: 1.65

Figure 24: American Airlines - final regression on quarterly average fares (non filtered data).

• Continental: We apply the same methodology as for American Airlines: the same initial process used for the quarterly average fares for Continental leads to the ARMA model ARMA(1,0), as the best ARMA model we can get according to the Schwarz criterion (see Figure 25). This model seems to be quite good, as the AR root is equal to 0.77, so the model is stationary. All the coefficients are individually significant, and jointly significant according to the F-statistic. Nevertheless, we can observe that the coefficient of determination is quite low ( $R^2 = 0.66$ ), and more importantly, the Durbin-Watson statistic is also quite low (1.83), which could mean that there is a positive autocorrelation in the residuals. This is confirmed by the correlograms of the regression, in which we can see a spike of autocorrelation in the PACF function for the fourth lag (see Figure 26). As a consequence, we may need to reconsider our regression. This autocorrelation may be caused by a seasonality in the average fares of Continental, but it could also be caused by a shock to the fares.

Convergence achieved after 3 iterations					
Variable	Coefficient	Std. Error	t-Statistic	Prob.	
C AR(1)	434.2499 0. <b>7</b> 56818	12.84776 0.073189	33. <b>7</b> 9967 10.34066	0.0000 0.0000	
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.632982 0.627063 24.11026 36040.89 -293.4849 1.847370	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		442.7685 39.48063 9.233903 9.301369 106.9292 0.000000	
Inverted AR Roots	.76				

Dependent Variable: FARE2 Method: Least Squares Date: 01/18/10 Time: 16:36 Sample (adjusted): 2 65

Included observations: 64 after adjustments

Figure 25: Continental Airlines - regression on quarterly average fares.

Indeed, if we look at the figure of the fares (Figure 27), we observe 2 major breaks in the fares, a sudden drop in the fares between the periods 5 and 8 (from the second quarter of 1994 to the first quarter of 1995), and a second one in period 35. This first drop is probably related to the period of troubles faced by the carrier in 1994 and the fact that Continental was only just emerging from bankruptcy that year. In the same period, we can observe a major increase in the number of passengers carried by the airline (Figure 52), so the drop in fares may be part of the strategy of the airline at the time. It could consequently be a mistake to consider that this drop in fares is caused by an event independent from the airline (as the terrorist attacks of 2001). The second drop happened during the terrorist attacks in 2001, so we could try to include a dummy variable in our regression as we did for American Airlines.

In fact, it turns out that if we include the same dummy variable used for American Airlines, we get a totally different model, a ARMA(0,2) with a dummy variable (see Figure 29). We

Date: 01/18/10 Time: 16:48 Sample: 2.65 Included observations: 64 Q-statistic probabilities adjusted for 1 ARMA term(s)

\_

Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
Autocorrelation	Partial Correlation	1 0.044 2 -0.076 3 -0.099 4 0.350 5 0.005 6 -0.005 7 0.108 8 0.148 9 0.044 10 -0.124 11 0.104 12 -0.037	0.044 -0.078 -0.093 0.358 -0.057 0.037 0.206 -0.011 0.084 -0.112 0.052 -0.117	0.1271 0.5160 1.1963 9.8149 9.8167 9.8189 10.684 12.327 12.476 13.681 14.542 14.654	0.473 0.550 0.020 0.044 0.081 0.099 0.090 0.131 0.134 0.150 0.199
		13 0.142 14 -0.099 15 0.072 16 -0.074 17 -0.022 18 -0.090 19 -0.012	0.117 -0.068 -0.009 -0.137 -0.012 -0.063 -0.008 -0.011	14.654 16.317 17.146 17.589 18.075 18.117 18.861 18.874 18.877 19.092 19.541 20.812 21.085	0.199 0.177 0.193 0.226 0.259 0.317 0.400 0.465 0.516 0.550 0.532 0.576
		24 -0.051 25 -0.104 26 -0.048 27 -0.046 28 0.145	-0.020	21.085 22.250 22.511 22.749 25.219	0.576 0.564 0.606 0.647 0.562

Figure 26: Continental Airlines - residual correlograms of the regression in Figure 25.

can observe that the model is better according to the Schwarz Information Criterion (lower for this second regression). The  $R^2$  is also higher than for the first regression. All the coefficients are still significant, the model is stationary, and the Durbin-Watson statistic exceeds 2, which could mean that there is negative autocorrelation in the residuals. Checking the correlograms (Figure 30), we observe that there is no remaining autocorrelation in the residuals at the 95% level of confidence. We can observe that including a trend in this model does not improve the fit. The t-statistic for this trend (the trend coefficient being equal to 0.45 according to

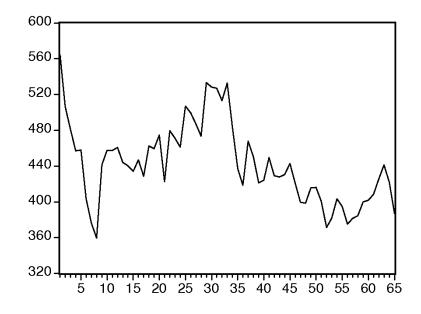


Figure 27: Quarterly average fares for Continental Airlines (\$ against time).

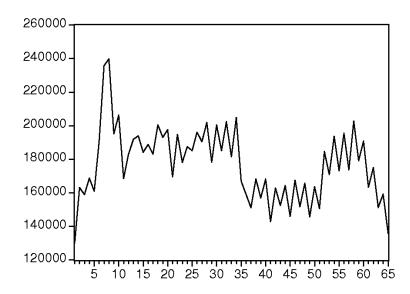


Figure 28: Number of passengers carried by Continental Airlines per quarter.

Dependent Variable: FARE2 Method: Least Squares Date: 01/18/10 Time: 16:59 Sample (adjusted): 1 65 Included observations: 65 after adjustments Convergence achieved after 10 iterations Backcast: -1 0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	466.3134	9.208430	50.63983	0.0000
DUMMY	-51.89094	12.92411	-4.015049	0.0002
MA(1)	0.926233	0.076501	12.10751	0.0000
MA(2)	0.548353	0.083744	6.547973	0.0000
R-squared	0.734066	Mean dependent var		444.5904
Adjusted R-squared	0.720987	S.D. dependent var		41.83435
S.E. of regression	22.09761	Akaike info criterion		9.088380
Sum squared resid	29786.57	Schwarz criterion		9.222188
Log likelihood	-291.3723	F-statistic		56.12665
Durbin-Watson stat	2.202367	Prob(F-statistic)		0.000000
Inverted MA Roots	46+.58i	4658i		

Figure 29: Continental Airlines - regression on quarterly average fares.

EViews6) is equal to 0.66, so we do not reject the hypothesis that this coefficient is null at the 95% level of confidence.

Moreover, if we use the non-filtered data (without the lower bound for the flights with more than 90 passengers), we observe that the best ARMA model is also the ARMA(0,2) model with a dummy variable. The coefficient of determination  $R^2$  is equal to 0.73, all the coefficients are individually significant, and the model is stationary. The Durbin-Watson statistic is also higher than 2. Moreover the SIC criterion is lower for this regression than for the regression with the filtered data, and so we can infer that this model better fits the data.

In order to improve our model, we could then try to catch possible seasonality in the fares as seen in the first regression (with autocorrelation at the fourth lag) for the model ARMA(1,0). If we include an autoregressive term of order 4 in our regression, which would "capture" the autocorrelation of the fourth lag, we can see that this solution does not improve the model.

Date: 01/18/10 Time: 17:03 Sample: 1.65 Included observations: 65 Q-statistic probabilities adjusted for 2 ARMA term(s)

\_

Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
		1 -0.111	-0.111	0.8360	
		2 0.022 3 0.066	0.010	0.8697	0.070
		4 0.249	0.0 <b>7</b> 0 0. <b>2</b> 69	1.1720	0. <b>27</b> 9 0.061
		5 -0.050	0.209	5.7907	0.122
		6 0.041	0.022	5.9135	0.206
		7 0.156	0.134	7.7483	0.171
		8 0.101	0.083	8.5337	0.202
		9 0.039	0.072	8.6493	0.279
ı 🖬 🗉		10 -0.105	-0.147	9,5249	0.300
ı 🗖 i	i 🛛 i	11 0.154	0.041	11.426	0.248
1		12 -0.176	-0.223	13.960	0.175
ı 💷 i	I I 🗖 I	13 0.162	0.119	16.160	0.135
1 🗖 1		14 -0.119	-0.093	17.370	0.136
1 1 1		15 -0.015	-0.108	17.389	0.182
I 🗖 I	I [] I	16 -0.083	-0.049	17.998	0.207
1 <b>[</b> 1	ı <b>⊑</b> ı	17 -0.036	-0.120	18.113	0.257
I 🗖 I	1 1 1	18 -0.085	-0.020	18.782	0.280
1 <b>I</b> 1		19 -0.040	-0.002	18.937	0.332
1 🛛 1	1 1 1	20 -0.046	-0.028	19.140	0.383
I 🗖 I	I [] I	21 -0.097	-0.037	20.075	0.390
· 🛛 ·	I I I I	22 -0.047	-0.062	20.298	0. <b>43</b> 9
· 🗖 ·		23 -0.143	-0.030	22.433	0.375
1 <b>[</b> 1		24 -0.031	-0.074	22.533	0.428
· 🗖 ·		25 -0.100	0.025	23.631	0.424
I I I		26 -0.033	-0.050	23.750	0.476
	I    I	27 -0.014	0.068	23.772	0.533
i 🛛 i	ı 🗖 ı	28 0.075	0.168	24.440	0.551

Figure 30: Continental Airlines - residual correlograms of the regression in Figure 29.

We get the model ARMA(0,2) with a AR(4) term and our dummy variable (Figure 31), which can be written:

$$\operatorname{Fare}(t) = \alpha_0 + \alpha_1 \times \operatorname{Dummy}(t) + \alpha_2 \times \operatorname{Fare}(t-4) + \varepsilon + \beta_1 \times \varepsilon(t-1) + \beta_2 \times \varepsilon(t-2).$$
(24)

There is no problem of autocorrelation for this model. The coefficient for the fourth lag is significant at the 97% level of confidence. All the other coefficients also remain individually significant. The coefficient of determination  $R^2$  for this regression is equal to 0.71. It was

Dependent Variable: FARE2 Method: Least Squares Date: 01/10/10 Time: 15:13 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 10 iterations Backcast: 3 4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	463.1689	12.28482	37.70254	0.0000
DUMMY	-49.20115	15.49425	-3.175446	0.0024
AR(4)	0.314990	0.132395	2.379172	0.0208
MA(1)	0.799716	0.125517	6.371387	0.0000
MA(2)	0.431340	0.123622	3.489191	0.0010
R-squared	0.712162	Mean dependent var		440.5456
Adjusted R-squared	0.691602	S.D. dependent var		39.03847
S.E. of regression	21.67947	Akaike info criterion		9.069021
Sum squared resid	26319.97	Schwarz criterion		9.242043
Log likelihood	-271.6051	F-statistic		34.63844
Durbin-Watson stat	1.956453	Prob(F-statistic)		0.000000
Inverted AR Roots Inverted MA Roots	.75 40+.52i	.00+. <b>7</b> 5i 4052i	00 <b>7</b> 5i	75

Figure 31: Continental Airlines - regression on quarterly average fares.

about 0.73 for the previous regression, so we do not lose much significance with this new model, but as for the filtered data, the SIC criterion is higher with this additional term than for the model in Figure 29, so we decide to keep the previous model (ARMA(0,2)) with a dummy variable).

• Delta: For Delta Airlines, the same methodology leads to an ARMA(3,2) model with a trend variable for the filtered data (see Figure 32), and the model ARMA(4,3) for the whole database. Nevertheless, these models are very complex, and show possible problems of non-stationarity in the AR roots (very close to 1), even if all the coefficients are significant. If we include a dummy variable in the regression, to catch possible external effects from the September 11, 2001, we observe that the model looks simpler, as we obtain a ARMA(0,3) with a dummy variable. All the coefficients remain significant, the  $R^2$  statistic is higher than

Dependent Variable: FARE3 Method: Least Squares Date: 01/18/10 Time: 17:35 Sample (adjusted): 4 65 Included observations: 62 after adjustments Convergence achieved after 11 iterations Backcast: 2 3

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	379.8326	26.79139	14.17741	0.0000
AR(1)	0.836018	0.107980	7.742305	0.0000
AR(2)	-0.811370	0.131557	-6.167449	0.0000
AR(3)	0.769838	0.099230	7.758092	0.0000
MA(1)	0.426887	0.109506	3.898309	0.0003
MA(2)	0.849721	0.097860	8.683040	0.0003
R-squared	0.905418	Mean dependent var		403.8854
Adjusted R-squared	0.896973	S.D. dependent var		52.89033
S.E. of regression	16.97665	Akaike info criterion		8.593320
Sum squared resid	16139.57	Schwarz criterion		8.799172
Log likelihood	-260.3929	F-statistic		107.2155
Durbin-Watson stat	1.898956	Prob(F-statistic)		0.000000
Inverted AR Roots Inverted MA Roots	.89 21+.90i	03+.93i 2190i	0393i	

Figure 32: Delta Airlines - regression on quarterly average fares.

for the first regression, but the SIC criterion has been increased. Looking at the fares, we can observe that including a dummy variable in the regression at period 35 seems to be a good idea as we can observe a drop in the fares at this period (Figure 33). However, could this drop reflect a more global decreasing trend in the fares of the airline? In fact we can observe that, if we include a trend in our model, we get quite a good model with a low SIC criterion, for the filtered data. For the whole database, this variable seems to add complexity to the model rather than improving it (we get a ARMA(4,1) model, with autocorrelation problems). For the filtered data, we get a ARMA(1,1) with the trend variable (see Figure 34). 34). This model is stationary, and all the coefficients seem to be significant in the regression (looking at the Student's t-statistics). The trend coefficient is equal to -1.83. The coefficient of determination for this regression is equal to 0.91, and the SIC is equal to 8.83,

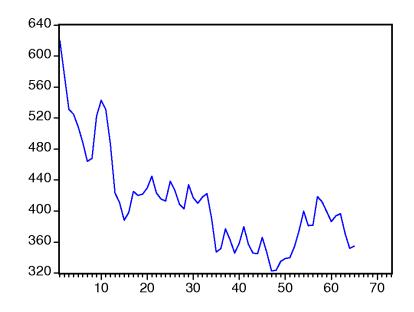


Figure 33: Quarterly average fares for Delta Airlines (\$ against time).

which is a little higher than for the first models for the airline, but much lower than with a dummy variable in the regression.

• Northwest: Looking at the graph of the quarterly fares for Northwest Airlines (Figure 35), a clear trend appears as the fares seem to continuously decrease over the 15 last years. This trend may also explain the recent merger between Northwest and Delta (completed in 2008), as Northwest airlines has tried to reduce its costs and expenses since 2001. Indeed, we can observe that the establishment of a statistical model for the fares of the airline is rather complicated without a coefficient of trend, for the filtered data (we get the model ARMA(3,1) or non-filtered data (we get the model ARMA(2,3)). Moreover these models show problems of stationarity and autocorrelation. When we include a trend in the model, we get a better model for these fares. The non-filtered data and the filtered data give us an ARMA(4,3) model. This model has a coefficient of determination  $R^2$  equal to 0.95 (0.96 without the

Dependent Variable: FARE3 Method: Least Squares Date: 01/10/10 Time: 11:19 Sample (adjusted): 2 65 Included observations: 64 after adjustments Convergence achieved after 8 iterations Backcast: 1

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	462.6359	26.48296	17.46919	0.0000
@TREND	-1.826865	0.656994	-2.780643	0.00 <b>72</b>
AR(1)	0.705859	0.085449	8.260588	0.0000
MA(1)	0.493513	0.122755	4.020321	0.000 <b>2</b>
R-squared	0.907808	Mean dependent var		408.5544
Adjusted R-squared	0.903198	S.D. dependent var		58.40192
S.E. of regression	18.17056	Akaike info criterion		8.697943
Sum squared resid	19810.14	Schwarz criterion		8.832874
Log likelihood	-274.3342	F-statistic		196.9387
Durbin-Watson stat	1.983053	Prob(F-statistic)		0.000000
Inverted AR Roots	.71			

Inverted MA Roots -.49

Figure 34: Delta Airlines - regression on quarterly average fares.

filter). There is no stationarity problem according to the unit root test, and the residuals are not correlated. Looking at the Schwarz criterion, we can observe that this statistic is lower for the non-filtered data, so we decide to keep this model (Figure 36). If we include a dummy variable in the regression, we can observe that the autocorrelation problems remain in the regression (we get the model ARMA(0,2)).

• United: For United Airlines (real fares in Figure 37), we find with the same methods used before that the model ARMA(0,2) with a dummy variable (to take into account a drop of the fares at the period 35) seems to be the best for this carrier (Figure 38) for the filtered data. The model is stable, the coefficients are all individually significant, and the correlograms of the regression do not show any spikes in the autocorrelation coefficients, so this model seems to be quite a good one. The coefficient of determination of the regression is equal

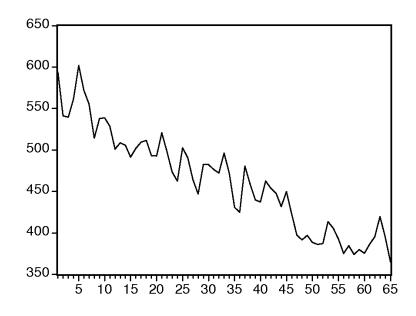


Figure 35: Quarterly average fares for Northwest Airlines (\$ against time).

to 0.85, which is quite high. The dummy variable is significant in the model ARMA(0,2), and reveals a drop of about \$78 in the fares at the time of the U.S. terrorist attacks. For the non-filtered data, EViews6 gives the model ARMA(1,2) with our dummy variable as the best model. This model is also stationary, and seems to be a good one. Nevertheless, the Schwarz criterion is higher for this regression than for the filtered data. Thus we can keep the filtered model for our analysis. If we do not include a dummy variable in the regression, the best model (according to the Schwarz Information Criterion) appears to be ARMA(3,2) for the filtered data, and ARMA(3,0) without the filter. These models appears to be good models too, but the use of a dummy variable decreases the SIC criterion. The use of a trend also could improve the model, but it leads to problems of autocorrelation with a quite low Durbin-Watson statistic.

• US Airways: For US Airways (real fares in figure 39), the same methods lead to the model ARMA(0,2) with a trend for the filtered data. This model seems to be stable, with nice t-

Dependent Variable: FARE4 Method: Least Squares Date: 01/08/10 Time: 16:38 Sample (adjusted): 5.65 Included observations: 61 after adjustments Convergence achieved after 76 iterations Backcast: 2.4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	556.4219	8.218436	67.70410	0.0000
@TREND	-2.865983	0.210066	-13.64325	0.0000
AR(1)	-0.494535	0.144094	-3.432030	0.0012
AR(2)	-0.395445	0.131545	-3.006146	0.00 <b>41</b>
AR(3)	-0.393415	0.124337	-3.164100	0.0026
AR(4)	0.469012	0.133880	3.503215	0.0010
MA(1)	1.427952	0.105101	13.58651	0.0000
MA(2)	1.273337	0.148822	8.556115	0.0000
MA(3)	0.813511	0.081167	10.02267	0.0000
R-squared	0.961141	Mean deper	ndent var	459.6851
Adjusted R-squared	0.955163	S.D. depend	dent var	55.37599
S.E. of regression	11.72578	Akaike info	criterion	7.896909
Sum squared resid	7149.684	Schwarz crit	terion	8.208349
Log li <b>ke</b> lihood	-231.8557	F-statistic		160.7710
Durbin-Watson stat	1.887232	Prob(F-stati	0.000000	
Inverted AR Roots Inverted MA Roots	.53 23+.88i	0295i 2388i	02+.95i 98	99

Figure 36: Northwest Airlines - regression on quarterly average fares.

statistics for all coefficients, and there are no spikes in the correlogram graphs. The coefficient of determination here is equal to 0.88 (see Figure 40). Without the use of this trend variable, the best ARMA model we get is ARMA(3,2), which is also a good, but more complicated model. Moreover the use of a dummy variable is less relevant here than for United Airlines (according to the Schwarz Criterion). The use of the whole database leads to the model ARMA(3,3), and is not improved by the use of a dummy variable or a trend.

• Southwest: For the low-cost airline (real fares in Figure 41), the best ARMA model given by EViews6 according to the Schwarz criterion is an ARMA(0,3) with dummy variable and the trend variable for the filtered and non-filtered data. As for United and US Airways, the

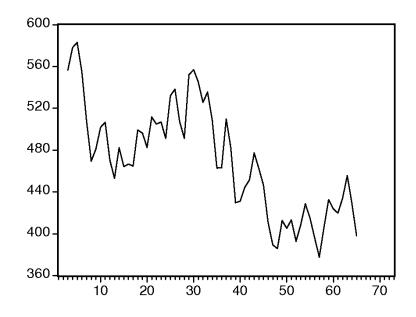


Figure 37: Quarterly average fares for United Airlines (\$ against time).

Schwarz criterion is higher for the non-filtered data, thus we will keep the regression output for the filtered data (Figure 142). The coefficient of determination is equal to 0.84, the model is stable, all the coefficients matter in the regression, and there is no spike in the correlogram graphs (despite a quite low Durbin-Watson statistic, equal to 1.63).

The use of simple ARMA models leads here to the AR(1) model as the best one for the filtered or non-filtered data. These models are transformed into ARMA(0,1) if we include a dummy variable or a trend coefficient in the regressions, but these models have a lower SIC criterion than the ARMA(0,3) model with a dummy variable and a trend. We can notice that the MA roots for this model are very close to 1, which could lead to problems of non-invertibility for the fares of Southwest.

Dependent Variable: FARE5 Method: Least Squares Date: 01/04/10 Time: 16:49 Sample (adjusted): 3 65 Included observations: 63 after adjustments Convergence achieved after 13 iterations Backcast: 1 2

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C DU <b>MMY</b> MA(1) MA(2)	506.1110 -77.86129 1.064661 0.673172	9.798012 13.35465 0.092880 0.092301	51.65446 -5.830275 11.46275 7.293217	0.0000 0.0000 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.847939 0.840207 20.95287 25902.35 -278.9902 1.981516	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		470.2444 52.41618 8.983816 9.119888 109.6677 0.000000
Inverted MA Roots	53+.62i	5362i		

Figure 38: United Airlines - regression on quarterly average fares.

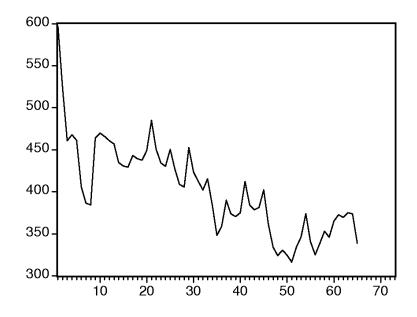


Figure 39: Quarterly average fares for US Airways (\$ against time).

Dependent Variable: FARE6 Method: Least Squares Date: 01/18/10 Time: 18:17 Sample: 1.65 Included observations: 65 Convergence achieved after 9 iterations Backcast: -1.0

Variable	Coefficient	Std. Error	t-Statistic	Prob.	
C @TREND MA(1) MA(2)	465.1703 -2.064267 1.007156 0.611885	12.42576 0.327728 0.073972 0.053711	37.43596 -6.298722 13.61534 11.39222	0.0000 0.0000 0.0000 0.0000	
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.884305 0.878615 18.79599 21550.64 -280.8536 2.147299	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		402.6931 53.94896 8.764727 8.898536 155.4164 0.000000	
Inverted MA Roots	50+.60i	5060i			

Figure 40: US Airways - regression on quarterly average fares.

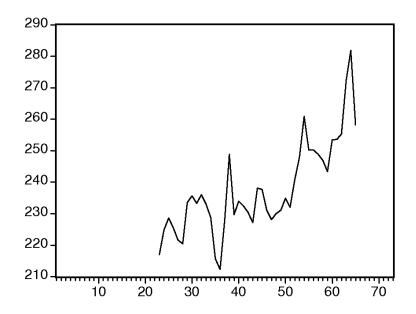


Figure 41: Quarterly average fares for Southwest Airlines (\$ against time).

Dependent Variable: FARE7 Method: Least Squares Date: 01/18/10 Time: 18:28 Sample (adjusted): 23.65 Included observations: 43 after adjustments Convergence achieved after 21 iterations Backcast: 20.22

Variable	Coefficient	Std. Error	t-Statistic	Prob.	
с	191.2149	2.219953	86.13462	0.0000	
DUMMY	-15.54111	2.749888	-5.651542	0.0000	
@TREND	1.321151	0.084972	15.54803	0.0000	
MA(1)	0.507582	0.040512	12.52921	0.0000	
MA(2)	-0.485910	0.032115	-15.13021	0.0000	
MA(3)	-0.900402	0.054744	-16.44746	0.0000	
R-squared	0.844654	Mean deper	237.7842		
Adjusted R-squared	0.823661	S.D. depend	14.63999		
S.E. of regression	6.147738	Akaike info	6.598833		
Sum squared resid	1398.403	Schwarz cri	6.844582		
Log likelihood	-135.8749	F-statistic	40.23547		
Durbin-Watson stat	1.629990	Prob(F-stati	0.000000		

Figure 42: Southwest Airlines - regression on quarterly average fares.

## 4.1.5 Summing up

Table 2 below summarizes the "best" models we get from our statistical regressions in EViews6. We can observe that there is no need for any carrier to use the differencing process to get the best model. The ARMA(0,2) model seems to be adopted by 4 carriers: American Airlines, Continental Airlines, United Airlines and US Airways. Among these carriers, the average fares of American Airlines seem to decrease since 1993, by about \$16.5 every 10 years, which is not so much for air transport fares. In addition to this trend, and as for the 3 other carriers, the fares of American Airlines seem to have been influenced by the terrorist attacks of September 11, 2001. Indeed, EViews6 shows a drop in these fares, at the time of these attacks, of about \$88 for American, \$52 for Continental, \$78 for United and \$65 for US Airlines. We can assume that for the other carriers, they may have been less affected by these attacks than American Airlines, or may have had a different strategy than its rival.

We can explain the use of ARMA(0,q) models by the use of a trend variable in many models, which reduces the importance of an autoregressive component in these models. These trends for the fares to decrease or increase over a period of 15 years may in part be explained by macroeconomic data. We will see that below. Indeed, we can observe that there is a trend for the fares of Northwest to decrease (by about \$29 every ten years), which may explain the situation of crisis recently undergone by the carrier before it was merged with Delta Airlines. On the contrary, here we can notice the obvious difference between the legacy carriers and Southwest, which is the only airline to progressively increase its fare (by about \$14 every ten years), even if the low-cost airline also suffered a sudden drop of its fares in 2001 (but of only \$16, in comparison with \$88 for American Airlines, for example).

All these models are stable, with no problems of autocorrelation in the residuals, high significance of each coefficient of the regressions and also high significance of all coefficients (given with the F-statistic of the regressions which follows a t-statistic). The Jarque-Bera statistic is also quite

Carriers	AA	СО	$\mathbf{DL}$	$\mathbf{NW}$	UA	$\mathbf{US}$	WN
use of filter on data	no	no	yes	no	yes	yes	yes
AR degree	0	0	1	4	0	0	0
MA degree	2	2	1	3	2	2	3
differencing	no	no	no	no	no	no	no
ARIMA model	(0,0,2)	(0,0,2)	(1,0,1)	(4,0,3)	(0,0,2)	(0,0,2)	(0,0,3)
trend variable	yes	no	yes	yes	no	yes	yes
value of trend coefficient	-1.65		-1.83	-2.87		-2.06	1.32
dummy variable at period 35	yes	yes	no	no	yes	no	yes
value of dummy coefficient	-88	-52			-78		-16
$R^2$	0.93	0.73	0.91	0.96	0.85	0.88	0.84
Schwarz criterion	9.20	9.22	8.83	8.21	9.12	8.90	6.84
Durbin-Watson statistic	2.22	2.20	1.98	1.89	1.98	2.15	1.63
Jarque-Bera statistic	4.99	2.13	0.71	2.51	4.49	0.20	0.40
F-statistic	214	56	197	161	110	155	40

Table 2: The carriers are reported with their IATA airline codes.

low for all the models, meaning that the residuals of all the models approximately follow a normal distribution.

### 4.1.6 Forecasting

Once we get these 7 ARIMA models for our carriers, we may wonder if we are able to infer the future average fares for an airline? A first idea in order to ensure the reliability of our model could be to "forecast the past" (in-sample). Indeed, we could try to apply our "best" model for each airline at a past period of time (for example from the first quarter in 2007), as if it was our last period of data, and compare this model for 2 years (until 2009) to the data we have for these 2 years. We get the following graphs (see Figure 43): we can observe 4 curves on these graphs, between quarter 58 and quarter 65: the real data, plotted for all the periods of observation (65 quarters), the best model for these fares (dashed curve), and around this forecast, the possible distribution of these fares at the 95% level of confidence around the value of the modelled fares. This distribution is computed as follows: at a given period t, for our model, and at a given level of confidence  $\alpha$ , we have

$$\widehat{\text{Fare}}(t) - (t - \text{stat}_{\alpha}(n) * \varepsilon(t)) \le \overline{\text{Fare}}(t) \le \widehat{\text{Fare}}(t) + (t - \text{stat}_{\alpha}(n) * \varepsilon(t))$$
(25)

, where t – stat<sub> $\alpha$ </sub>(n) is the t-statistic at the  $\alpha$  level of confidence for 2-tailed testing. Here, since n = 65, t – stat<sub> $\alpha$ </sub>(n)  $\approx 2$ .  $\widehat{\text{Fare}}(t)$  is the estimated fare at time t according to the best model for our regression.

We can observe that the trend for all the fares is quite well represented by our forecast. The real data are caught within the bounds of the standard errors for this model. However, in most cases, the model is not able to catch the short spikes in the real data and the forecast softens quite quickly.

We can also use this method to forecast the fares after the 65 periods of observations (out-ofsample). If we use the best model for each carrier and apply this model during 8 periods after the period 65, we get the following graphs (Figure 44). As we saw in 43, the forecast quickly softens after 3 or 4 quarters of modelled fares. This is a consequence of the stationarity of our models. We can observe that the model foresees decreasing trends of the fares for American Airlines, Delta Air Lines, Northwest Airlines and US Airways. For Continental Airlines and United Airlines, the fares seems to converge to a limit (about \$420 for both carriers). And as we saw in the regressions for Southwest airlines, the model for the low-cost airline predicts an important increasing trend for the average fares.

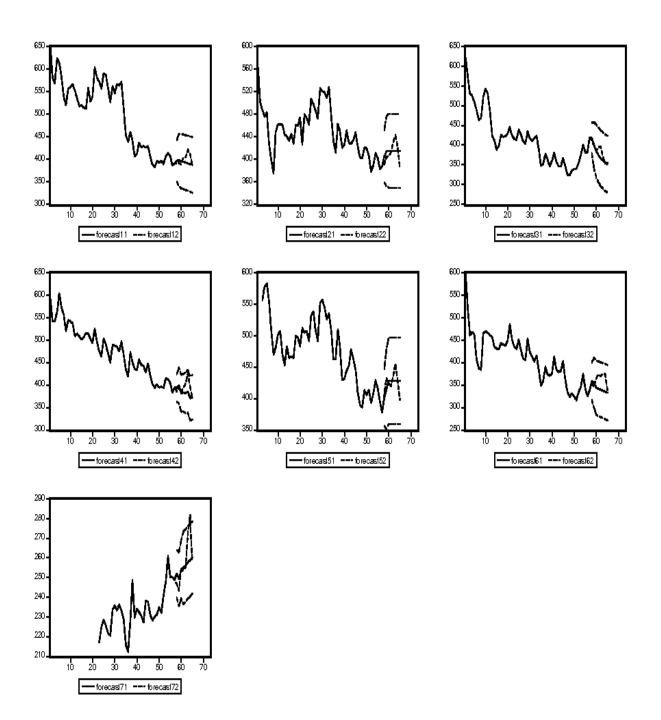


Figure 43: In-sample dynamic forecasts of average fares from quarter 58 to quarter 65. Forecast 1 refers to American, forecast 2 refers to Continental, 3 refers to Delta, 4 refers to Northwest, 5 refers to United, 6 refers to US Airways and 7 refers to Southwest.

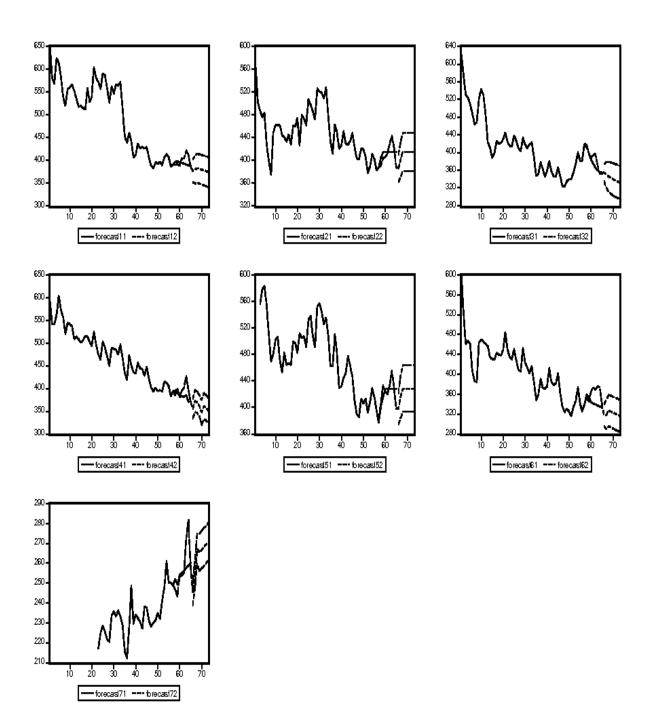


Figure 44: Out-of-sample dynamic forecasts of average fares from quarter 65 to quarter 73. Forecast 1 refers to American, forecast 2 refers to Continental, 3 refers to Delta, 4 refers to Northwest, 5 refers to United, 6 refers to US Airways and 7 refers to Southwest.

# 4.2 Passengers

We can now try to find models for the number of passengers (for domestic round trips in the U.S.) of these same 7 airlines. We first look at the graphs of this statistic (Figure 45). We notice that

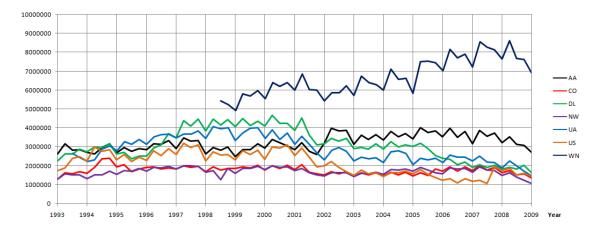


Figure 45: Number of passengers carried per quarter (on round trips) from 1993 (quarter 1) to 2009 (quarter 65).

the number of passengers for these airlines seems to include a quarterly component of seasonality. Indeed, we saw in the first part of the report that the number of passengers flying during the second quarter of the year is significantly higher than during the first or the fourth quarter of the year. A good model will need to take that into account. In order to catch this seasonality of fares for several airlines, we can add a seasonal autoregressive component in the regressions. Consider for example an ARMA(2,2) model :

$$\operatorname{Fare}(t) = \alpha_0 + \alpha_1 \times \operatorname{Fare}(t-1) + \alpha_2 \times \operatorname{Fare}(t-2) + \varepsilon(t) + \beta_1 \times \varepsilon(t-1) + \beta_2 \times \varepsilon(t-2).$$
(26)

This model can also be written, using the lag operator L,

$$A(L) \times \text{Fare}(t) = \alpha_0 + B(L) \times \varepsilon(t).$$
 (27)

Then, the insertion of a seasonal autoregressive lag of order 4 (SAR(4)) can be included:

$$A(L) * (1 - \gamma_0 \times L^4) \times \text{Fare}(t) = \alpha_0 + B(L) \times \varepsilon(t).$$
(28)

The parameter  $\gamma_0$  is associated with the seasonal component of the process. This method can also be used for the MA part of the model, with the use of a seasonal moving average component of order 4 (SMA(4)) in the regression, using the product of the polynomial B(L) with the lag polynomial  $1 + \delta_0 \times L^4$ . The use of a lag of order 4 for the seasonal component of the models seems to be here the most natural solution for our models, as the period of seasonality for the number of passengers appear to be one year (4 quarters).

If we run a first series of simple ARMA regressions, allowing our program in EViews6 to use a seasonal AR component of order 4 if it can reduce the Schwarz Information Criterion and, as a consequence, maybe improve our model, we get the following results:

• American: For American Airlines, even if the number of passengers appears to be seasonal (Figure 46), EViews6 chooses an ARMA(2,1) model without a seasonal component as the best model it can find (Figure 47). Nevertheless, we can observe from the regression output that this model is non-stationary and non-invertible, with an AR root higher than 1 in absolute value and a MA root equal to 1 in absolute value. If we include our seasonal component SAR(4) (Figure 48), even if the Schwarz Information Criterion is higher than for the first regression, this new coefficient AR(4) leads to a stationary and invertible model. Nevertheless, not all the coefficients in the regression appear to be individually significant. The Durbin Watson statistic is also quite low (1.92), and we can observe from the correlograms that there is some autocorrelation between the residuals of the regression. The  $R^2$  statistic is also quite low (0.59), so we can infer that this model can be improved. We saw that it is also possible to use a seasonal MA component (also of order 4) in our models. If we include

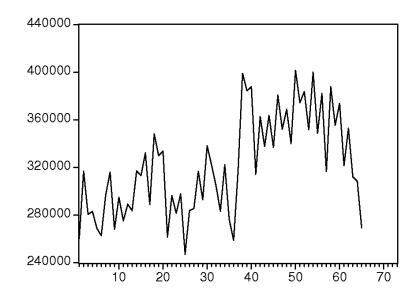


Figure 46: Quarterly number of passengers carried by American Airlines on round trips.

a SMA(4) coefficient in the regression, we obtain a non-stationary and maybe non-invertible model (Figure 49). If we impose the use of the seasonal component AR(4), and run the program in order to keep the model with the lowest SIC, we obtain an ARMA(0,2) model (with the seasonal component SAR(4)) (Figure 50). We can observe that all the coefficients are individually and jointly significant, and that the model is invertible and stationary. The Durbin Watson statistic is still quite low, but we can check on the correlograms that there is no autocorrelation in the residuals at the 95% level of confidence. We obtain an  $R^2$  statistic equal to 0.62.

**Remark**: As for the regressions on the quarterly average fares of the airline, these regressions on the number of passengers use the filtered data of our database. However, if we use the nonfiltered data, the result appears to be an ARMA(0,2) with the seasonal component SAR(4) too (Figure 51). The  $R^2$  statistic and the SIC are nonetheless not as good as for the regression with the filtered data.

Dependent Variable: PAX1 Method: Least Squares Date: 01/21/10 Time: 09:49 Sample (adjusted): 3 65 Included observations: 63 after adjustments Convergence achieved after 28 iterations Backcast: 2

Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	322180.7	16902.76	19.06083	0.0000
<b>A</b> R(1)	-0.192253	0.078517	-2.448555	0.0173
AR(2)	0.838684	0.077086	10.87980	0.0000
MA(1)	0.99 <b>738</b> 5	0.045562	21.89049	0.0000
R-squared	0.669609	Mean dependent var		322969.0
Adjusted R-squared	0.652809	S.D. dependent var		41344.73
S.E. of regression	24361.52	Akaike into criterion		23.10078
Sum squared resid	3.50E+10	Schwarz crit	terion	23.23686
Log likelihood	-723.6747	F-statistic		39.85870
Durbin-Watson stat	1.870131	Prob(F-stati	stic)	0.000000
Inverted AR Roots	.82	-1.02		
	Estimated A	R process is	nonstationar	v
Inverted MA Roots	-1.00			-

Figure 47: American Airlines - regression on the quarterly number of passengers (filtered data).

• Continental: Using the same methodology, we also find out that if we do not impose the use of the coefficient SAR(4) in our regression, the model we get (an ARMA(3,4) with our dummy variable and without the coefficient SAR(4)) is non-stationary and non-invertible (for the filtered and non-filtered data). However, we notice that, even if we include an SAR(4) variable or SMA(4) variable, we still have problems of stationarity for both databases.

Looking at the graph of the number of passengers for the carrier (Figure 52), we can observe that there seems to be a gap in the number of passenger in the period 35 (presumably related to the September 11 attacks). Thus if we try to impose the use of our dummy variable in the model for Continental Airlines, the model we get with the filtered data appears to be very complex (an ARMA(2,4) with a dummy variable and a seasonal component SAR(4)). However, if we use the complete database, we get an ARMA(0,2) model with our dummy

Dependent Variable: PAX1 Method: Least Squares Date: 01/21/10 Time: 10:12 Sample (adjusted): 7 65 Included observations: 59 after adjustments Convergence achieved after 228 iterations Backcast: 6

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C AR(1) AR(2) SAR(4) MA(1)	333135.7 0.573187 -0.071156 0.714231 0.137400	28234.90 0.406710 0.277897 0.105706 0.428566	11.79872 1.409327 -0.256051 6.756761 0.320604	0.0000 0.1645 0.7989 0.0000 0.7497
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.592411 0.562220 26840.61 3.89E+10 -682.7677 1.917247	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent var criterion terion	326291.7 40566.20 23.31416 23.49022 19.62164 0.000000
Inverted AR Roots	.92 .00+.92i 14	.39 92	.18	.009 <b>2</b> i

Figure 48: American Airlines - regression on the quarterly number of passengers (filtered data).

variable and the seasonal component SAR(4) (see Figure 53), which appears to be quite a good model. This model is stationary, so we can infer that the use of this dummy variable is a good solution for Continental Airlines. Indeed, we can observe that all the coefficients are significant, with a coefficient for the dummy variable equal to -4,8710, which means that according to this model the number of passengers dropped by about 50,000 in the period of the U.S. terrorist attacks. The Durbin Watson statistic is quite low, but there is no apparent spike in the correlograms of the regressions, so the residuals appear not to be autocorrelated. The  $R^2$  statistic is very high (0.81) compared to the statistic we get with the model for American Airlines.

• Delta Air Lines: For Delta Air Lines, the use of seasonal components in the regression

Dependent Variable: PAX1 Method: Least Squares Date: 01/21/10 Time: 10:17 Sample (adjusted): 7 65 Included observations: 59 after adjustments Convergence achieved after 21 iterations Backcast: 2 6

Variable	Coefficient	Std. Error	t-Statistic	Prob.
с	326285.2	180699.2	1.805682	0.0766
AR(1)	0.281747	0.167523	1.681842	0.0985
AR(2)	0.406260	0.167297	2.428377	0.0186
SAR(4)	1.027199	0.025439	40.37888	0.0000
MA(1)	0.570184	0.136224	4.185633	0.0001
SMA(4)	-0.916045	0.069 <b>748</b>	-13.13361	0.0000
R-squared	0.722963	Mean deper	ndent var	326291.7
Adjusted R-squared	0.696828	S.D. depen	dent var	40566.20
S.E. of regression	22336.20	Akaike info	criterion	22.96195
Sum squared resid	2.64E+10	Schwarz cri	terion	23.17322
Log li <b>ke</b> lihood	-671.3775	F-statistic		27.66205
Durbin-Watson stat	1.656182	Prob(F-stati	stic)	0.000000
Inverted AR Roots	1.01	.79	.00+1.01i	00-1.01i
	51	-1.01		
	Estimated A	R process is	nonstationa	ry
Inverted MA Roots	.98			

Figure 49: American Airlines - regression on the quarterly number of passengers (filtered data).

appears to make the model unstable, and EViews6 does not manage to find a stationary ARMA model with a seasonal component. If we look at the graph of the number of passengers for the airline (Figure 54), we can observe that, as for Continental Airlines, there was an important drop in the number of passengers carried by Delta in period 35. Thus, as we could expect according to this graph, if we do not use the seasonal coefficients in our regression, EViews6 gives the model AR(3) with a dummy variable as the best model according to the Schwarz Information Criterion, for the filtered data (Figure 55). For the non-filtered data, EViews6 gives a ARMA(2,1) with a dummy variable and a trend variable (Figure 56). Both models are stationary, but the model for non-filtered data is not invertible, so we may keep the regression output for the filtered data. All coefficients are individually significant,

Dependent Variable: PAX1 Method: Least Squares Date: 01/21/10 Time: 10:41 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 13 iterations Backcast: 3 4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C AR(4) MA(1) MA(2)	326588.4 0.555991 0.499125 0.606607	15818.06 0.113867 0.102449 0.098701	20.64655 4.882813 4.871933 6.145918	0.0000 0.0000 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.623211 0.603380 26030.31 3.86E+10 -704.6747 1.766312	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		324314.0 41332.54 23.23524 23.37365 31.42613 0.000000
Inverted AR Roots Inverted MA Roots	.86 - 25- 74i	25+.74i		

Figure 50: American Airlines - regression on the quarterly number of passengers (filtered data).

with a high coefficient of determination for both regressions. The Durbin-Watson statistic is quite low as for the previous airlines, but there are no spikes to indicate possible problems of autocorrelation in the correlograms. For the model obtained with the filtered data, we can notice that the drop in the number of passengers after the period of the U.S. terrorist attacks is about 135,000 passengers, which is roughly much 30% of the total number of passengers carried by Delta in period 34!

• Northwest Airlines: It also appears difficult to avoid the problems of stationarity for the number of passengers carried quarterly by Northwest Airlines (Figure 57). The best model we can obtain with all the possible parameters in our program is an ARMA(2,1) with a dummy variable and no correction for possible seasonality of the fares. However, this model appears to be non-stationary. If we do not filter the data, EViews6 proposes the same model

Dependent Variable: PAX1 Method: Least Squares Date: 01/21/10 Time: 10:48 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 12 iterations Backcast: 3 4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C AR(4) MA(1) MA(2)	380058.1 0.428841 0.519392 0.546597	14059.06 0.125038 0.106697 0.108486	27.03296 3.429687 4.867896 5.038411	0.0000 0.0011 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.453922 0.425181 30231.56 5.21E+10 -713.8018 1.842834	Mean depen S.D. depend Akaike info Schwarz crit F-statistic Prob(F-statistic	lent var criterion erion	384009.7 39874.47 23.53449 23.67290 15.79355 0.000000
Inverted AR Roots Inverted MA Roots	.81 26+.69i	.0081i 2669i	.00+.81i	81

Figure 51: American Airlines - regression on the quarterly number of passengers (non-filtered data).

as the best one (according to the SIC), but with a seasonal coefficient SAR(4) (Figure 58). This model is stationary, but non-invertible. All coefficients are individually significant, the  $R^2$  statistic is quite high (0.80), but there are still some problems of autocorrelation in the residuals (we can observe a spike in the correlograms at the 6th lag).

• United Airlines: For United Airlines (quarterly number of passengers plotted in Figure 59), EViews6 gives the ARMA(0,2) with a dummy variable, a trend variable and the seasonal variable SAR(4) (here equal to the variable AR(4) as there is no other AR lag in the regression) (Figure 60). For the non-filtered data, EViews6 adds an AR lag of order 1 to the regression to find the best model for the number of passengers of the airline (Figure 61). Both models seem to be quite good: all coefficients are individually (and jointly) significant, stationary, invertible, with no problems of autocorrelation. The  $R^2$  statistic is quite high (0.93 and 0.94),

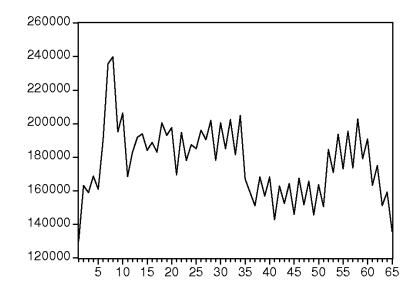


Figure 52: Number of passengers carried by Continental Airlines per quarter.

the Schwarz criterion is a little lower for the regression on the filtered data (the different number of explanatory variables in the regression can explain that the SIC is higher for the regression on the whole database). These regressions show an important trend for the number of passengers of the airline to decrease over time, by more or less 4000 passengers per quarter. United Airlines also suffered an important drop in its number of passengers in 2001, of about 59,000 passengers for the filtered database and 70,000 passengers without the lower bound on the data (lower bound for all flights with less than 90 passengers, which explains the difference between the coefficients of the dummy variables).

• US Airways: For US Airways (quarterly number of passengers plotted in Figure 62), the best model we get is an ARMA(2,1) with a dummy variable, for the filtered data (Figure 63). We can observe that this regression also has problems with stationarity. In order to make our model stationary, we include in the model the seasonal coefficient SAR(4). According to the SIC, the best model we can then get is an ARMA(1,2) with a dummy variable, the

Dependent Variable: PAX2 Method: Least Squares Date: 01/21/10 Time: 11:20 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 22 iterations Backcast: 3 4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C DUMMY AR(4) MA(1)	229040.4 -48709.56 0.255780 0.201643	6214.957 7348.126 0.109379 0.025081	36.85309 -6.628841 2.338471 8.039579	0.0000 0.0000 0.0230 0.0000
MA(2)	0.953083	0.026899	35.43151	0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.807005 0.793220 13093.30 9.60E+09 -662.2181 1.406419	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		204695.8 28793.51 21.87600 22.04902 58.54074 0.000000
Inverted AR Roots Inverted MA Roots	.71 10+ .97i	.00 <b>71</b> i 1097i		

Figure 53: Continental Airlines - regression on the quarterly number of passengers (non-filtered data).

seasonal coefficient SAR(4) and a seasonal moving average component SMA(4) (Figure 64). For the non-filtered data, the best model with a seasonal component is the same model with a trend variable (this coefficient shows a trend of about -1922 passengers carried by the airline per quarter). This model is still non-invertible, but it is stationary. All the coefficients are individually significant, and the  $R^2$  statistic is equal to 0.94. The SIC criterion is again higher for the more complicated model (regression with the trend variable), so we will keep the results for the filtered data.

• Southwest: For Southwest, there are some problems with stationarity for many models, so it is very difficult to compare an important number of regressions with our program. Looking at the graph of the number of passengers for the low-cost airline, we can observe that there is a

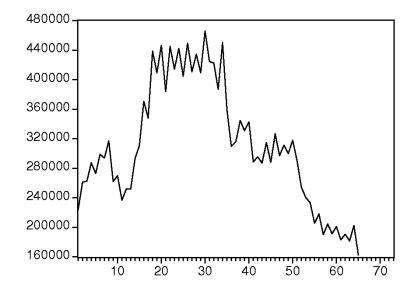


Figure 54: Number of passengers carried by Delta Air Lines per quarter.

Dependent Variable: PAX3
Method: Least Squares
Date: 01/21/10 Time: 12:27
Sample (adjusted): 4 65
Included observations: 62 after adjustments
Convergence achieved after 10 iterations

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C DUMMY AR(1) AR(2)	381400.0 -134581.6 0.639650 0.786474	41941.45 24922.08 0.116538 0.101400	9.093630 -5.400095 5.488761 7.756157	0.0000 0.0000 0.0000 0.0000
AR(3)	-0.503618	0.111887	-4.501142	0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.927800 0.922733 23389.76 3.12E+10 -709.0909 1.793060	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent <b>v</b> ar criterion terion	314346.4 84145.02 23.03519 23.20673 183.1173 0.000000
Inverted AR Roots	.89	.64	89	

Figure 55: Delta Air Lines - regression on the quarterly number of passengers (filtered data).

Dependent Variable: PAX3
Method: Least Squares
Date: 01/21/10 Time: 12:32
Sample (adjusted): 3 65
Included observations: 63 after adjustments
Convergence achieved after 89 iterations
Backcast: OFF (Roots of MA process too large)

Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	600 <b>737</b> .5	65773.57	9.133418	0.0000
DUMMY	-120190.6	31818.37	-3.777397	0.0004
@TREND	-3631.146	1624.054	-2.235853	0.0293
AR(1)	-0.128164	0.046742	-2.741924	0.0081
AR(2)	0.837394	0.041679	20.09168	0.0000
MA(1)	1.156464	0.085352	13.54934	0.0000
R-squared	0.958505	Mean dependent var		401949.3
Adjusted R-squared	0.954865	S.D. dependent var		106588.0
S.E. of regression	22644.55	Akaike info criterion 22		22.98362
Sum squared resid	2.92E+10	Schwarz criterion 23.18		23.18773
Log likelihood	-717.9840	F-statistic 263.3		263.3331
Durbin-Watson stat	1.651653	Prob(F-stati	stic)	0.000000
Inverted AR Roots	.85	98		
Inverted MA Roots	-1.16			
Estimated MA process is noninvertible				

Figure 56: Delta Air Lines - regression on the quarterly number of passengers (non-filtered data).

significant trend for this statistic to increase over time (see Figure 65). Thus we can infer that we need to consider a model which takes into account this trend. Then we can first try to run a basic regression with a constant and a trend to observe the correlograms of the regression. We get the following regression output (Figure 66) and the associated correlograms (Figure 66). We can observe that the use of the trend is very important in this model, as we do not reject the coefficient at the 99% level of confidence. This trend is equal to +6533 passengers per quarter for the airline: this is clearly a sign of the strength of the low-cost airline in the U.S. domestic market, where almost all its "rivals" have faced a roughly stable or decreasing number of passengers over the past 15 years. The correlograms of the regression show a high autocorrelation with the fourth lag of the regression. We can assume that this is perhaps a

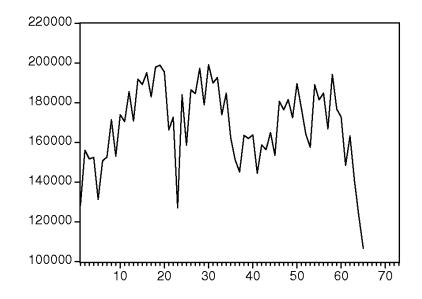


Figure 57: Number of passengers carried by Northwest Airlines per quarter.

sign of seasonality for the fares, so we can try to include a coefficient SAR(4) in the regression (Figure 68). We can see in the regression output that this model is better than the previous one (a higher  $R^2$  statistic and a lower SIC). This model remains stationary, and is invertible. Nevertheless, there is an important spike which appeared in the correlograms (for the first lag of the residuals), so there are problems of autocorrelation in this regression, which does not include any ARMA term. In fact, we can observe that if we try to run our program with these coefficients of trend and seasonality, EViews6 is not able to find a better model than this one. The same problems also remain with the non-filtered data.

Dependent Variable: PAX4 Method: Least Squares Date: 01/21/10 Time: 13:30 Sample (adjusted): 7 65 Included observations: 59 after adjustments Convergence achieved after 58 iterations Backcast: OFF (Roots of MA process too large)

•	•• •		
Coefficient	Std. Error	t-Statistic	Prob.
254617.2	15436.95	16.49401	0.0000
-43080.92	17440.01	-2.470234	0.0168
-0.217220	0.100772	-2.155565	0.0357
0.751454	0.074553	10.07951	0.0000
0.304807	0.135366	2.251722	0.0285
1.203116	0.139858	8.602432	0.0000
0.804739	Mean deper	ndent var	232577.6
0.786318	S.D. dependent var		35134.29
16241.08	Akaike info	criterion	22.32462
1.40E+10	Schwarz crit	terion	22.53589
-652.5763	F-statistic		43.68636
1.799537	Prob(F-stati	stic)	0.000000
.77	.74		
-1.20			
	254617.2 -43080.92 -0.217220 0.751454 0.304807 1.203116 0.804739 0.786318 16241.08 1.40E+10 -652.5763 1.799537	254617.2         15436.95           -43080.92         17440.01           -0.217220         0.100772           0.751454         0.074553           0.304807         0.135366           1.203116         0.139858           0.804739         Mean deper           0.786318         S.D. depend           16241.08         Akaike info           1.40E+10         Schwarz crit           -652.5763         F-statistic           1.799537         Prob(F-stati           .77         .74	254617.2         15436.95         16.49401           -43080.92         17440.01         -2.470234           -0.217220         0.100772         -2.155565           0.751454         0.074553         10.07951           0.304807         0.135366         2.251722           1.203116         0.139858         8.602432           0.804739         Mean dependent var           0.786318         S.D. dependent var           16241.08         Akaike info criterion           1.40E+10         Schwarz criterion           -652.5763         F-statistic           1.799537         Prob(F-statistic)

Estimated MA process is noninvertible

Figure 58: Northwest Airlines - regression on the quarterly number of passengers (non-filtered data).

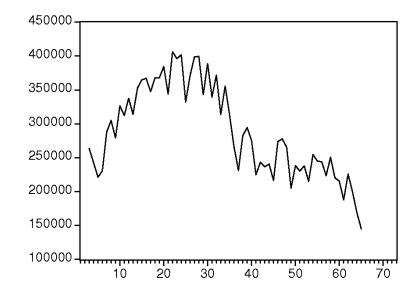


Figure 59: Number of passengers carried by United Airlines per quarter.

Dependent Variable: PAX5 Method: Least Squares Date: 01/21/10 Time: 13:54 Sample (adjusted): 7.65 Included observations: 59 after adjustments Convergence achieved after 13 iterations Backcast: 5.6

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C DUMMY @TREND AR(4) MA(1) MA(2)	513864.2 -58526.63 -4370.729 0.689866 0.522843 0.614518	76554.14 19200.79 1499.527 0.082843 0.114180 0.113511	6.712428 -3.048137 -2.914738 8.327378 4.579130 5.413733	0.0000 0.0036 0.0052 0.0000 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.929813 0.923192 18845.88 1.88E+10 -661.3526 2.043954	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent <b>v</b> ar criterion terion	292042.9 68000.47 22.62212 22.83340 140.4250 0.000000
Inverted AR Roots Inverted MA Roots	.91 2674i	.0091i 26+.74i	.00+.91i	91

Figure 60: United Airlines - regression on the quarterly number of passengers (filtered data).

Dependent Variable: PAX5 Method: Least Squares Date: 01/21/10 Time: 14:00 Sample (adjusted): 6 65 Included observations: 60 after adjustments Convergence achieved after 24 iterations Backcast: 4 5

Variable	Coefficient	Std. Error t-Statistic		Prob.	
C	522589.0	7.5118709.15-3.734938.315991.5509-3.842783.3980.097803-4.390460.8790.0815867.254673.8560.1263656.867870		0.0000	
DUMMY	-69877.51			0.0005	
@TREND	-3810.315			0.0003	
AR(1)	-0.429398			0.0001	
SAR(4)	0.591879			0.0000	
MA(1)	0.867856			0.0000	
MA(2)	0.599171			0.0000	
R-squared	0.941251	Mean dependent var		333356.2	
Adjusted R-squared	0.934600	S.D. dependent var		78728.78	
S.E. of regression	20133.58	Akaike info criterion		22.76745	
Sum squared resid	2.15E+10	Schwarz criterion		23.01179	
Log likelihood	-676.0234	F-statistic		141.5244	
Durbin-Watson stat	1.942071	Prob(F-statistic)		0.000000	
Inverted AR Roots	.88 88 43+.64i	00+.88i 4364i	00 <b>88i</b>	43	

Figure 61: United Airlines - regression on the quarterly number of passengers (non-filtered data).

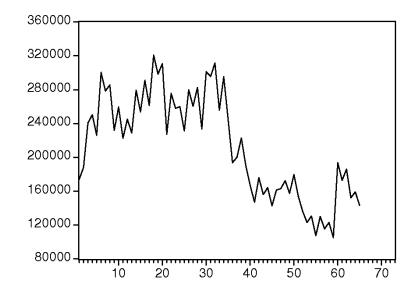


Figure 62: Number of passengers carried by US Airways per quarter.

Dependent Variable: PAX6 Method: Least Squares Date: 01/21/10 Time: 14:40 Sample (adjusted): 3.65 Included observations: 63 after adjustments Convergence achieved after 12 iterations Backcast: 2							
Variable	Prob.						
C DUMMY AR(1) AR(2) MA(1)	267344.2 -109693.0 -0.429863 0.556714 0.997127	8060.288 10620.38 0.092585 0.091936 0.033607	33.16807 -10.32854 -4.642904 6.055473 29.66990	0.0000 0.0000 0.0000 0.0000 0.0000			
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.900232 0.893352 20180.78 2.36E+10 -711.2749 1.581042	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		214699.5 61796.14 22.73889 22.90898 130.8378 0.000000			
Inverted AR Roots Inverted MA Roots	.56 -1.00	99					

Figure 63: US Airways - regression on the quarterly number of passengers (filtered data).

Dependent Variable: PAX6 Method: Least Squares Date: 01/21/10 Time: 14:52 Sample (adjusted): 6 65 Included observations: 60 after adjustments Convergence achieved after 33 iterations Backcast: 0 5

Variable	Coefficient	Std. Error t-Statistic		Prob.
C DUMMY AR(1) SAR(4) MA(1) MA(2) SMA(4)	285182.8 -126797.1 -0.819342 0.743030 1.543017 0.969097 -0.899145	10821.30 11166.48 0.051731 0.064832 0.028907 0.025384 0.032669	26.35385 -11.35515 -15.83851 11.46089 53.37941 38.17788 -27.52285	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.922032 0.913205 18577.73 1.83E+10 -671.1979 1.890107	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		213485.1 63058.81 22.60660 22.85094 104.4607 0.000000
Inverted AR Roots Inverted MA Roots	.93 .97 77+.61i	.0093i .00+.97i 97	009 <b>7</b> i	<b>77</b> 61i

Figure 64: US Airways - regression on the quarterly number of passengers (non-filtered data).

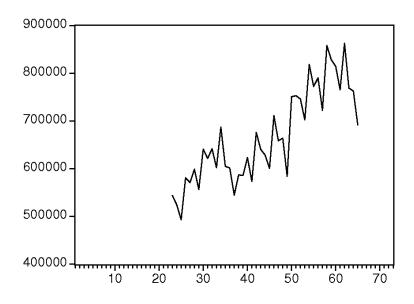


Figure 65: Number of passengers carried by Southwest Airlines per quarter.

Dependent Variable: PAX7 Method: Least Squares Date: 01/21/10 Time: 15:39 Sample (adjusted): 23 65 Included observations: 43 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.	
C	388125.5	28956.25	13.40386	0.0000	
@TREND	6533.313	646.9963	10.09791	0.0000	
R-squared	0.713222	Mean dependent var		669057.9	
Adjusted R-squared	0.706228	S.D. dependent var		97138.40	
S.E. of regression	52649.76	Akaike info criterion		24.62611	
Sum squared resid	1.14E+11	Schwarz criterion		24.70802	
Log likelihood	-527.4613	F-statistic		101.9679	
Durbin-Watson stat	1.525955	Prob(F-statistic)		0.000000	

Figure 66: Southwest Airlines - regression on the quarterly number of passengers (filtered data).

Date: 01/21/10 Time: 15:39 Sample: 23 65 Included observations: 43

\_

Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
· 🗐 ·	I I 🗖 I	1 0.143	0.143	0.9369	0.333
ı 🔲 i	I I 🔲 I	2 0.261	0.246	4.1506	0.126
1 <b>1</b> 1	I I I I	3 0.033	-0.032	4.2044	0.240
		4 0.447	0.416	14.100	0.007
I 🔲 I	I I I	5 -0.090	-0.251	14.511	0.013
1 <b>1</b> 1	I I I I	6 -0.032	-0.206	14.564	0.024
I 🛄 I	I I I I	7 -0.196	-0.118	16.631	0.020
ı 🗖 ı	I I I I	8 0.169	0.102	18.217	0.020
I 🔲 I		9 -0.178	-0.030	20.022	0.018
- <b>- - -</b>		10 -0.076	-0.012	20.361	0.026
I 🔲 I	I I I I	11 -0.119	0.074	21.220	0.031
1 🔲 1	I I I I	12 0.093	-0.063	21.762	0.040
I 🔲 I	I I I I	13 -0.132	-0.068	22.886	0.043
I 🛛 I	I [] I	14 -0.072	-0.055	23.228	0.057
I 🔲 I	I I I I	15 -0.145	-0.103	24.677	0.054
1 1	1 1 1	16 0.018	-0.027	24.701	0.075
I 🛛 I	I I 🗖 I	17 -0.066	0.103	25.025	0.094
	I <b> </b> I	18 -0.008	0.071	25.029	0.124
1 1	I <b> </b> I	19 0.007	0.092	25.033	0.159
1 <b>þ</b> . í		20 0.036	-0.075	25.145	0.196

Figure 67: Southwest Airlines - correlograms of the residuals for the regression in Figure 66.

Dependent Variable: PAX7 Method: Least Squares Date: 01/21/10 Time: 15:55 Sample (adjusted): 27 65 Included observations: 39 after adjustments Convergence achieved after 7 iterations

Variable	Coefficient	Std. Error	. Error t-Statistic	
C	440934.0	96946.85	1823.321 2.994573	
@TREND	5460.067	1823.321		
AR(4)	0.623446	0.149988		
R-squared	0.764005	Mean dependent var		682713.4
Adjusted R-squared	0.750894	S.D. dependent var		90907.93
S.E. of regression	45372.61	Akaike info criterion		24.35701
Sum squared resid	7.41E+10	Schwarz criterion		24.48497
Log likelihood	-471.9617	F-statistic		58.27279
Durbin-Watson stat	0.785936	Prob(F-statistic)		0.000000
Inverted AR Roots	.89			

Figure 68: Southwest Airlines - regression on the quarterly number of passengers (filtered data).

#### 4.2.1 Summing up

Table 3 below summarizes the "best" models we get from our statistical regressions in Eviews6. We can again observe that there is no need for any carrier to use the differencing process to get the best model. The ARMA(0,2) model seems again to be adopted by 4 carriers, as it was the most adopted model for the regressions on fares, and for the same models: American Airlines, Continental Airlines, United Airlines. Here we found that the regressions for US Airways also need an autoregressive component to best fit the data. For Delta Air Lines and Northwest Airlines, we found an important autoregressive part in the model for the number of passengers. For Delta, this autoregressive component can also be related to the absence of seasonality coefficient in its regression, which leads to a stronger dependence from the closest past lags rather than from the usual quarterly number of passengers in a given quarter of the year. This may perhaps be explained by a higher volatility in the number of passengers carried by the airline.

We can see that 5 of the carriers underwent an important drop of their number of passengers after September 11, 2001, especially for Delta Air Lines and US Airways. The line "drop of number of passengers after period 34" (equal to the ratio between the dummy variable and the number of passengers carried during the period 34) shows the percentage decrease of the fares after period 34 which we can attribute to the consequences of the September 11, 2001 attacks. We can also observe that there seems to be a trend for the number of passengers flying with United Airlines to decrease by about 4370 passengers per quarter. On the contrary, as we saw for the fares, the low-cost carrier Southwest continuously increases its number of passengers by about 5460 per quarter, whereas the other airlines are stable or try to keep their passengers!

All these remarks should be qualified by the relative quality of these regressions. Even if these models are stationary and invertible, the low values of the Durbin-Watson show that it is difficult to find good models with no autocorrelation. We can partly explain this by the fact that, contrary to the fares, the number of passengers carried by an airline is more subject to volatility and depends

Carriers	AA	CO	$\mathbf{DL}$	NW	UA	$\mathbf{US}$	WN
use of filter on data	yes	no	yes	no	yes	yes	yes
AR degree	0	0	3	2	0	1	0
MA degree	2	2	0	1	2	2	0
differencing	no	no	no	no	no	no	no
ARIMA model	$(0,\!0,\!2)$	(0,0,2)	$(3,\!0,\!0)$	(2,0,1)	(0,0,2)	(1,0,2)	no
seasonal AR variable	yes	yes	no	yes	yes	yes	yes
seasonal MA variable	no	no	no	no	no	yes	no
trend variable	no	no	no	no	yes	no	yes
value of trend coefficient	no	no	no	no	-4370	no	5460
dummy variable at period 35	no	yes	yes	yes	yes	yes	no
value of dummy coefficient	no	-48700	-134600	-43100	-58500	-126800	no
passengers at period 34		233841	450327	246746	355741	295224	
drop of number of passengers		21%	30%	17%	16%	43%	
after period 34							
$R^2$	0.62	0.81	0.93	0.80	0.93	0.92	0.76
Schwarz criterion	23.2	22.1	23.2	22.5	22.8	22.9	24.5
Durbin-Watson statistic	1.77	1.41	1.79	1.80	2.04	1.89	0.79
Jarque-Bera statistic	0.77	2.07	1.54	9.83	0.10	0.31	3.10
F-statistic	31	59	183	44	140	104	58

Table 3: The carriers are reported with their IATA airline codes.

more on other economic, political and social parameters than the fares of a carrier.

#### 4.2.2 Forecasting

With these 7 models, as for the fares, we could try to forecast the number of passengers for 1 on 2 years in the future. To ensure the reliability of our model, we can try to "forecast the past", as we did for the fares. We get the following graphs (see Figure 69), the real data plotted for all periods of observation (65 quarters), the best model for these data (dashed curve), and around this model, the possible distribution of the number of passengers at the 95% level of probability around the modelled value. We can see that, as expected, these models are not as good as the regressions for the fares of the airline, and hardly stabilize (especially for American Airlines). We also emphasize the small number of observations used for these regressions, which makes it very difficult to fit data correctly. However, we can again try to use this method to forecast the number of passengers after the 65 periods of observations. If we use the best model for each carrier and apply this model over 8 periods after period 65, we get the following graphs (Figure 70). We can also notice that the recent economic crisis also undergone by the U.S. airlines has led to a recent drop in the number of passengers for several airlines. As a consequence, our stationary models forecast for American Airlines, Continental Airlines, Delta and Northwest, an increase in passenger numbers for the next 2 years. On the contrary, United Airlines is here expected to continuously lose some passengers, following a global decreasing trend for the traffic of the carrier. For US Airways, this number of passengers may remain constant for the next 2 years, at around 150,000 passengers per quarter.

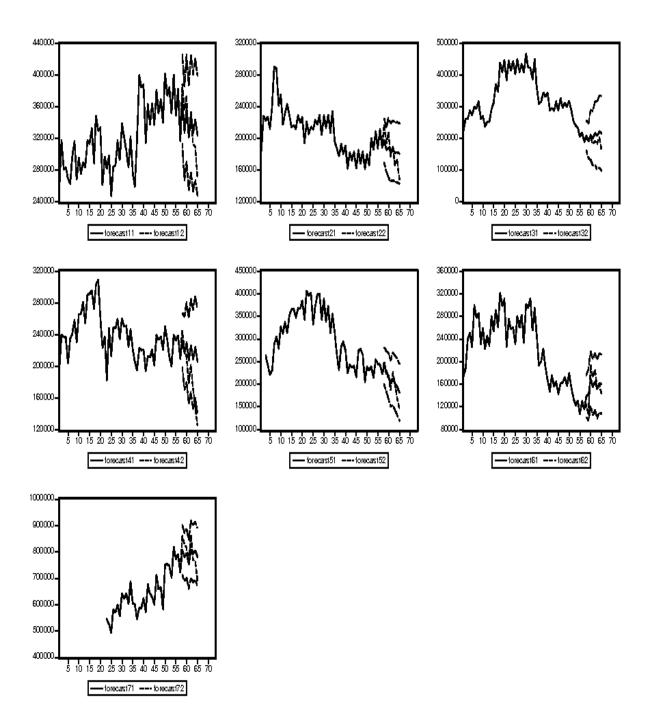


Figure 69: In-sample dynamic forecasts of the number of passengers carried from quarter 58 to quarter 65. Forecast 1 refers to American, forecast 2 refers to Continental, 3 refers to Delta, 4 refers to Northwest, 5 refers to United, 6 refers to US Airways and 7 refers to Southwest.

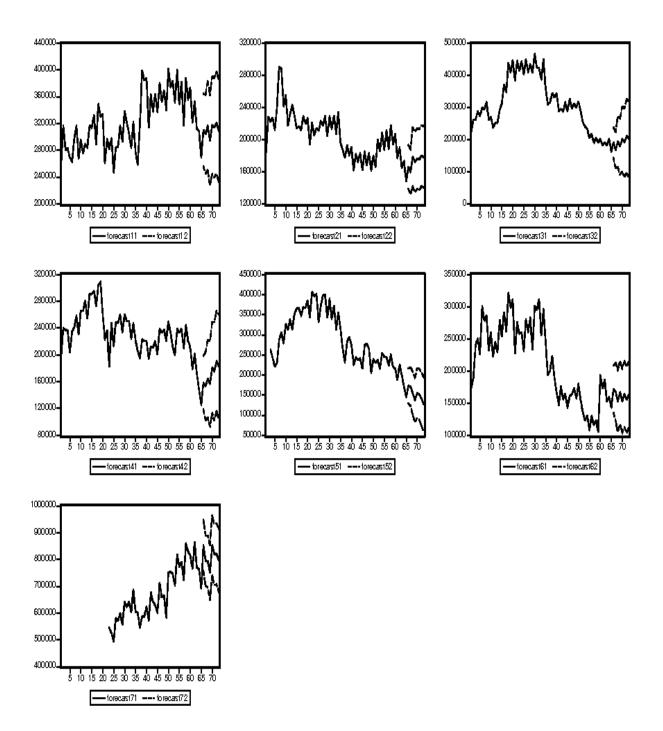


Figure 70: Out-of-sample dynamic forecasts of the number of passengers carried from quarter 65 to quarter 73. Forecast 1 refers to American, forecast 2 refers to Continental, 3 refers to Delta, 4 refers to Northwest, 5 refers to United, 6 refers to US Airways and 7 refers to Southwest.

# 5 Insertion of economic data

In order to improve the reliability of our models, we could then try to include some economic data in these regressions, especially for the regressions on fares.

## 5.1 Economic Data

#### 5.1.1 Form 41 Financial Data

To implement real world economic data on the airlines into our models we use the so-called "Form 41 Financial Data" collected by the Bureau of Transport Statistics.<sup>17</sup> This dataset covers various financial and other core data of U.S. airlines with an annual operating revenue of more than \$20 million. We use the "Schedule B-1" table out of which we only take the accrued salaries in every quarter, the "Schedule P-10" table containing information on the number of people employed by each airline in every year, the "Schedule P-12" table which gives quarterly information on different financial facts and the "Schedule P-12A" with data on each airline's monthly fuel consumption and expenses. In order to be able to properly include all financial information into the models, adjustments for the inflation effects have to be made. This is carried out as described in Section 3.1.3. The treatment of the raw data is carried out with Excel and the help of programs written in VBA which can be found in Appendix A.3.

#### 5.1.2 B-1 Table Data

The only variable out of this table that we want to use is ACCR\_SALARIES. Unfortunately for this variable there is no information available after 2006, and for Northwest even the 2006Q4 datapoint is missing. Delta Airline's graph, as seen in Figure 71, shows between 1997 and 2002 a very high level of salary expenses which seems odd and for which we cannot find an explanation. It can be

<sup>&</sup>lt;sup>17</sup>The data is available on the Bureau's website: http://www.transtats.bts.gov/DatabaseInfo.asp?DB\_ID= 135&Link=0.

assumed though that such behaviour will not help when trying to model the development of Delta's fares using this variable.

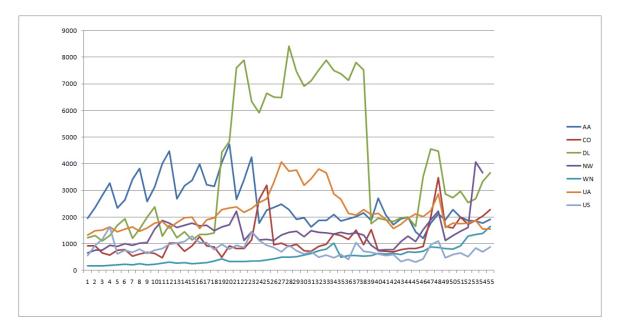


Figure 71: Accrued Salaries of the 7 airlines between 1993 and 2006, i.e. quarter no. 1 is 1993Q1 and quarter no. 55 is 2006Q4.

## 5.1.3 P-10 Table Data

Out of all the variables available in the table, we decided to download and examine the following:

- GENERAL\_MANAGE
- PILOTS\_COPILOTS
- OTHER\_FLT\_PERS
- PASSENGER\_HANDLING
- TRANSPORT\_RELATED

### • TOTAL

The employee data was available for every year until 2008, so in order to get quarterly data that could be used in the model we use a simple linear regression between the figures for two years. Out of all the variables several turn out not to be usable. For GENERAL\_MANAGE, i.e. the number of general management staff, the definition between the carriers seemed to vary considerably, so for example in 2005 Southwest Airlines reported 1809 general managers whereas US Airways reported only 12. Three other variables, OTHER\_FLT\_PERS, PASSENGER\_HANDLING and TRANSPORT\_RELATED were largely incomplete and thus we remove them as well. This leaves us with the following variables:

- **PILOTS\_COPILOTS:** Figure 72 shows the number of pilots and co-pilots employed by the companies. As Southwest did not report any employee numbers in 1998 we approximated the missing figure through a simple linear regression using the figures for 1997 and 1999.
- **TOTAL:** This variable shows the total number of employees for each company. The data for Southwest in 1998 is missing here as well so we apply the same method as for the pilots to approximate a likely amount. Figures 73 and 74 show the variable's graph before and after the conversion into quarterly data.

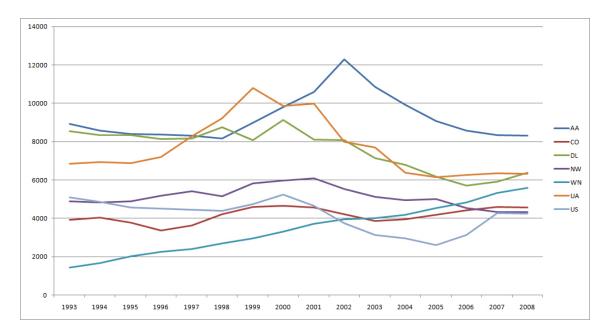


Figure 72: Number of pilots and co-pilots in the original yearly format.

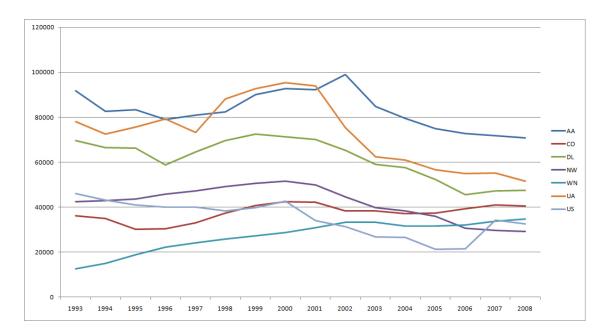


Figure 73: Total number of employees in the original yearly format.

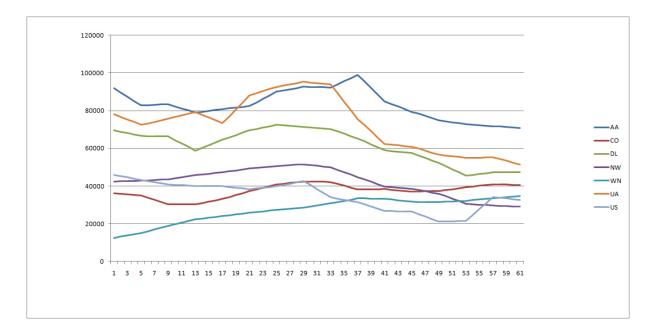


Figure 74: Total number of employees after the expansion to quarterly data through linear regression.

## 5.1.4 P-12 Table Data

Out of all the variables available in the table, we decided to download and examine the following:

- AIRCFT\_SERVICES
- DEPREC\_AMORT
- FLYING\_OPS
- GENERAL\_ADMIN
- GENERAL\_SERVICES
- INCOME\_PRE\_TAX
- INCOME\_TAX
- INTEREST\_EXP\_OTH
- INTEREST\_LONG\_DEBT
- MAINTENANCE
- NET\_INCOME
- NON\_OP\_INCOME
- OP\_EXPENSES
- OP\_PROFIT\_LOSS
- OP\_REVENUES
- PAX\_SERVICE

- PROMOTION\_SALES
- PUB\_SVC\_REVENUE
- RES\_CANCEL\_FEES
- TRANS\_REV\_PAX
- TOTAL\_MISC\_REV
- TRANS\_EXPENSES
- TRANS\_REVENUE
- UNIQUE\_CARRIER\_NAME

All variables were reported separated into operational regions. Here, only the figures of the airline as a whole are interesting, and so we combine all regions to form a single datapoint per airline and quarter for every variable.

Several of the variables can at first glance be omitted as their content is obviously largely incomplete. This leaves us with the following variables:

- AIRCFT\_SERVICES: This variable contains the airlines' expenses for aircraft and traffic servicing. The graphs in Figure 75 show a steady increase for most of the airlines most of the time. Only US Airways reports a longer period of decreasing aircraft servicing costs.
- **DEPREC\_AMORT:** Depreciation and amortization of the airlines' assets. Figure 76 shows several peaks for various airline during the sample period, the reason for which remains unclear. These peaks could result from high one-time payments (or data errors) but a validation of these peaks certainly requires further research.

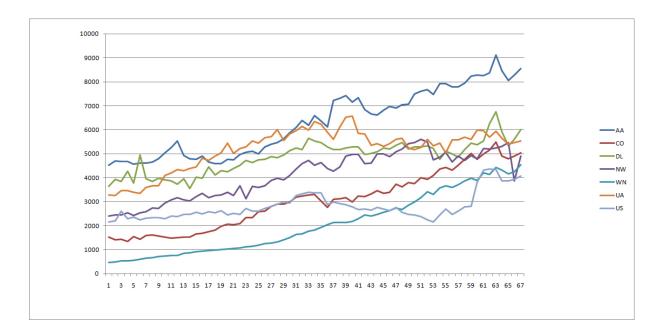


Figure 75: Aircraft and traffic servicing expenses.

- FLYING\_OPS: The airlines expenses for their flight operations are contained here. The graph in Figure 77 shows an increasing increase of operating costs which drop sharply just before our observation period ends. This is probably due to the price for fuel which had a similar development in the last years and expenses for aircraft fuel are one of the major drivers of operations costs.
- GENERAL\_ADMIN: GENERAL\_ADMIN displays general and administrative expenses. Figure 78 shows several peaks that give the impression of being rather random and further analysis would have to be carried out to determine whether the peaks are real or errors. Especially the negative values found for US Airways and Continental in quarters 35 and 42 and the zero value for US in quarter 50 must raise doubts concerning the credibility of this statistic as expenses should normally not be negative. It is therefore also unlikely that this variable will be able to explain the development of the fares in our models.

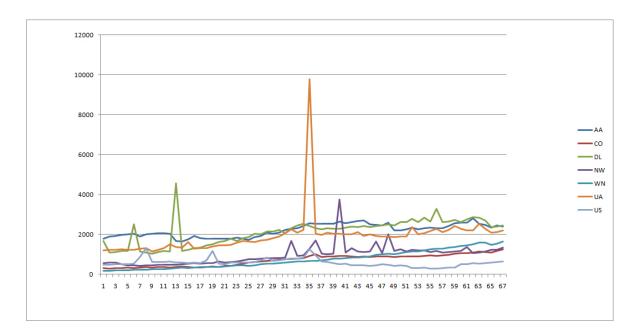


Figure 76: Expenses for depreciation and amortization.

- **GENERAL\_SERVICES:** This variable will not undergo further examination since too much data is missing to form a dataset that could be used in the models.
- INCOME\_PRE\_TAX: The income before payment of income tax is depicted in Figure 79 and the corresponding variable. As with the administrative expenses variable, this variable also shows some very strong peaks. The most notable one is the low and high peak of the United Airlines data in 2005Q4 and 2006Q1 respectively. In February 2006, United Airlines left bankruptcy protection and the peaks are likely have something to do with that event. Two other peaks that are worth noting are those of Northwest and Delta in quarter 61 which almost coincides with the announcement of the merger of the two companies. All other peaks would require further research as we were not able to find any obvious explanations.
- **INCOME\_TAX:** The INCOME\_TAX variable shows the income tax paid by the airline in the respective period. The large number of peaks in the graphs in Figure 80 and the very

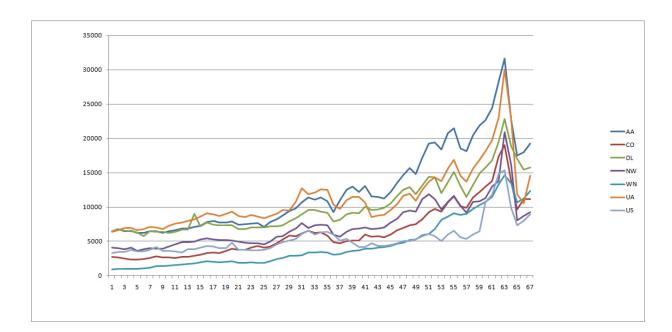


Figure 77: Flying operations expenses.

random appearance of the graphs indicate that the development of this variable will most likely not have a great explanatory effect on the fare models. Further research would be required though to identify whether the peaks are real or errors. The large number of gaps in the database for this variable will not help either.

- **INTEREST\_EXP\_OTH:** This variable (Figure 81) shows all interest expenses that are not interest expenses for long term debts. In general, if a company needs to borrow money on a short-term basis (which is usually more expensive than long term loans) this is not a good sign for the company's financial health. On the other hand, it is probably not a very important factor and thus, as with the income tax variable, due to the very high volatility of the development, explanatory power of this variable would be surprising.
- **INTEREST\_LONG\_DEBT:** Due to the expensive equipment (i.e. aircraft) needed in aviation, and due to the often low availability of cash money for purchases of aircraft, many

102

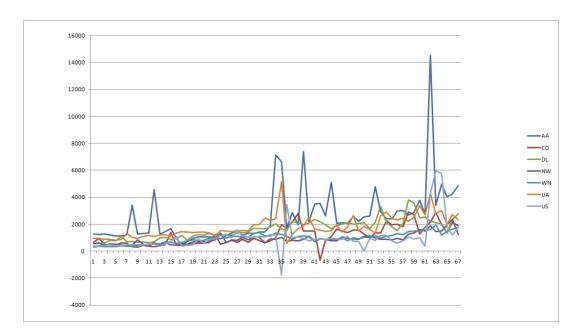


Figure 78: General and administrative expenses.

large carriers have to finance their planes through loans. Low-Cost carriers are often in a better situation and Southwest is no exception here. As one can see in Figure 82 Southwest clearly has to pay less interest than the other large carriers. The graphs feature a small number of peaks. Most of them require further research, only the US peak in quarter 55 is most probably a sign error as expenses should by definition be negative and the affected value would, multiplied by -1, fit into the graph very well.

- MAINTENANCE: This variable shows the expenses for aircraft maintenance.
- **NET\_INCOME:** The net income graph (Figure 84) features similar characteristics to the pre tax income graph and has the same peak pattern which means that the UA double peak in 2005/2006 is likely a result of the end of the Chapter 11 bankruptcy protection for the carrier and the peak of DL and NW in quarter 61 coincides with the companies' merger.

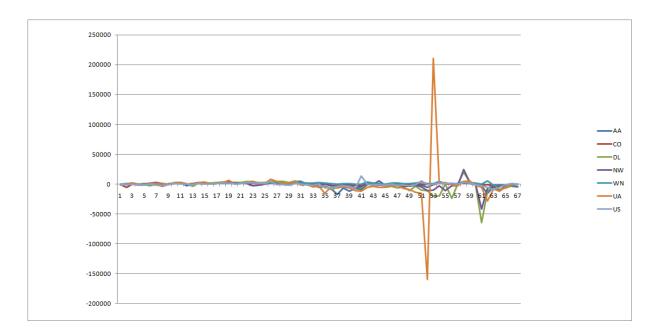


Figure 79: Income before income tax.

- NON\_OP\_INCOME: The non operating income visible in Figure 85 pretty much follows the net income and pre tax income graphs as well, which, together with the fact that the peaks do not appear in the OP\_REVENUE and OP\_PROFIT\_LOSS variables (see Figures 88 and 87), supports the hypothesis that the peaks are related to accounting issues and financial business of the airline rather than having anything to do with the airline's actual operations.
- **OP\_EXPENSES:** This variable seen in Figure 86 is similar to the graph in Figure 77, the effect of the oil price does not seem as severe, though, as in the flying operations graph because the OP\_EXPENSES variable comprises more accounts than just those that directly deal with the flight operations.
- **OP\_PROFIT\_LOSS:** The operating profit and loss graph in Figure 87 features a clear seasonal effect which is introduced through the operating revenues, i.e. the revenues that with these carriers mainly come from the passengers whose numbers underly a seasonal periodicity.

104

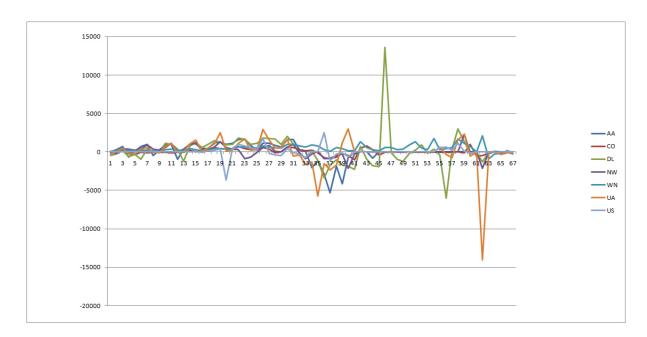


Figure 80: Income tax.

In this graph, certain effects in the airline economy like the September 11 attacks and the resulting losses and the losses due to high oil prices in 2008 are clearly visible.

- **OP\_REVENUES:** The revenues of the airlines (Figure 88) are a direct result of the number of passengers flying and the fares these passengers are paying. Of course in the year 2001 effects of the terror attacks are visible, but also the financial crisis shock which reaches its peak in early 2009, after the high peak of the operating expenses due to high fuel prices which was in 2008.
- **PAX\_SERVICE:** The airlines' expenses for passenger services seen in Figure 89 are far less volatile than other expenses, after 2001 they stayed relatively constant, despite increasing passenger numbers. The only exception is Southwest.
- **PROMOTION\_SALES:** This variable shows the amount of money spent by the airline

105

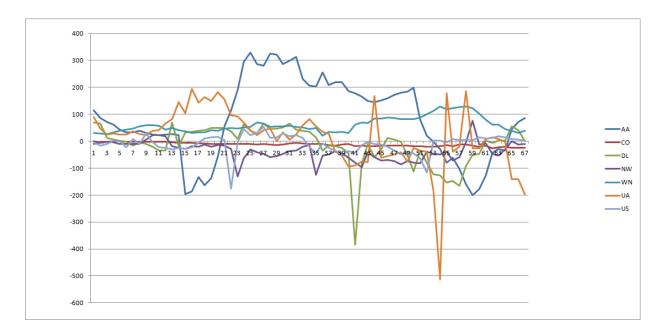


Figure 81: Other interest expense.

for promotion and sales. The graphs in Figure 90 suggest that the airlines have reduced their expenditure here in 2001, possibly due to their worsened financial situation and tighter budgets.

### • PUB\_SVC\_REVENUE, RES\_CANCEL\_FEES, TOTAL\_MISC\_REV,

**TRANS\_REV\_PAX:** These variables will not undergo further examination as too much data is missing to form a dataset that could be used in the models.

- **TRANS\_EXPENSES:** All transport related expenses are included in this variable and it is therefore not surprising that its graph in Figure 92 is quite similar to the operating and flying operations expenses.
- **TRANS\_REVENUE:** All transported related expenses are included in this variable. Only the Southwest figures seem a little small by a factor of possibly around 100, which looks like

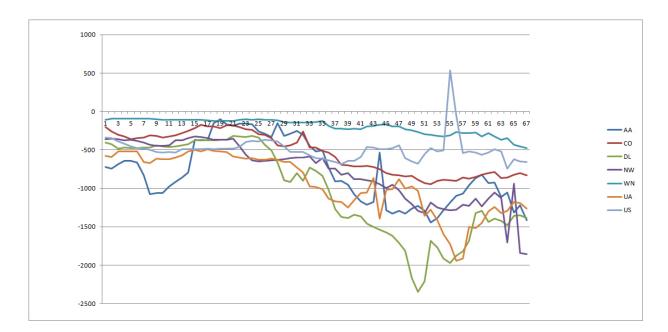


Figure 82: Interest on long-term debt and capital leases.

a reporting error. This should not have a very large effect on the models though. 2 minor corrections to the data have been made as well. Firstly, Southwest's figures for quarters 30 and 62 have been missing and were approximated through linear regression. Secondly, Delta Airlines reported a negative figure for quarter one, and as negative revenue would more or less mean that Delta paid its passengers for flying instead of getting paid, which seems unlikely, and since the absolute term of the figure fit very well to the figures in the quarter before and after we assumed that the mistake could be corrected by making the value positive.

• UNIQUE\_CARRIER\_NAME: This field identifies the airline that reported the number in the respective row of the database. In order to give every airline a unique name, numbers are added to the name should one name be used by different companies.

107

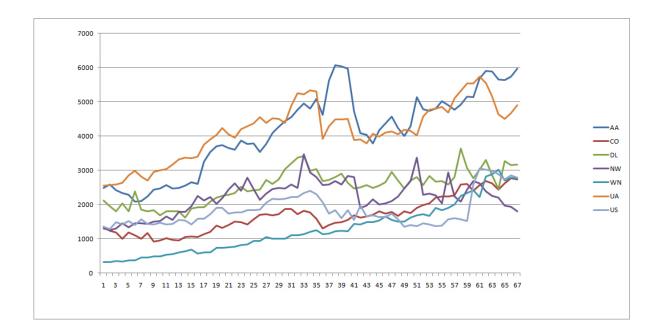


Figure 83: Aircraft maintenance.

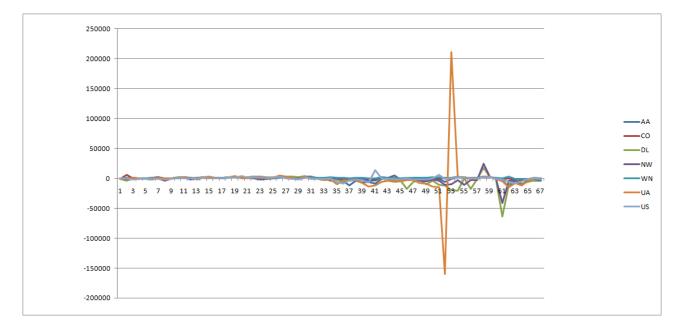


Figure 84: Net income.

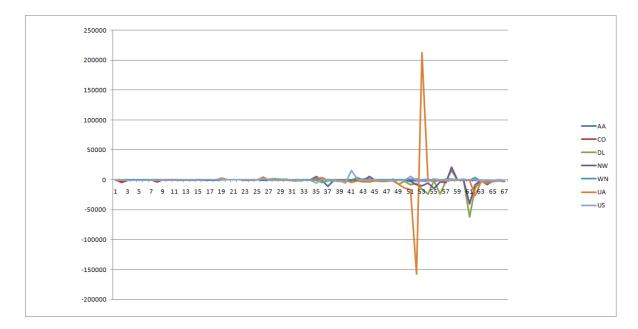


Figure 85: Nonoperating income and expenses.

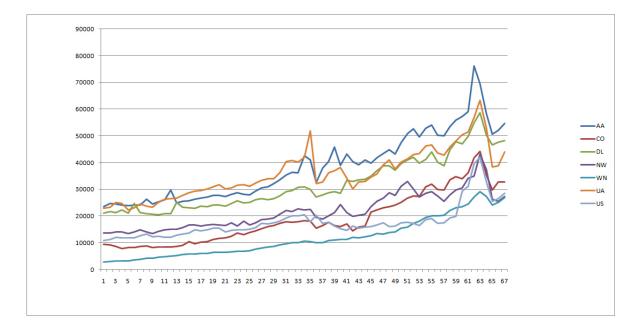


Figure 86: Total Operating Expenses.

109

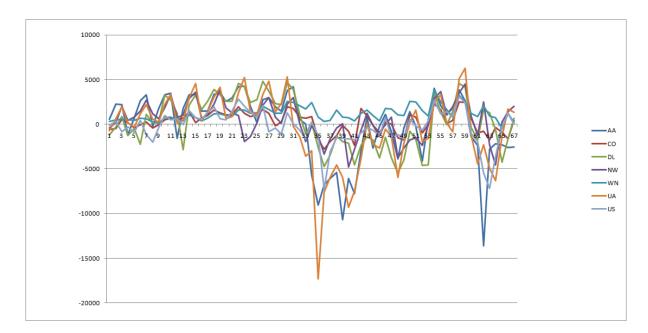


Figure 87: Operating profit or loss.

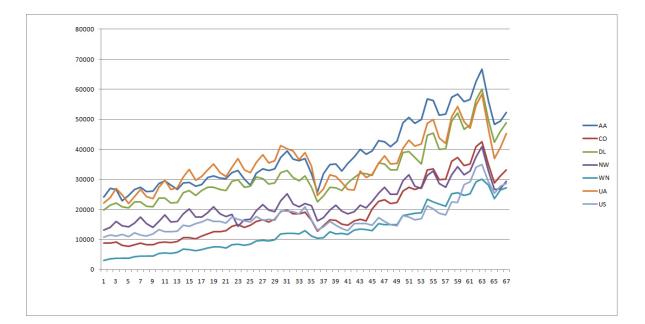


Figure 88: Total operating revenues.

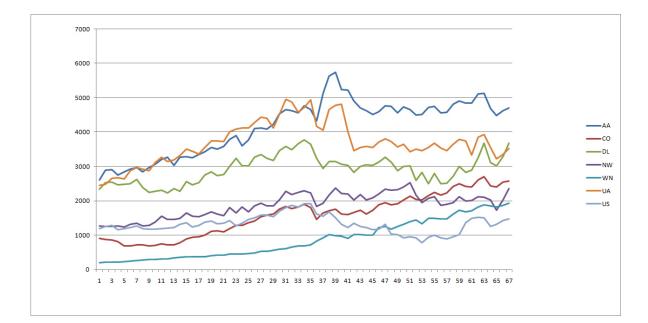


Figure 89: Passenger service.



Figure 90: Expenses for promotion and sales.

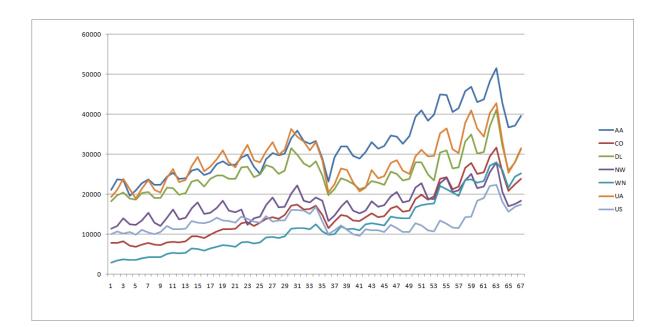


Figure 91: Passenger transport revenues.

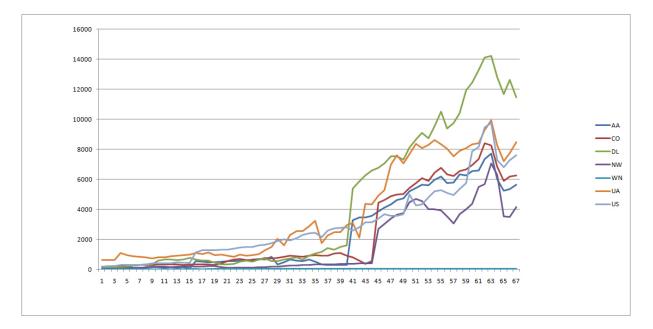


Figure 92: Transport related expenses.

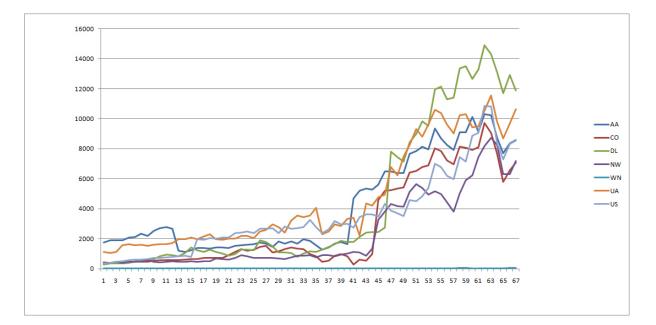


Figure 93: Transport related revenues.

### 5.1.5 P-12A Table Data

The P-12 table contains data about the airlines' total fuel consumption and their expenses for fuel. Detailed data for each airline is unfortunately only available for the years since 2000. From this database we downloaded the following four variables:

• **TDOMT\_GALLONS:** This variable shows the fuel consumption for all domestic operations of an airline in gallons. The graph in Figure 94 shows the variable's graph.

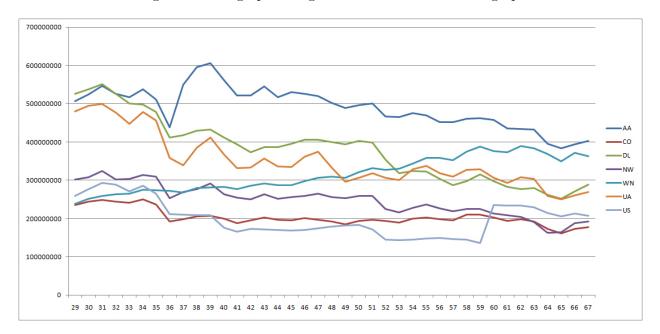


Figure 94: Domestic fuel consumption.

- **TOTAL\_GALLONS:** This variable shows the fuel consumption for all domestic operations of an airline in gallons. The graph in Figure 95 shows the variable's graph.
- **TDOMT\_COST:** This variable, graphed in Figure 96 shows the amount of money paid by each airline for its fuel used in its domestic operations. As the fuel price has a large impact on this variable, the oil price bubble in 2008 and the oil price drop in 2009 are clearly visible.

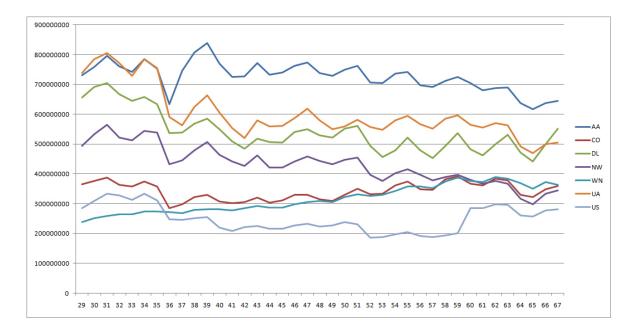


Figure 95: Total fuel consumption.

• **TOTAL\_COST:** This variable, graphed in Figure 97 shows the amount of money paid by each airline for its fuel used in its domestic operations. As the fuel price has a large impact on this variable, the oil price bubble in 2008 and the oil price drop in 2009 are clearly visible.

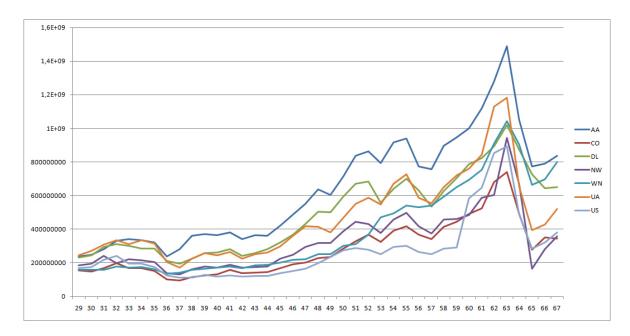


Figure 96: Domestic fuel expenses.

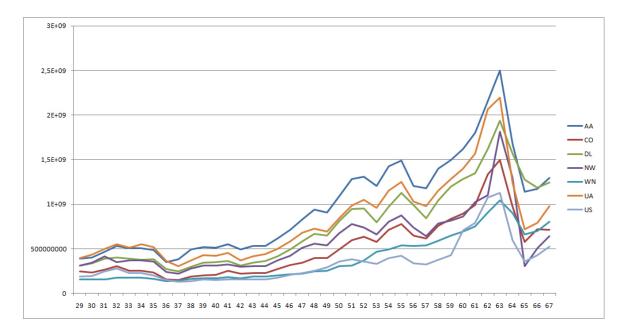


Figure 97: Total fuel expenses.

### 5.1.6 GDP

One of the most general macro economic variables we can have on the U.S. economy is the Gross Domestic Product of the country.<sup>18</sup> Consider for example the variation of the Gross Domestic Product (annual percent change) against time, between 1993 and 2008 (Figure 98). If we compare

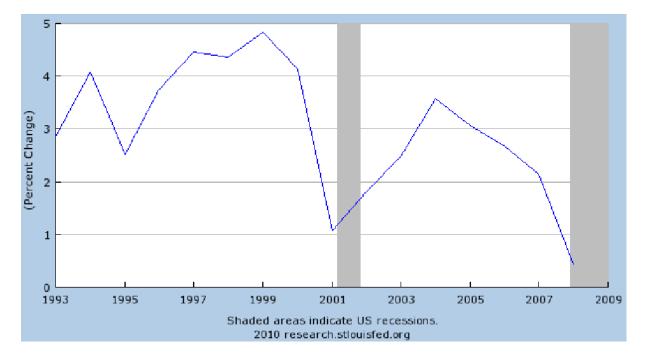


Figure 98: Real Gross Domestic Product (GDPCA) (% of annual variation against time).

this statistic with the variation of the fares of airlines over time (Figure 99), we can observe that the GDP and the airline average fares seem to be related: the same trends appear to connect the data, especially in the first periods of regression. Indeed, as the GDP statistic is the variation of the GDP from one year to another (and the GDP statistic being given at January the 1st), a spike at a given period means that the GDP had greatly increased during the year before this period. That can explain the apparent time lag between the variation of the GDP and the variation of the fares

<sup>&</sup>lt;sup>18</sup>The GDP and other macroeconomic data are available on http://research.stlouisfed.org.

for the airlines, for the first periods of regression. On the contrary, this lag seems to be reversed in 2001 and for the periods of the U.S. terrorist attacks and the actual economic crisis. We can then assume that in 2001, the drop in GDP compared to the GDP in 2000 may be explained by the bust cycle of the dot-com bubble which happened during that year. The U.S. recession we can observe in Figure 98 can then be a combination of the end of the dot-com bubble and the terrorist events of September 11. In 2007, we can also see the beginning of the financial crisis, which has become the current economic crisis where the airlines, as many other U.S. industries, have faced financial problems.

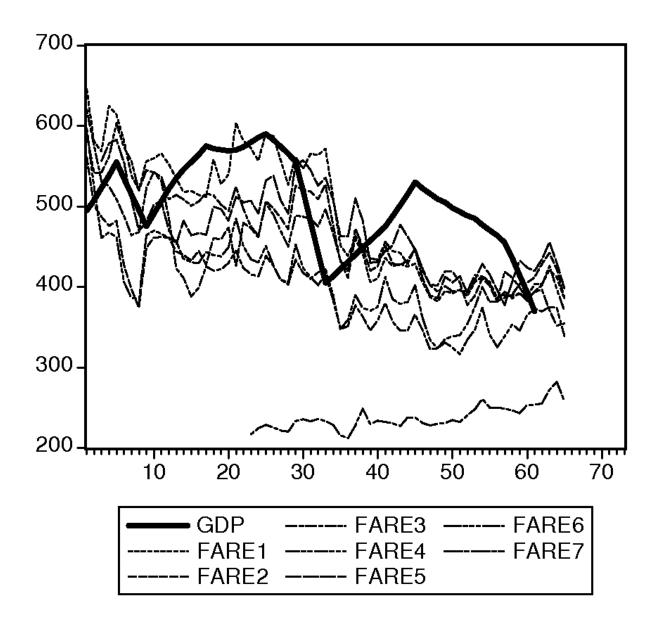


Figure 99: GDPCA (scaled to appear with the average fares of the airlines), and the quarterly average fares of the airlines (fare1 is for American, 2 is for Continental, 3 for Delta, 4 for Northwest, 5 for United, 6 for US Airways, 7 for Southwest).

#### 5.2 Insertion of economic data into ARIMA models for fares

We can notice that in our ARIMA models, the use of dummy variables or trend was a tool to proxyh macroeconomic variables in our regressions. In fact, we can assume that these 2 effects can also be found in the economic data of the carrier, such as its operational profits, revenues, expenses, the price and consumption of fuel, the net income.

If we run some regressions using our best models for average fares (as computed above) and including economic data such as the fuel, we can observe that models for the fares deteriorate: many variables become insignificant, and not necessarily the economic data. In fact, we can try to explain these results by the fact that the dummy variable or trend variable also try to take into account macroeconomic trends, thus there may be some autocorrelation between these 2 variables and the economic data we want to include.

Now if we run these regressions using our best models for fares without the dummy and trend variables, we can have interesting results. As for the ARIMA models, we decided to run all the possible regressions (using our best ARIMA model with one economic variable), and retained the best model for each carrier according to the Schwarz Information Criterion.

• American: For American Airlines, we observe that all the regressions have insignificant coefficients if we include the trend variable in the model. If not, then we can observe that the best model we can get with EViews6 is the model with no trend variable and the variable of operational expenses (Figure 100). The  $R^2$  statistic is very high for this regression (0.93), all the coefficients are individually significant, the model is stable and not autocorelated. Thus we can infer that the fare setting for American Airlines is highly correlated with the operational expenses of the carrier, which seems to be quite logical. If we consider the variable of operational revenues, transport expenses or transport revenues instead of this variable, the result is very similar and confirms this trend for the airline to determine its average fares with the operational expenses.

Dependent Variable: FARE1 Method: Least Squares Date: 01/24/10 Time: 22:49 Sample (adjusted): 1 65 Included observations: 65 after adjustments Convergence achieved after 12 iterations Backcast: -1 0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO1_13 C	-0.00 <b>17</b> 09 600. <b>4467</b>	0.0005 <b>7</b> 9 19.10238	-2.949296 31.43309	0.00 <b>45</b> 0.0000
DUMMY	-106.8731	15.57458	-6.862022	0.0000
MA(1)	0.896658	0.089225	10.04943	0.0000
MA(2)	0.385501	0.084943	4.538349	0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.934951 0.930615 21.19818 26961.77 -288.1341 2.239931	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent <b>v</b> ar criterion terion	488.0287 80.47577 9.019511 9.186772 215.5967 0.000000
Inverted MA Roots	45+.43i	4543i		

Figure 100: American Airlines - regression on quarterly average fares. ecol\_13 stands for the variable of Operational Expenses.

• **Continental:** For Continental Airlines, EViews6 gives as the best regression for fares (Figure 101) the model which includes the variable of the total number of employees in the airline! It appears to be quite unlikely that the average fares of an airline can be connected to the total number of employees. However, we could imagine that if the number of employees increases, it is an additional expense for the airline, and as these new employees may improve the quality of the service offered to the passenger, this latter would consequently be less reluctant to pay more if there are more people taking care of him during his travel!

If we do not include the dummy variable in our regression, then we get the variable of transport expenses as the best variable explaining the data of fares for the carrier (Figure 102). As for Continental Airlines, we can observe that the sign of the economic coefficient is negative, which would mean that the greater the transport expenses are, the lower the fares

Dependent Variable: FARE2 Method: Least Squares Date: 01/24/10 Time: 23:09 Sample (adjusted): 1 61 Included observations: 61 after adjustments Convergence achieved after 11 iterations Backcast: -1 0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO2_21 C DUMMY MA(1) MA(2)	0.004463 303.7066 -61.54282 0.889295 0.513502	0.001923 70.70151 13.52376 0.080480 0.088953	2.320354 4.295617 -4.550719 11.04982 5.772743	0.0240 0.0001 0.0000 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.756709 0.739331 21.62428 26186.14 -271.4497 2.405410	Mean deper S.D. depend Akaike info Schwarz crit F-statistic Prob(F-stati	dent <b>v</b> ar criterion terion	446.2246 42.35422 9.063923 9.236946 43.54417 0.000000
Inverted MA Roots	4456i	44+.56i		

Figure 101: Continental Airlines - regression on quarterly average fares. eco2\_21 stands for the variable of the total number of employees.

become. The sign does not change if we include the transport revenues variable instead of the first one (as the transport expenses and revenues will not be so different for given airline). Indeed, we can assume that the transport revenues or expenses are a sign of the strength and development of the airline, and a larger airline (in terms of demand) will maybe have more ability to set lower fares than a startup company.

• Delta: For Delta Air Lines, the best model we get is the model with the variable of Passenger Services (Figure 103). This variable is indeed similar to the variable Operational Expenses, as the cost of the passenger services is a component of the operational expenses. So the sign of the coefficient for this regression (negative) is coherent with the above explanations for the model of Continental Airlines. Here again, the  $R^2$  statistic (0.91) is very high, and our regression consequently seems to explain a important part of the fares.

Dependent Variable: FARE2 Method: Least Squares Date: 01/24/10 Time: 23:10 Sample (adjusted): 1 65 Included observations: 65 after adjustments Convergence achieved after 11 iterations Backcast: -1 0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO2_24	-0.00 <b>732</b> 0	0.002468	-2.966053	0.00 <b>43</b>
C	459.3858	9.377713	48.98698	0.0000
MA(1)	0.927830	0.076417	12.14171	0.0000
MA(2)	0.550311	0.083340	6.603195	0.0000
R-squared	0.706116	Mean dependent var		444.5904
Adjusted R-squared	0.691663	S.D. dependent var		41.83435
S.E. of regression	23.22983	Akaike into criterion		9.188315
Sum squared resid	32917.12	Schwarz criterion		9.322123
Log likelihood	-294.6202	F-statistic		48.85500
Durbin-Watson stat	2.174646	Prob(F-statistic)		0.000000
Inverted MA Roots	4658i	46+.58i		

Figure 102: Continental Airlines - regression on quarterly average fares. eco2\_24 stands for the variable of Transport Expenses.

• Northwest: For Northwest, we get very different behaviour than for the other airlines, as we can observe that it is difficult to find a reliable and coherent model for the fares if we do not include the trend variable in the regression. This may be explained by the difficulties of the airline and the fact that it has recently been forced to merge with Delta Air Lines.

If we consider the entire model with the trend variable, EViews6 gives the model with the Flying Operations as the best regression (Figure 104). All the coefficients are here again significant at the 95% level, and the regression explains more than 96% of the fare data according to the  $R^2$  statistic.

• United: For United Airlines, again the best economic variable we may include in the regression seems to be the Passenger Services. The sign of the coefficient is negative as we found for the regression for Delta, and the coefficient of determination  $R^2$  is equal to 0.83.

Dependent Variable: FARE3 Method: Least Squares Date: 01/24/10 Time: 23:46 Sample (adjusted): 2 65 Included observations: 64 after adjustments Convergence achieved after 18 iterations
Convergence achieved after 18 iterations Backcast: 1

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO3_16	-0.022901	0.010847	-2.111201	0.0389
С	457.4865	37.22225	12.29067	0.0000
<b>A</b> R(1)	0.820283	0.055311	14.83029	0.0000
MA(1)	0.416047	0.123755	3.361849	0.0014
R-squared	0.908452	Mean dependent var		408.5544
Adjusted R-squared	0.903874	S.D. dependent var		58.40192
S.E. of regression	18.10701	Akaike info criterion		8.690937
Sum squared resid	19671.82	Schwarz criterion		8.825867
Log likelihood	-274.1100	F-statistic		198.4642
Durbin-Watson stat	1.979693	Prob(F-stati	stic)	0.000000
Inverted AR Roots	.82			

Inverted MA Roots -.42

Figure 103: Delta Air Lines - regression on quarterly average fares. eco3\_16 stands for the variable of Passenger Services.

- US Airways: The best model we find is a regression with the variable of the Transport Expenses, as for Continental and American Airlines (for the latter it is the Operational Expenses). We can check that the coefficient is negative as for the 2 other airlines, and the model explains almost 87% of the data on fares for the airline.
- Southwest: Finally, for the low-cost airline, we found as the best economic variable the Transport Revenue variable. Nevertheless, we can notice that here the sign for the economic coefficient is positive, which is contrary to the sign we expected for the other airlines (as we stressed that the variable of revenues and expenses are quite similar here). In fact we can try to explain this positive sign by the traditional strategy of a low-cost airline. For a traditional

Dependent Variable: FARE4 Method: Least Squares Date: 01/25/10 Time: 00:12 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 21 iterations Backcast: 2 4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO4_4	0.002982	0.0010 <b>77</b>	2.769215	0.00 <b>78</b>
С	548.7059	7.776075	70.56334	0.0000
@TREND	-3.300531	0.241603	-13.66098	0.0000
<b>A</b> R(1)	-0.544158	0.135673	-4.010819	0.0002
AR(2)	-0.452372	0.134231	-3.370111	0.0014
<b>A</b> R(3)	-0.424567	0.129552	-3.277199	0.0019
AR(4)	0.431459	0.128378	3.360859	0.0015
MA(1)	1.449148	0.081450	17.79187	0.0000
MA(2)	1.338471	0.110766	12.08383	0.0000
MA(3)	0.860623	0.066376	12.96582	0.0000
R-squared	0.966290	Mean dependent var		459.6851
Adjusted R-squared	0.960342	S.D. depend	ent var	55.37599
S.E. of regression	11.02780	Akaike info d	riterion	7.787536
Sum squared resid	6202.225	Schwarz criterion		8.133580
Log li <b>ke</b> lihood	-227.5198	F-statistic		162.4359
Durbin-Watson stat	1.963799	Prob(F-statis	stic)	0.000000
Inverted AR Roots Inverted MA Roots	.49 - 23- 91i	02+.95i - 23+.91i	0295i 98	98

Figure 104: Northwest Airlines - regression on quarterly average fares. eco4\_4 stands for the variable of Flying Operations.

airline, an increase in operational revenue strengthens the airline, which can then lower its fares and attract more passengers, maybe in order to catch a part of the passengers of the low-cost airlines. On the other hand, the well-known strategy of a low-cost airline is to charge the passenger for any additional service he wants to get. Thus we can assume that an increase in the operational expenses/revenues causes/is caused by an increase of the passenger fares (that is to say, an increase of the passenger service).

Dependent Variable: FARE5 Method: Least Squares Date: 01/25/10 Time: 00:31 Sample (adjusted): 3 65 Included observations: 63 after adjustments Convergence achieved after 10 iterations Backcast: 1 2

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO5_16 C MA(1) MA(2)	-0.070699 529.8724 1.040072 0.541555	0.013389 13.79505 0.108339 0.107949	-5.280222 38.41031 9.600208 5.016770	0.0000 0.0000 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.833793 0.825341 21.90586 28312.13 -281.7923 1.932181	Mean deper S.D. depend Akaike info Schwarz crit F-statistic Prob(F-stati	dent var criterion terion	470.2444 52.41618 9.072772 9.208844 98.65945 0.000000
Inverted MA Roots	52+.52i	5252i		

Figure 105: United Airlines - regression on quarterly average fares.  $eco5_16$  stands for the variable of Passenger Services.

Dependent Variable: FARE6 Method: Least Squares Date: 01/25/10 Time: 00:27 Sample (adjusted): 1.65 Included observations: 65 after adjustments Convergence achieved after 10 iterations Backcast: -1.0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO6_24	-0.010046	0.001929	-5.207162	0.0000
C	434.0422	9.626895	45.08642	0.0000
MA(1)	0.989819	0.068762	14.39478	0.0000
MA(2)	0.603541	0.051846	11.64096	0.0000
R-squared	0.867096	Mean dependent var		402.6931
Adjusted R-squared	0.860560	S.D. dependent var		53.94896
S.E. of regression	20.14545	Akaike info criterion		8.903398
Sum squared resid	24756.20	Schwarz criterion		9.037206
Log likelihood	-285.3604	F-statistic		132.6594
Durbin-Watson stat	2.190492	Prob(F-statistic)		0.000000
Inverted MA Roots	49+.60i	4960i		

Figure 106: US Airways - regression on quarterly average fares. eco6\_24 stands for the variable of Transport Expenses.

Dependent Variable: FARE7 Method: Least Squares Date: 01/25/10 Time: 00:28 Sample (adjusted): 23 65 Included observations: 43 after adjustments Convergence achieved after 42 iterations Backcast: 20 22

Variable	Coefficient	Std. Error	t-Statistic	Prob.
ECO7_26 C MA(1) MA(2) MA(3)	0.004920 215.2520 0.412661 -0.543348 -0.732100	0.000219 1.037382 0.093590 0.106619 0.111419	22.49275 207.4954 4.409263 -5.096145 -6.570674	0.0000 0.0000 0.0001 0.0000 0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.851341 0.835693 5.934298 1338.204 -134.9288 1.994172	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent var criterion terion	237.7842 14.63999 6.508319 6.713109 54.40465 0.000000
Inverted MA Roots	.96	68+.55i	6855i	

Figure 107: Southwest Airlines - regression on quarterly average fares.  $eco7_26$  stands for the variable of Transport Revenue.

## 6 Regressions for specific routes

It is interesting to see whether our "global" models for average fares and passengers for the entire domestic network in the U.S. could be used for specific round trips that are proposed by the 7 carriers examined in this project.

We can infer that on a specific route in the U.S. domestic market, the fares proposed by the airline would depend upon the competition between these airlines, the characterics of the route (distance, population data, airport data,...). In this section we want to assess how well a simple ARIMA model can work for a "given" route.

### 6.1 Chicago (ORD) - Atlanta (ATL)

The airports of Chicago O'Hare International (IATA airport code ORD) and Hartsfield-Jackson Atlanta International (IATA airport code ATL) were, in 2008, the 2 biggest airports in the U.S. in terms of enplanements. Indeed, we can assume that if we choose big airports, we will be able to get more general data, and not be stopped with specific characteristics we could have in smaller airports. We can also assume that the concentration of the market may be lower in these big airports.

We observe that the route between these 2 airports is only served by 3 carriers among the 7 airlines we study: American Airlines, Delta Air Lines, and United Airlines (see Figure 108). The other airlines may also propose some flights between Chicago O'Hare and Hatrsfield-Jackson Atlanta, but either they use code-sharing to do these flights, or they have not reported these flights to the DOT. We try to apply our best models (according to Section 4) to these average fares. We get the following regression outputs for the 3 carriers (Figures 109 to 111): we observe that these models do not seem to be the best regressions we can get to fit the fares between the 2 airports. The ARMA component of the model seems to be good, but the coefficients of trend or the dummy variable are insignificant for all regressions, according to the Student's t-statistics. As we said, this

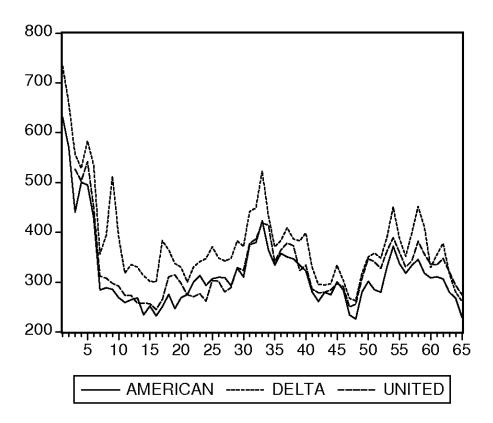


Figure 108: Quarterly average fares between Chicago (ORD) and Atlanta (ATL) (\$ against time).

does not necessarily mean that our models are bad, but they seems to be too global to be able to capture the specificity of this particular route.

We may also assume that these global trends for the fares to decrease for these carriers, as well as the dummy variable modeling the impacts of September 11, 2001, may have been less important for the behaviour of the airlines between Chicago and Atlanta than between other U.S. cities such as New-York.

If we run the regressions for our best models for the number of passengers, we get the following results (Figures 112 to 114): curiously, as our models for these statistics on passengers appeared to be less accurate and precise than the best global regressions for average fares, we can see that these

Method: Least Squa Date: 01/22/10 Tim Sample: 1 65 Included observation Convergence achiev Backcast: -1 0	ne: 19:14 ns: 65	ations	
Variable	Coefficient	Std. Error	t-Statistic
C DU <b>MMY</b> @TREND	344.6375 33.72505 -1.538010	24.36217 33.68619 0.9 <b>7</b> 6840	14.14642 1.001154 -1.574476

Dependent Variable: AMERICAN

0.3208 .001154 0.1206 .574476 MA(1) 1.027928 0.067404 15.25027 0.0000 0.057092 MA(2)0.702527 12.30515 0.0000 R-sauared 0.827813 Mean dependent var 318.8659 Adjusted R-squared 0.816333 S.D. dependent var 76.34632 S.E. of regression 32.71923 Akaike info criterion 9.887607 Sum squared resid 64232.89 Schwarz criterion 10.05487 Log likelihood -316.3472 F-statistic 72.11440 Durbin-Watson stat 1.670324 Prob(F-statistic) 0.000000 Inverted MA Roots -.51-.66i -.51+.66i

Figure 109: American Airlines - regression on quarterly average fares.

models for American Airlines and for United Airlines are quite good. For the model for American Airlines, the model is stationary, all the coefficients are individually and jointly significant, the Durbin Watson statistic is quite low but there is no spike in the correlograms, the  $R^2$  statistic is even higher than the coefficient of determination we have for the global regression (0.65 here against 0.62 for the regression on all passengers data).

For United Airlines, as we reject the dummy variable for the regression on fares, this coefficient is not very significant for our regression (but it remains significant at the 88% level of confidence, which is better than for the model for the average fares). All the other coefficients are individually significant at the 95% level of confidence.

For Delta Air Lines, our model does not seem to be the best one for the statistic on passengers for the airline. In fact, we can notice that in our regression on the number of passengers for Delta Air Lines, we did not consider any seasonality effect for the airline in our best model according

Prob.

0.0000

Dependent Variable: DELTA Method: Least Squares Date: 01/22/10 Time: 19:16 Sample (adjusted): 2 65 Included observations: 64 after adjustments Convergence achieved after 13 iterations Backcast: 1

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	409.8577	40.40135	10.14465	0.0000
@TREND	-1.302440	1.032429	-1.261530	0.2120
AR(1)	0.557524	0.110048	5.066178	0.0000
MA(1)	0.495031	0.130422	3.795600	0.0003
R-squared	0.698170	Mean dependent var		375.3657
Adjusted R-squared	0.683078	S.D. dependent var		79.70510
S.E. of regression	44.87062	Akaike info criterion		10.50591
Sum squared resid	120802.3	Schwarz criterion		10.64084
Log likelihood	-332.1890	F-statistic		46.26243
Durbin-Watson stat	2.212073	Prob(F-statistic)		0.000000
Inverted AR Roots	.56			

Inverted MA Roots -.50

Figure 110: Delta Air Lines - regression on quarterly average fares.

to the SIC. Here we can see that the coefficients AR(1) and AR(2) do not seem to be significant, but this result could also mean that the data would better fit a seasonal autoregressive component rather than individual AR variables. In fact, if we try to find the best model for the number of passengers of Delta between these airports, we find with EViews6 an ARMA(2,1), with a seasonal variable SAR(4) and a trend variable (see Figure 115). This result seems to be quite a good model, except for the invertibility of the regression. All coefficients are significant, the Durbin-Watson statistic is higher than 2, there is no sign of autocorrelation in the correlograms, the model is stationary, and the  $R^2$  statistic is very high (0.90). As a consequence, we can confirm that the seasonality of the number of passengers really matters in the models for the number of passengers.

Dependent Variable: UNITED Method: Least Squares Date: 01/22/10 Time: 19:20 Sample (adjusted): 3 65 Included observations: 63 after adjustments Convergence achieved after 17 iterations Backcast: 1 2

Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	316.6032	14.44881	21.91207	0.0000
DUMMY	11.70167	19.96145	0.586214	0.5600
MA(1)	1.075850	0.0600 <b>7</b> 5	17.90849	0.0000
MA(2)	0. <b>44354</b> 6	0.0 <b>77294</b>	5.738405	0.0000
R-squared	0.741212	Mean dependent var		326.8441
Adjusted R-squared	0.728054	S.D. dependent var		63.47751
S.E. of regression	33.10256	Akaike info criterion		9.898485
Sum squared resid	64650.98	Schwarz crit	erion	10.03456
Log likelihood	-307.8023	F-statistic		56.32870
Durbin-Watson stat	1.695740	Prob(F-statis	stic)	0.000000
Inverted MA Roots	5439i	54+.39i		

Figure 111: United Airlines - regression on quarterly average fares.

Dependent Variable: PAX1\_R Method: Least Squares Date: 01/22/10 Time: 20:45 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 11 iterations Backcast: 3 4

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C AR(4) MA(1) MA(2)	1625.691 0.494290 0.684753 0.468036	186.7098 0.134612 0.124421 0.128473	8.707048 3.671966 5.503531 3.643073	0.0000 0.0005 0.0000 0.0006
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.652094 0.633783 342.1839 6674119. -440.4429 1.778421	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion F-statistic Prob(F-statistic)		1633.131 565.4451 14.57190 14.71032 35.61247 0.000000
Inverted AR Roots Inverted MA Roots	.84 3459i	.0084i 34+.59i	00+. <b>84</b> i	84

Figure 112: American Airlines - regression on the number of passengers per quarter.

Dependent Variable: PAX3\_R Method: Least Squares Date: 01/22/10 Time: 20:50 Sample (adjusted): 4 65 Included observations: 62 after adjustments Convergence achieved after 9 iterations

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C DU <b>MMY</b> AR(1) AR(2) AR(3)	4922.134 -1984.482 0.428583 0.153651 0.216699	665.2754 691.7610 0.136457 0.146554 0.133430	7.398640 -2.868739 3.140799 1.048425 1.624071	0.0000 0.0058 0.0027 0.2989 0.1099
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.695189 0.673799 807.3718 37155410 -500.3822 2.183800	Mean depen S.D. depend Akaike info Schwarz crit F-statistic Prob(F-stati	lent var criterion erion	3897.839 1413.615 16.30265 16.47420 32.50033 0.000000
Inverted AR Roots	.88	23+.44i	2344i	

Figure 113: Delta Air Lines - regression on the number of passengers per quarter.

Dependent Variable: PAX5\_R Method: Least Squares Date: 01/22/10 Time: 20:49 Sample (adjusted): 7 65 Included observations: 59 after adjustments Convergence achieved after 23 iterations Backcast: 5 6

Variable	Coefficient	Std. Error	t-Statistic	Prob.
с	3783.720	315.7964	11.98152	0.0000
DUMMY	-515.8166	319.3217	-1.615351	0.1122
@TREND	-33.90916	11.05596	-3.067047	0.00 <b>34</b>
AR(4)	0.281860	0.100272	2.810952	0.0069
MA(1)	0.271190	0.135097	2.007367	0.0498
MA(2)	0.296377	0.134230	2.207978	0.0316
R-squared	0.841305	Mean dependent var		2287.169
Adjusted R-squared	0.826334	S.D. dependent var		856.7830
S.E. of regression	357.0496	Akaike info	criterion	14.68977
Sum squared resid	6756676.	Schwarz criterion		14.90105
Log likelihood	-427.3482	F-statistic		56.19477
Durbin-Watson stat	1.849356	Prob(F-statistic)		0.000000
Inverted AR Roots	.73	.00 <b>73</b> i		
Inverted MA Roots	1453i	14+.53i		

Figure 114: United Airlines - regression on the number of passengers per quarter.

Dependent Variable: PAX3\_R Method: Least Squares Date: 01/22/10 Time: 21:15 Sample (adjusted): 7 65 Included observations: 59 after adjustments Convergence achieved after 67 iterations Backcast: OFF (Roots of MA process too large)

Variable	Coefficient	Std. Error	t-Statistic	Prob.
с	9766.443	3413.447	2.861168	0.0060
@TREND	-129.5204	61.88975	-2.092760	0.0412
<b>A</b> R(1)	1.659360	0.110624	15.00001	0.0000
AR(2)	-0.721732	0.106080	-6.803671	0.0000
SAR(4)	0.754986	0.085112	8.870495	0.0000
MA(1)	-1.192886	0.151067	-7.896419	0.0000
R-squared	0.903605	Mean dependent var		3937.305
Adjusted R-squared	0.894511	S.D. dependent var		1436.651
S.E. of regression	466.6113	Akaike info	15.22501	
Sum squared resid	11539481	Schwarz cri	15.43629	
Log likelihood	-443.1379	F-statistic	99.36384	
Durbin-Watson stat	2.202642	Prob(F-stati	0.000000	
Inverted AR Roots	.93 .00+.93i	.83+.18i 93	.8318i	.009 <b>3i</b>
Inverted MA Roots	1.19			
	Estimated N	MA process is	noninvertible	e

Figure 115: Delta Air Lines - regression on the number of passengers per quarter.

# 6.2 Los Angeles (LAX) - New-York (JFK)

We now consider 2 other big airports, Los Angeles International (IATA airpot code LAX) and John F Kennedy International (IATA airport code JFK), in Los Angeles and New-York respectively. The same airlines as for the previous route are competing between these 2 airports (see Figure 116). If

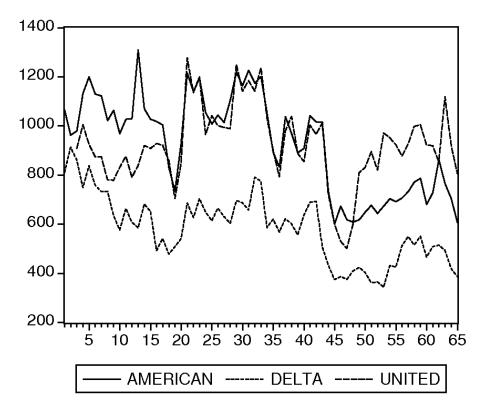


Figure 116: Quarterly average fares between Los Angeles (LAX) and New-York (JFK) (\$ against time).

we run the same regressions as for the previous route for the fares of the 3 airlines (Figure 117 to 119), we can then observe that the conclusions are not the same as for the previous route: we can observe that all the coefficients are significant for the regression of United. For Delta Airlines, the trend variable also seems to be significant, as the dummy variable is for American Airlines. The model for United even seems to be a good one, but the low  $R^2$  statistic may be a sign that this

ARMA model does not explain all the variations of the data.

Dependent Variable: FARE1 Method: Least Squares Date: 01/22/10 Time: 22:05 Sample: 1.65 Included observations: 65 Convergence achieved after 11 iterations Backcast: -1.0

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C @TREND DUMMY MA(1) MA(2)	1111.544 -2.668128 -216.1821 0.767416 0.423425	58.38891 2.547093 92.76353 0.116795 0.116223	19.03691 -1.047519 -2.330465 6.570635 3.643226	0.0000 0.2991 0.0232 0.0000 0.0006
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.779936 0.765265 96.16759 554892.3 -386.4256 1.927842	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent var criterion terion	927.1746 198.4905 12.04387 12.21113 53.16198 0.000000
Inverted MA Roots	38+.53i	3853i		

Figure 117: American Airlines - regression on quarterly average fares.

For the regressions on the number of passengers (Figure 120 to 122), the results are also different from the previous conclusions. We get quite a good model for American Airlines, as all the coefficients of the regression are significant. There is no problem of stationarity or autocorrelation, and the coefficient of determination  $R^2$  is also higher than for the global regression on passengers (0.70 here). For Delta Airlines, again we may infer that the seasonality of the number of passengers is the cause of the rejection of the variable AR(2) and AR(3), and the model is consequently not as good as the global regression. On the contrary, for United Airlines, the model seems to reject the seasonality of the number of passengers, whereas we kept this variable for the route between Chicago and Atlanta. Again it stresses the importance of taking into account local effects and the characteristics of the routes in order to better fit the data we have from our databases. Here we notice that the dummy variable seems to be important in the regression, whereas this coefficient

Dependent Variable: FARE3 Method: Least Squares Date: 01/22/10 Time: 22:06 Sample (adjusted): 2.65 Included observations: 64 after adjustments Convergence achieved after 8 iterations Backcast: 1

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	732.4027	70.37203	10.40758	0.0000
@TREND	-4.901531	1.745794	-2.807623	0.0067
AR(1)	0.760075	0.113175	6.715953	0.0000
MA(1)	-0.077398	0.175711	-0.440488	0.6612
R-squared	0.767188	Mean dependent var		579.0942
Adjusted R-squared	0.755548	S.D. dependent var		134.5663
S.E. of regression	66.53241	Akaike info criterion		11.29372
Sum squared resid	265593.7	Schwarz criterion		11.42865
Log likelihood	-357.3989	F-statistic		65.90636
Durbin-Watson stat	1.914511	Prob(F-statistic)		0.000000
Inverted AR Roots Inverted MA Roots	.76 .08			

Figure 118: Delta Air Lines - regression on quarterly average fares.

was not significant on the first route studied.

Dependent Variable: FARE5 Method: Least Squares Date: 01/22/10 Time: 22:04 Sample (adjusted): 3 65 Included observations: 63 after adjustments Convergence achieved after 11 iterations Backcast: 1 2

Variable	Coefficient	Std. Error	t-Statistic	Prob.
с	979.1359	43.94639	22.28023	0.0000
DUMMY	-123.4689	61.24552	-2.015966	0.0484
MA(1)	0.737380	0.106797	6.904489	0.0000
MA(2)	0.526463	0.114141	4.612393	0.0000
R-squared	0.522884	Mean deper	ndent var	922.2468
Adjusted R-squared	0.498624	S.D. depend	dent var	158.1343
S.E. of regression	111.9716	Akaike info	criterion	12.33575
Sum squared resid	739721.0	Schwarz crit	terion	12.47183
Log likelihood	-384.5763	F-statistic		21.55320
Durbin-Watson stat	1.941271	Prob(F-stati	stic)	0.000000
Barbin Matoon olar				
Inverted MA Roots	- 37+.62i	3762i		

Figure 119: United Airlines - regression on quarterly average fares.

Dependent Variable: FARE1 Method: Least Squares Date: 01/22/10 Time: 22:22 Sample (adjusted): 5 65 Included observations: 61 after adjustments Convergence achieved after 69 iterations Backcast: 3 4

Coefficient	Std. Error	t-Statistic	Prob.
900 0526			
2000000	52.20771 17.23984		0.0000
0.383516	0.137257	2.794135	0.0071
0.693463	0.124630	5.564155	0.0000
0.494549	0.118599	4.169912	0.0001
0.699325	Mean dependent var		920.1204
0.683500	S.D. dependent var		202.2118
113.7610	Akaike info criterion		12.36940
737669.6	Schwarz criterion		12.50782
-373.2668	F-statistic		44.19113
1.601820	Prob(F-statistic)		0.000000
.79 - 35- 61i		00 <b>7</b> 9i	79
	0.693463 0.494549 0.699325 0.683500 113.7610 737669.6 -373.2668 1.601820	0.693463         0.124630           0.494549         0.118599           0.699325         Mean depender           0.683500         S.D. depender           113.7610         Akaike inford           737669.6         Schwarz criter           -373.2668         F-statistic           1.601820         Prob(F-statistic)           .79        00+.79i	0.693463         0.124630         5.564155           0.494549         0.118599         4.169912           0.699325         Mean dependent var           0.683500         S.D. dependent var           113.7610         Akaike info criterion           737669.6         Schwarz criterion           -373.2668         F-statistic           1.601820         Prob(F-statistic)           .79        00+.79i        0079i

Figure 120: American Airlines - regression on the number of passengers per quarter.

Dependent Variable: FARE3 Method: Least Squares Date: 01/22/10 Time: 22:23 Sample (adjusted): 4 65 Included observations: 62 after adjustments Convergence achieved after 10 iterations

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C DU <b>MMY</b> AR(1) AR(2) AR(3)	611.6708 -123.8819 0.695335 -0.052021 0.092662	45.20144 53.73269 0.132409 0.160163 0.126210	13.53211 -2.305521 5.251425 -0.324799 0.734190	0.0000 0.0248 0.0000 0.7465 0.4658
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.737159 0.718714 65.94297 247863.1 -345.0726 1.941385	Mean deper S.D. depend Akaike info Schwarz cri F-statistic Prob(F-stati	dent <b>v</b> ar criterion terion	569.1426 124.3354 11.29266 11.46421 39.96534 0.000000
Inverted AR Roots	.78	04+.34i	0434i	

Figure 121: Delta Air Lines - regression on the number of passengers per quarter.

Dependent Variable: FARE5 Method: Least Squares Date: 01/22/10 Time: 22:26 Sample (adjusted): 7 65 Included observations: 59 after adjustments Convergence achieved after 11 iterations Backcast: 5 6

Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	851.7924	92.43592	9.214950	0.0000
DUMMY	-293.7036	115.3611	-2.545951	0.0138
@TREND	6. <b>147</b> 600	3.574554	1.719823	0.0913
AR(4)	0.057623	0.151746	0.379733	0.7057
MA(1)	0.713245	0.128705	5.541704	0.0000
MA(2)	0.511023	0.130599	3.912911	0.0003
R-squared	0.562606	Mean deper	ndent var	921.8376
Adjusted R-squared	0.521343	S.D. depend	lent var	163.0129
S.E. of regression	112.7806	Akaike info	Akaike info criterion	
Sum squared resid	674131.4	Schwarz criterion		12.59618
Log likelihood	-359.3548	F-statistic		13.63447
1	-359.3548 1.9 <b>7</b> 5700	F-statistic Prob(F-stati		
Log li <b>ke</b> lihood		Prob(F-stati		13.63447
Log likelihood Durbin-Watson stat	1.975700	Prob(F-stati	stic)	13.63447 0.000000

Figure 122: United Airlines - regression on the number of passengers per quarter.

#### 6.3 Baltimore (BWI) - Seattle (SEA)

What about the low-cost airline Southwest? Its specificity may also lead to disruption of our models for fares and passengers in case of competition with the major airlines. Consider for example the route between Baltimore/Washington International Airport (BWI) and Seattle-Tacoma International Airport. This route has been offered by the 2 major carriers Northwest, United since 1993, and also by Southwest If we consider the fares for this route (Figure 123), we can observe that there seems to be a trend for the fares to continuously decrease after 1993 probably to align with the fares proposed by the low-cost airline. In addition we can also observe the trend for the fares of Northwest to keep on decreasing below the fares of Southwest, following the global decreasing trend of fares we observed in the previous part for Northwest. If we try to run the regressions on the

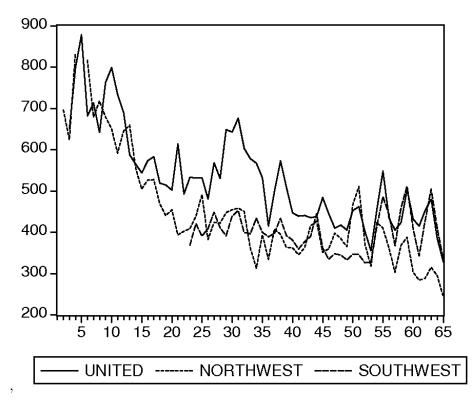


Figure 123: Quarterly average fares between Baltimore (BWI) and Seattle (SEA) (\$ against time).

fares for these 3 airlines, we get the following results (Figures 124 to 126): we can observe similar results as for the previous routes studied: we can see that the coefficient of trend is significant for the regression on the fares of Northwest Airlines, as is the the dummy variable for United Airlines.

> Dependent Variable: FARE4 Method: Least Squares Date: 02/03/10 Time: 18:30 Sample (adjusted): 10.65 Included observations: 56 after adjustments Convergence achieved after 33 iterations Backcast: 7.9

Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	467.8731	45.96929	10.17795	0.0000
@TREND	-2.125384	0.919522	-2.311401	0.0252
<b>A</b> R(1)	1.246599	0.140570	8.868170	0.0000
AR(2)	-1.239577	0.109543	-11.31585	0.0000
AR(3)	1.282528	0.132087	9.709718	0.0000
AR(4)	-0.434433	0.121779	-3.567379	0.0008
MA(1)	-0.730179	0.055077	-13.25737	0.0000
MA(2)	0.768951	0.053460	14.38374	0.0000
MA(3)	-0.959601	0.038778	-24.74629	0.0000
R-squared	0.845225	Mean deper	ndent var	414.4536
Adjusted R-squared	0.818880	S.D. depend		90.9 <b>7878</b>
S.E. of regression	38.71890	Akaike info	criterion	10.29676
Sum squared resid	70460.22	Schwarz cri	terion	10.62226
Log likelihood	-279.3092	F-statistic		32.08331
Durbin-Watson stat	2.004095	Prob(F-stati	stic)	0.000000
Inverted AR Roots Inverted MA Roots	.86 .96	.52 12+.99i	0 <b>7</b> +.98i 1299i	0 <b>7</b> 98i

Figure 124: Northwest Airlines - regression on quarterly average fares.

These 2 regressions remain stationary and do not show problems of autocorrelation in the residuals, but we may assume that again an ARIMA model is not sufficiently able to represent the behaviour of passenger fares on a route.

For Southwest Airlines, the model reveals the increasing trend for the fares, and a dummy variable after the terorist events of September 2001 (however this possible impact is quite low in

Dependent Variable: FARE5 Method: Least Squares Date: 02/03/10 Time: 18:32 Sample (adjusted): 3:65 Included observations: 63 after adjustments Convergence achieved after 11 iterations Backcast: 1:2

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	620.4826	24.44770	25.38000	0.0000
DUMMY	-183.6631	33.87270	-5.422156	0.0000
MA(1)	0.828315	0.090572	9.145405	0.0000
MA(2)	0.555726	0.093072	5.970957	0.0000
R-squared	0.756772	Mean dependent var		532.9023
Adjusted R-squared	0.744405	S.D. dependent var		117.0788
S.E. of regression	59.19086	Akaike info criterion		11.06080
Sum squared resid	206709.9	Schwarz criterion		11.19687
Log likelihood	-344.4151	F-statistic		61.19030
Durbin-Watson stat	1.929481	Prob(F-statistic)		0.000000
Inverted MA Roots	4162i	41+.62i		

Figure 125: United Airlines - regression on quarterly average fares.

comparison with the global impact we observed for the major airlines). Nevertheless, it appears difficult to find a quite good model with all the coefficients remaining significant.

The same conclusions can be drawn for the statistic on the number of passengers: we can observe that the dummy variable and trend variable appear to be insignificant for most airlines, and the  $R^2$  statistics are very low for all the regressions.

Dependent Variable: FARE7 Method: Least Squares Date: 02/03/10 Time: 18:32 Sample (adjusted): 23 65 Included observations: 43 after adjustments Convergence achieved after 22 iterations Backcast: 20 22

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	385.8249	36.67719	10.51948	0.0000
@TREND DU <b>MM</b> Y	0. <b>7</b> 95493 -31.69342	1.160668 31.10817	0.6853 <b>7</b> 5 -1.018814	0.49 <b>7</b> 4 0.3149
MA(1) MA(2)	0.914172 0.049678	0.159901 0.216083	5.717103 0.229902	0.0000 0. <b>8194</b>
MA(3)	-0.354064	0.145176	-2.438863	0.0197
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.507488 0.440933 35.30584 46120.58 -211.0374 2.039542	Mean deper S.D. depend Akaike info Schwarz crit F-statistic Prob(F-stati	dent var criterion terion	398.2017 47.21875 10.09476 10.34051 7.625026 0.000052
Inverted MA Roots	.49	70+.49i	7049i	

Figure 126: Southwest Airlines - regression on quarterly average fares.

## 7 Purely economic models

We saw in the previous sections some time series models for quarterly average fares for our 7 airlines. However, we can suppose that the fares proposed by an airline on a given route also depend on the characteristics of the market, and are not purely caused by the economic state of the airline. The fares may also be a function of the length of the route, the kind of route (e.g. route for leisure or business travellers), the population living at the endpoints of the route, and so on. The IENAC06TE study led by Jonathan Cobb and Nico Metzger, "Entry Strategy for Southwest Airlines", tries to find the models which could explain the fares of the low-cost airline for a specific route.<sup>19</sup>

We would like to observe whether it is possible to add some of the variables used in that study on Southwest to some basic panel data, taking into account the possible trend on the fares and the impacts of September 11, 2001 (with our dummy variable). Then we have to estimate, for a given carrier, the following equation:

$$Fare(t) = \alpha_0 + \alpha_1 \times t + \alpha_2 \times D(t) + \alpha_3 \times distance + \alpha_4 \times distance + \alpha_5 \times population + \alpha_6 \times leisure + \alpha_7 \times business + \alpha_8 \times GDP + \varepsilon(t),$$
(29)

where "distance", "population" and "GDP" are discrete variables chosen by Jonathan Cobb and Nico Metzger to model the characteristics of the market around the endpoints of the route. D(t) is a dummy variable used to model the U.S. terrorist attacks in 2001 (equal to 1 at and after period 35, and 0 otherwise), and "leisure" and "business" are also dummy variables, taking the value 1 if the route can be considered (according to the criteria developed in the study of Cobb and Metzger) as a "leisure" or "business" route. Here, we also include the variable of time in the regression to capture possible trends.

<sup>&</sup>lt;sup>19</sup>Research Project "Entry Strategy for Southwest Airlines", by Jonathan Cobb and Nico Metzger, supervised by Steve Lawford [6].

We get the following regression output from EViews6: we can observe that in fact these models are quite good! Most of coefficients of the 7 regressions are individually and jointly significant at the 95% and very often at the 99% levels, except for the population variable for Southwest and Northwest, and the Business or Leisure variable for Continental Airlines and Northwest.

Dependent Variable: FARE Method: Least Squares Date: 01/24/10 Time: 19:00 Sample: 1 31960 Included observations: 31960

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	379.5481	11.81848	32.11481	0.0000
T	-2.290994	0.083773	-27.34761	0.0000
DISTANCE	0.084423	0.000661	127.6961	0.0000
POPN/1000	-0.029912	0.001619	-18.47698	0.0000
LEISURE	-75.06033	2.213105	-33.91630	0.0000
BUSINESS	24.31567	11.68333	2.081228	0.0374
GDP/1000	0.696193	0.033023	21.08175	0.0000
SEP11	-87.25337	3.139054	-27.79608	0.0000
R-squared	0.472109	Mean dependent var		488.1838
Adjusted R-squared	0.471994	S.D. dependent var		191.3783
S.E. of regression	139.0632	Akaike info criterion		12.70798
Sum squared resid	6.18E+08	Schwarz criterion		12.71008
Log likelihood	-203065.6	F-statistic		4082.239
Durbin-Watson stat	0.310945	Prob(F-statistic)		0.000000

Figure 127: American Airlines - economic regression on quarterly average fares.

We note that if we do not include these variables in the regression, we only get significant variables in all our models. The  $R^2$  statistics of the models are quite high. Indeed, the  $R^2$  statistic for American Airlines is equal to 0.47, meaning that these variables already explain 47% of the fare setting behaviour for this carrier! This statistic is equal to 0.31 for Continental, 0.36 for Delta, 0.17 for Northwest, 0.54 for United,0.22 for US Airways and 0.52 for Southwest Airlines.

Again, we can observe a clear difference between the trend variable for the major carriers and Southwest: whereas the coefficient for the trend variable is lower than -1.70 dollars per quarter for all the major carriers but Continental, this coefficient is equal to 0.81 for Southwest. This trend

Included observations: 15184				
Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	309.3503	18.44364	16.77274	$\begin{array}{c} 0.0000\\ 0.0056\\ 0.0000\\ 0.0000\\ 0.0000\\ 0.1110\\ 0.0000\\ 0.0000\\ 0.0000\\ 0.0000\\ \end{array}$
T	-0.303479	0.109420	-2.773528	
DISTANCE	0.063429	0.000934	67.91425	
POPN/1000	-0.045714	0.002243	-20.38514	
LEISURE	-53.28485	2.691832	-19.79501	
BUSINESS	29.28988	18.37931	1.593633	
GDP/1000	1.051212	0.044194	23.78629	
SEP11	-58.11834	4.106555	-14.15258	
R-squared	0.314461	Mean dependent var		444.4828
Adjusted R-squared	0.314145	S.D. dependent var		154.4615
S.E. of regression	127.9194	Akaike info criterion		12.54120
Sum squared resid	2.48E+08	Schwarz criterion		12.54522
Log likelihood	-95204.83	F-statistic		994.4739
Durbin-Watson stat	0.366560	Prob(F-statistic)		0.000000

Dependent Variable: FARE Method: Least Squares Date: 01/24/10 Time: 19:01

Sample: 1 15184

Figure 128: Continental Airlines - economic regression on quarterly average fares.

shows the competition between these 2 models of airlines, and we may suggest according to these statistics, that there is a trend for the difference of fare setting between a low-cost airline and a major one, to be reduced.

The coefficient of the route length is positive for all the airlines: indeed, we can assume that the fares will be higher on a longer route.

We can observe that the coefficient for the population variable is negative, meaning that the fares tend to be higher between less populated areas. Indeed, it seems logical that in more populated areas, where demand and competition between airlines is higher, the fares will decrease. However we can observe that we reject this coefficient for Southwest Airlines, which can also be interpreted as a characteristic for the low-cost airline, to use secondary airports, and point-to-point services rather than hub-and-spoke networks. Using these secondary airports, Southwest also serves less populated areas in the neighbourhood of big cities where major airlines develop their hub airports.

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	435.6770	6.049651	72.01688	0.0000
T	-3.794347	0.071961	-52.72758	0.0000
DISTANCE	0.071834	0.000605	118.7003	0.0000
POPN/1000	-0.042562	0.001961	-21.70131	0.0000
LEISURE	-67.63937	1.597287	-42.34642	0.0000
BUSINESS	27.85667	5.816673	4.789107	0.0000
GDP/1000	0.798462	0.040062	19.93091	0.0000
SEP11	-14.17621	2.495536	-5.680627	0.0000
R-squared	0.360563	Mean dependent var		454.4555
Adjusted R-squared	0.360452	S.D. dependent var		166.4448
S.E. of regression	133.1089	Akaike info criterion		12.62041
Sum squared resid	7.10E+08	Schwarz criterion		12.62213
Log likelihood	-252968.1	F-statistic		3228.757
Durbin-Watson stat	0.320995	Prob(F-statistic)		0.000000

Dependent Variable: FARE Method: Least Squares Date: 01/24/10 Time: 19:03 Sample: 1 40090 Included observations: 40090

Figure 129: Delta Air Lines - economic regression on quarterly average fares.

The "leisure" and "business" variables show the trend for major airlines to decrease their fares on specific leisure routes, and increase these fares on business routes. For Southwest again, the traditional strategy for the low-cost airline is to not discriminate between business or leisure travellers but offer them the lower fare for their trip. Consequently, we can observe that the low-cost airline is the only airline with both coefficients negative for the variables leisure and business.

Again the low-cost airline is traditionaly not supposed to take into account the GDP on a given region to fix a higher or lower fare than for another U.S. region. Thus we can see that the coefficient for GDP is almost equal to 0 for Southwest. On the contrary, as this coefficient is definitely positive for the major airlines, we can assume that they seem to use this statistic in their fare setting to propose enforce higher fares in richer regions of the USA!

The impact of the terrorist attacks in September 11 may be one of the only coefficients with a similar impact on the low-cost airline and the legacy carriers. These events seem to have forced the

Included observations: 14264 Variable Coefficient Std. Error t-Statistic Prob. 434.4327 14.90564 29.14553 0.0000 С Т -2.252883 0.122767 -18.35084 0.0000 DISTANCE 0.023312 0.000952 24.47742 0.0000 POPN/1000 0.003287 -1.406055 0.1597 -0.004622 LEISURE 1.154329 2.621522 0.440328 0.6597 BUSINESS 52.21146 14.43909 3.615979 0.0003 GDP/1000 0.064672 0.067278 0.961259 0.3364 SEP11 -32.22625 0.0000 4.437407 -7.262405 R-squared 0.167501 Mean dependent var 447.7542 Adjusted R-squared 0.167092 S.D. dependent var 147.8276 S.E. of regression 134.9131 Akaike info criterion 12.64770 Sum squared resid 2.59E+08 Schwarz criterion 12.65194 Log likelihood -90195.39 F-statistic 409.7629 Durbin-Watson stat 0.290115 Prob(F-statistic) 0.000000

Dependent Variable: FARE Method: Least Squares Date: 01/24/10 Time: 19:04

Sample: 1 14264

Figure 130: Northwest Airlines - economic regression on quarterly average fares.

airlines to adapt their fares to a decreasing demand. This decrease of the fares appears to be very high for American Airlines and United Airlines (minus \$87 and \$89 respectively for the average fares of the 2 airlines), whereas Delta and Southwest seem to have been able to lower the impact of the terrorist attacks on their fare strategy (which can also be explained by the fact that Southwest in particular already had the lowest fares among these airlines before September 2001).

Dependent Variable: FARE Method: Least Squares Date: 01/24/10 Time: 19:04 Sample: 1 24728 Included observations: 24728

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C T DISTANCE POPN/1000 LEISURE BUSINESS GDP/1000	270.5218 -1.700538 0.099579 -0.055815 -89.06896 74.95982 1.266880	15.04574 0.098881 0.000691 0.001845 2.601667 14.93683 0.037283	17.97996 -17.19781 144.0634 -30.24770 -34.23535 5.018456 33.98007	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
SEP11	-89.75342	3.440959	-26.08384	0.0000
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood Durbin-Watson stat	0.545722 0.545593 141.7049 4.96E+08 -157579.8 0.333079	Mean deper S.D. depend Akaike info Schwarz crit F-statistic Prob(F-stati	dent var criterion terion	508.3681 210.2143 12.74569 12.74832 4242.283 0.000000

Figure 131: United Airlines - economic regression on quarterly average fares.

Dependent Variable: FARE
Method: Least Squares
Date: 01/24/10 Time: 19:05
Sample: 1 27230
Included observations: 27230

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	469.9082	6.293602	74.66443	0.0000
T	-1.971294	0.083367	-23.64598	0.0000
DISTANCE	0.033739	0.000859	39.26543	0.0000
POPN/1000	-0.083990	0.002229	-37.68008	0.0000
LEISURE	-90.25694	2.052832	-43.96704	0.0000
BUSINESS	20.49648	6.071357	3.375931	0.0007
GDP/1000	1.569493	0.044537	35.23984	0.0000
SEP11	-39.05656	3.014560	-12.95597	0.0000
R-squared	0.217890	Mean dependent var		424.9593
Adjusted R-squared	0.217689	S.D. dependent var		146.0084
S.E. of regression	129.1420	Akaike info criterion		12.56000
Sum squared resid	4.54E+08	Schwarz criterion		12.56241
Log likelihood	-170996.3	F-statistic		1083.409
Durbin-Watson stat	0.318775	Prob(F-statistic)		0.000000

Figure 132: US Airways - economic regression on quarterly average fares.

Dependent Variable: FARE Method: Least Squares Date: 01/24/10 Time: 19:06 Sample: 1 30324 Included observations: 30324

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	214.7214	2.594307	82.76636	0.0000
T	0.809883	0.040662	19.91738	0.0000
DISTANCE	0.060413	0.000333	181.4040	0.6272
POPN/1000	-0.000445	0.000916	-0.485621	0.0000
LEISURE	-22.89062	0.833207	-27.47291	0.0000
BUSINESS	-16.20416	2.238844	-7.237737	0.0000
GDP/1000	-0.078174	0.018652	-4.191260	0.0000
SEP11	-20.48762	1.180283	-17.35823	0.0000
R-squared	0.529839	Mean dependent var		302.9831
Adjusted R-squared	0.529730	S.D. dependent var		82.57083
S.E. of regression	56.62396	Akaike info criterion		10.91101
Sum squared resid	97201369	Schwarz criterion		10.91320
Log likelihood	-165424.7	F-statistic		4880.570
Durbin-Watson stat	0.335705	Prob(F-statistic)		0.000000

Figure 133: Southwest Airlines - economic regression on quarterly average fares.

## 8 Concluding remarks

The objective of this project was to conduct research into the modelling of the dynamic strategic behaviour of U.S. major carriers since 1993. The first step consisted in filtering the data that we were able to get from the U.S. Department of Transportation on the coupons and tickets bought by U.S. travellers. In particular, we decided to use the quarterly average fares proposed by the airlines for all round trips inside the U.S. domestic market, and the quarterly number of passengers which travelled on these routes since 1993. The data treatment and descriptive analysis formed an important first step of the work.

Then we supposed that the fares set by the airlines may depend on the past evolution of fares, and on the impact of economical or political events such as the U.S. terrorist attack in 2001. We built software to select and test rigorous time series models, we observed that we were able to capture a large amount of the fare setting strategies for these airlines. In particular, these models enabled us to clarify and quantify the different strategies between legacy airlines and a low-cost carrier such as Southwest Airlines. We also saw the impact that the September 11, 2001, had on each of the carriers, and the possible trends for these fares to decrease (especially for Northwest Airlines), or to increase as they seem to do for Southwest. These time series models also enabled us to make some robust static and dynamic forecasts on a short-term horizon, as to how fares may behave in the next 1 to 2 years, and how the number of passengers may evolve. This analysis has been fully automated using customized code, which formed a significant part of the modelling work, before we could begin interpretation of the results. It would also be a vital part of a repeated model estimation procedure, such as is often found in the private sector and other business settings.

Then we attempted to see whether the economic state of the carriers could be correlated with their fare setting behaviour. Using our best time series models, we included financial variables such as operational revenues or expenses, the cost of passenger services or the total number of employees in a given airline, and saw that these variables can in fact explain most of the trends and drops observed in the purely statistical models.

Finally, we wished to see whether purely economic models could be used to explain the fare setting. Using variables on route characteristics such as distance, whether the route is used more for business or leisure purposes, and the characteristics of the population and the GDP at the endpoints of this route, we saw that we could explain 30 to 40% of what is happening on these routes!

However, none of these models can be perfect. They could be improved in a number of ways. For example, it would be interesting to model more carefully the competition between the major airlines, to capture more realistically the strategy of the airlines in the U.S. market. It could be very revealing to observe what competitors do on a given route and to include the entry decisions of competitors. One of the difficulties we noticed with the major airlines is that there are also many existing and nascent code-sharing agreements between these carriers and smaller ones, which allow the carriers to extend their networks without necessarily being involved in the fare setting, nor in the strategy of these smaller carriers. These code-sharing effects are very difficult to capture as these agreements are temporary, but they may also have an impact on the behaviour of airlines and on their competition with other airlines.

## 8.1 Acknowledgements

Since this project would not have been possible without the data and support from many people we want to thank everybody who contributed, directly or indirectly, and especially:

- Steve Lawford, who very patiently gave answers to most of our questions and without whose support and ideas this project would have never been started, let alone finished.
- The DOT and BoTS for providing the data and for very quickly answering our questions.
- Mehrdad Farzinpour for maintaining the ENAC aviation database which was very useful during the project.
- Roseline Bilina at Cornell University, for very helpful comments on the project results and report.
- And everybody we might have forgot to mention in this list. Thank you!

## References

- [1] Continental Airlines, awards since 1996. http://www.continental.com/web/en-US/ content/company/globalcitizenship/awards.aspx.
- [2] Air transport association, 2009 Economic Report, 2009.
- [3] American Airlines. http://www.wikinvest.com/stock/American\_Airlines\_(AMR)#\_ note-2, 2009.
- [4] BARNUM, J. W. What prompted airline deregulation 20 years ago? What were the objectives of that deregulation and how were they achieved? http://library.findlaw.com/1988/Sep/ 1/129304.html, 1988.
- [5] BRYANT, A. Delta to buy only Boeing jets for 20 years. http://www.nytimes.com/1997/03/
   21/business/delta-to-buy-only-boeing-jets-for-20-years.html, 1997.
- [6] COBB, J., AND METZGER, N. Entry strategy for Southwest airlines. http://www.enac.fr/ recherche/leea/SteveLawford/steve\_site1\_links\_student\_projects.html, 2009.
- [7] DOERMER, M., AND LAVELL, T. Continental Air may reconsider combining with United. http://www.bloomberg.com/apps/news?pid=20601103&sid=aORDoRb8FJqE, 2009.
- [8] FISCHER, J. W. Aviation finance : FAA reauthorization and related issues. http://assets. opencrs.com/rpts/RL33913\_20080421.pdf, 2008.
- [9] GUZHVA, V. S., AND PAGIAVLAS, N. U.S. commercial airline performance after September 11,2001.
- [10] HAMILTON, J. D. Time Series Analysis, Princeton : Princeton University Press, 1994.

# A Appendix

## A.1 ARIMA models (automated outputs)

alpha         381.0909         1.056713         -0.415496         0.319092           se_alpha         3.3027         12.437         0.15544         0.455604         2.655630           IAR roots         0.5674139         0.574139         0.574139         0.100000         P[O-stats[1]         0.106000           R*         0.517633         JB         1.389676         max P[O-stats]         0.629000         P[O-stats[3]         0.41000           Continental         1.157432         0.241000         p[O-stats[3]         0.410000         p[O-stats[3]         0.410000           Continental         1.157432         0.400000         d=         0.000000         b=         0.000000         t=         0.000000           Continental         0.411570         0.778432         0.660123         SiC         9.3860307         max P[O-stats]         0.881000         P[O-stats[2]         0.880000         L=         0.000000         L=         0.000000         L=         0.000000         L=         0.0000												
se_apha         123.3027         0.124757         0.124757         0.256530           IAR roots1         0.986016         0.574139         0.574139         0.574139         0.00000         P[Q-stats[1]]         0.108000         P[Q-stats[2]]         0.241000           R*         0.917633         JB         1.389676         min P[Q-stats]         0.108000         P[Q-stats[2]]         0.241000           Continental         D=         1.000000         q=         0.000000         d=         0.000000         b=         0.000000         l=         0.000000           Se_alpha         14.13002         0.070481         tstats[1]         0.715000         F[Q-stats[2]]         0.281000         F[Q-stats[2]]         0.28100	American		p =	3.000000	q =	0.000000	d =	0.000000	b =	0.000000	t =	0.000000
t=statighpla         3.090638         8.470207 - 2.866904         2.659630           [AR roots]         0.917633         SiC         9.328462         max P[O-stats]         0.00000         P[O-stats[2]]         0.108000         P[O-stats[2]]         0.108000         P[O-stats[2]]         0.00000         L         0.00000         L         0.000000         L         0.00000	alpha	381.0909	1.056713	-0.415496	0.319092							
IAR roots         0.988016         0.574139           R*         0.917633         SIC         9.328462         min P[Q-stats[]         0.629000         P[Q-stats[2]]         0.241000           Down         2.017633         JB         1.398676         min P[Q-stats[]         0.108000         P[Q-stats[2]]         0.241000           Constinuental         D=         1.000000         q=         0.000000         d=         0.000000         b=         0.000000         t=         0.000000           Se, apha         14.35092         0.0773432         SiC         9.398567         max P[Q-stats]         0.881000         P[Q-stats[2]]         0.881000         E         0.000000         t=         0.00000	se alpha	123.3027	0.124757	0.175544	0.118374							
IAR roots         0.988016         0.574139           R*         0.917633         SIC         9.328462         min P[Q-stats[]         0.629000         P[Q-stats[2]]         0.241000           Down         2.017633         JB         1.398676         min P[Q-stats[]         0.108000         P[Q-stats[2]]         0.241000           Constinuental         D=         1.000000         q=         0.000000         d=         0.000000         b=         0.000000         t=         0.000000           Se, apha         14.35092         0.0773432         SiC         9.398567         max P[Q-stats]         0.881000         P[Q-stats[2]]         0.881000         E         0.000000         t=         0.00000	t-stat(alpha)	3.090693	8.470207	-2.366904	2.695630							
R*         0.917633         SIC         9.328462         max P[Q-stats]         0.629000         P[Q-stats](2]         0.241000           Continental         p =         1.00000         q =         0.000000         d =         0.000000         b         b         0.000000         b         0.000000		0.968016	0.574139	0.574139								
D-W         2.015383         JB         1.389676         min P[C-stats]         0.100000         P[C-stats]         0.240000           Continental         D =         1.000000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.00000           abe, aipha         141.35092         0.0774432         =         0.00000         d =         0.00000         t =         0.00000           IAR         0.03381         0.0773452         =         0.00000         d =         0.00000         t =         0.00000           D-W         1.837109         JB         5.386324         min P[C-stats]         0.028000         P[C-stats[3]         0.028000         P[C-stats[3]         0.028000         I =         0.00000           Bela         D         p =         3.000000         q =         2.000000         d =         0.000000         b =         0.00000         t =         0.00000           Bela         D         p =         3.000000         q =         1.000000         d =         0.000000         b =         0.000000         t =         0.00000           IAR         Col 21803         0.21803         0.21803         0.2180457         0.82810 <td>MA roots</td> <td></td>	MA roots											
D-W         2.015383         JB         1.389676         min P[C-stats]         0.108000         P[C-stats]         0.241000           Continental         D =         1.000000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.00000           apha         41.1574         0.773432         0.773432         0.0774432         0.0774432         0.00000         d =         0.000000         t =         0.00000           D-W         1.837109         JB         5.986324         min P[C-stats]         0.028000         D =         0.000000         t =         0.00000           apha         37.9.5326         0.538010         0.61737         0.038200         0.48670         0.49721           D-W         1.837109         JB         5.986324         0.48670         0.49271         D         0.00000         t =         0.00000           apha         28.79139         0.13780         0.13857         0.098230         0.48670         0.43570         P[C-stats[3]         0.020000         L         0.000000         L         0.000000         L         0.000000         L         0.000000         L         0.000000         L         0.000000         L         <		0.917633		SIC	9.328462	max	P[Q-stats]	0.629000	Pſ	Q-stats(1)]	0.108000	
Pic-stats[3]         0.415000         Pic-stats[3]         0.415000           alpha         431.1574         0.773432         0         0.00000         b         0.00000         1         0.00000           es_alpha         14.3002         0.774432         0.773432         0.773432         0.00000         1         <	D-W											
Continental         p =         1.00000         q =         0.00000         d =         0.00000         t =         0.00000           se_alpha         14.35092         0.070481         - </td <td></td>												
alpha         431.1574         0.773432           es_alpha         13.0922         0.773432           [MA roots]         0.660123         SIC         9.380507         max P[O-stats]         0.881000         P[O-stats[1]]         0.751000           D-W         1.837109         JB         5.986324         min P[O-stats]         0.029000         b         0.000000         b         0.0000000         b	Continental		p =	1.000000	a =	0.000000	d =	0.000000				0.000000
se, alpha Fielda(alpha) 30.04388 10.97355 Fielda(alpha) 379.8326 0.636018 0.811370 0.769838 0.426887 0.449721 se, alpha 27.9139 0.1073857 0.013157 0.026923 0.108506 0.097860 Fielda(alpha) 14.17741 7.742.05 6.167449 7.758052 3.848309 8.683040 Fielda(alpha) 14.17741 7.742.05 6.167449 7.758052 3.688309 8.683040 Fielda(alpha) 14.17741 7.742.05 6.167449 7.758052 3.688209 min P[C-stats] 0.026000 pr[C-stats[1] 0.026000 Fielda(alpha) 14.027409 0.044651 0.743569 Fielda(alpha) 2.02766 0.15650 0.197862 0.042935 Fielda(alpha) 2.07769 1.50630 0.197824 0.074569 Fielda(alpha) 2.07769 1.5063 0.197824 0.742169 0.139852 0.6822511 Fielda(alpha) 2.07769 1.5064235 0.642335 Fielda(alpha) 2.07769 1.50654 0.093980 0.106240 0.096300 Fielda(alpha) 2.07769 0.150540 0.033980 0.106240 0.096300 Fielda(alpha) 2.055159 JB 2.857827 min P[C-stats] 0.000000 b = 0.000000 t = 0.000000 Fielda(alpha) 2.055159 JB 2.857827 min P[C-stats] 0.076000 b = 0.000000 t = 0.000000 Fielda(alpha) 2.055159 JB 2.857827 min P[C-stats] 0.076000 b = 0.000000 t = 0.000000 Fielda(alpha) 2.055159 JB 1.985714 min P[C-stats] 0.076000 b = 0.000000 t = 0.000000 Fielda(alpha) 2.055159 JB 1.985714 min P[C-stats] 0.076000 Fielda(alpha) 2.026100 Fielda(alpha) 2.055159 JB 1.985714 min P[C-stats] 0.076000 Fielda(alpha) 2.060000 Fielda(alpha) 2.055159 JB 1.985714 min P[C-stats] 0.076000 Fielda(alpha) 2.000000 Fielda(alpha) 2.055159 JB 1.925157 min P[C-stats] 0.070000 Fielda(alpha) 2.000000 Fiel		431.1574			•							
t-state(a)pha         30.04388         10.97355           IAR roots         0.660123         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats[3]         0.029000           D-W         1.837109         JB         5.986324         min P[Q-stats]         0.029000         D         P[Q-stats[3]         0.029000         t=         0.00000         D         P[Q-stats[3]         0.029000         t=         0.00000         D         D         0.00000         D <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>												
IAR roots1         0.773432           IAR roots1         0.773432           IAR roots1         0.660123         SiC         9.380507         max P[C-stats]         0.029000         P[C-stats(2])         0.881000           D-W         1.837109         JB         5.986324         min P[C-stats]         0.029000         t=         0.00000           alpha         379.8326         0.836018         0.811370         0.769838         0.426887         0.449721           se_alpha         2.79139         0.179080         0.131557         0.099200         1.050066         0.97860           I-stattalpha         14.17741         7.74205         6.167449         7.758092         3.863040           IAR roots1         0.928163         0.922803         0.926300         0.926300         P[C-stats[1]         0.026000           IAR roots1         0.928163         0.922803         0.426451         0.743569         0.9172-stats[2]         0.003000           Northwest         p =         3.000000         d =         1.009000         d =         0.000000         P[C-stats[3]         0.000000           Northwest         p =         3.000000         g =         0.000000         P[C-stats[3]         0.000000         P[C-stats[3] </td <td></td> <td>30.04388</td> <td>10.97355</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>		30.04388	10.97355									
IMA rootsi         P[Q-stats]         OBS1000         P[Q-stats[1]         0.751000           D-W         1.837109         JB         5.986324         min P[Q-stats]         0.881000         P[Q-stats[2]         0.881000           Delta         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.000000           Japha         379.8326         0.380015         0.179508         0.175638         0.42887         0.4972.           istatialphal         J.17774         7.725092         3.898309         8.683040         I           IAR rootsl         0.528530         0.922630         0.922003         max P[Q-stats]         0.935000         P[Q-stats[2]         0.805000           PLV         1.898956         JB         9.078859         max P[Q-stats]         0.920000         t =         0.00000           alpha         316.1128         1.381132         0.807099         0.424651         0.73062         -         0.000000         t =         0.00000           alpha         316.1128         1.381132         0.807099         0.424651         0.743569         -         0.000000         t =         0.00000         t =         0.00000         t =         0.000000         F[Q-stats[2]         <								-				
R*         0.660123         SIC         9.380507         max P[C-stats]         0.029000         P[C-stats[2]         0.081000         P[C-stats[2]         0.081000           alpha         379.8326         0.036018         0.811370         0.769338         0.426887         0.849721         0.00000         t=	IMA rootsl											
D-W         1.837109         JB         5.986324         min P[Q-stats]         0.029000         P[Q-stats[3]         0.081000           Defta         p         3.000000         q         2.000000         d         0.000000         b         0.000000         t         0.000000           se, alpha         379.8326         0.38001         0.175800         0.131557         0.099320         0.105866         0.097860           Listatlabpla         1.17741         7.742025         6.167449         7.758092         3.8883040           R*         0.905418         SIC         8.799172         max P[Q-stats]         0.935000         P[Q-stats[2]         0.086500           D-W         1.898956         JB         9.078859         min P[Q-stats]         0.305000         P[Q-stats[2]         0.00000           as alpha         316.1128         1.381132         0.807099         0.404651         0.743569         0.000000         t=         0.00000           as alpha         336.1128         0.307099         0.404651         0.743569         0.000000         t=         0.00000           Lestattalpha         3.030102         9.176753         4.211901         3.260420         1.22256         0.178230         0.616300		0.660123		SIC	9.380507	max	P[Q-stats]	0.881000	Pſ	Q-stats(1)]	0.751000	
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $					5.986324	min	P[Q-stats]	0.029000				
Delta         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.00000           se, alpha         26.79139         0.107980         0.131557         0.092230         0.109506         0.097860           t-statidabhal         1.17741         7.742305         -6.67449         7.758092         3.89309         8.683040           IAR rootsl         0.928530         0.928250         0.929209         min P[C-stats]         0.935000         P[C-stats(1)]         0.026000           IAR rootsl         0.921803         0.921803         0.892909         min P[C-stats]         0.935000         P[C-stats(2)]         0.000000           alpha         316.1128         1.381132         -0.807099         0.404651         -7.43569         0.000000         b =         0.000000         I =         0.000000           alpha         3.016.1128         1.381132         -0.807099         0.404651         -7.43569         0.000000         P[C-stats(2)]         0.000000           AR rootsl         0.6778019         0.642935         0.642935         0.642935         0.642935         0.642935         0.000000         P[C-stats(2)]         0.000000         P[C-stats(2)]         0.000000         I<=				•			[ == = ====]					
alpha         379.8326         0.811370         0.769383         0.426887         0.849721           se_alpha         2.67139         0.179980         0.13557         0.09920         0.109566         0.97860           Lataitdapha         14.17741         7.742005         5.167449         7.758092         3.898309         8.683040           JAR rootsi         0.2921803         0.922630         0.922630         0.922630         0.292500         0.926500	Delta		p =	3.000000	a =	2.000000	d =	0.000000				0.000000
se, alpha Participant Partici		379.8326										
t-staticiphal         14.17741         7.742305         6.167449         7.758092         3.898309         8.683040           IAR rootsi         0.922530         0.922530         0.922530         0.922530         0.922530         0.926530         0.922500         0.925630         0.922500         0.925000         P[Q-stats[2]         0.085000         P[Q-stats[2]         0.085000         P[Q-stats[2]         0.085000         P[Q-stats[3]         0.103000         I=         0.00000         b=         0.000000         b=         0.000000         t=         0.00000         I=         0.000000         I=         0.00000												
IAR rootsi MA rootsi D. 0.921803         0.922830         0.922803         0.922803         0.921803 <th0.921803< th=""> <th0.921803< th=""> <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<></th0.921803<></th0.921803<>												
IMA rootsi R <sup>2</sup> 0.925183         0.925418         SiC         8.799172         max P[Q-stats]         0.935000         P[Q-stats[1]         0.026000           D-W         1.898956         JB         9.078859         min P[Q-stats]         0.026000         P[Q-stats[3]         0.03000           application         p =         3.00000         q =         1.00000         d =         0.00000         t =         0.00000           application         3.181132-0.80709         0.40451-0.743569         s         0.00000         t =         0.00000         t =         0.00000           application         9.023760         0.150530         0.191624         0.124160         0.30652         1         1         1         1         0.00000         P[Q-stats[1]         0.00000         P[Q-stats[2]         0.000000         P[Q-stats[3]         0.000000         P[Q-stats[3]         0.000000         P[Q-stats[3]         0.00000         P[Q-stats[3]         0.000000         P[Q-stats[3]         0.000000         P[Q-stats[3]         0.000000         P[Q-stats[3]         0.000000         P[Q-stats[3]         0.000000         F[Q-stats[3]         0.000000         F[Q-stats[3]         0.00000         F[Q-stats[3]         0.00000         F[Q-stats[2]         0.174000         P[Q-stats												
R²         0.905418         SiC         8.799172         max P[Q-stats]         0.935000         P[Q-stats[1])         0.026000           D-W         1.889556         JB         9.078859         min P[Q-stats]         0.026000         P[Q-stats[2]]         0.080000           alpha         316.1128         1.381132         0.807009         0.404651         0.426050         0.103082           estatina         0.03766         0.150050         0.11624         0.130852         -         -         0.000000         t=         0.000000         t=         0.000000           MArcotsl         0.743569         JE         2.55782         min P[Q-stats]         0.000000         P[Q-stats[2]]         0.000000           D-W         2.047965         JB         2.55782         min P[Q-stats]         0.000000         P[Q-stats[2]]         0.000000           JD-W         2.047965         JB         2.55782         0.098300         0.426000         b=         0.000000         t=         0.000000           Lastatis[1]         0.917017         SIC         8.765514         max P[Q-stats]         0.000000         t=         0.000000         t=         0.000000         t=         0.000000         t=         0.000000         t=												
D-W         1.898956         JB         9.078859         min P[Q-stats]         0.026000         P[Q-stats]         0.03000           Northwest         p = 3.000000         q = 1.000000         d = 0.000000         b = 0.000000         t = 0.00000           Se_alpha         30.23796         0.150503         0.191624         0.124109         0.130852           L-statialpha         3.00120         9.176753         4.211901         3.260439         5.662511           IAR rootsi         0.743569         JB         2.867827         min P[Q-stats]         0.000000         P[Q-stats(1)]         0.000000           United         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.00000           United         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.00000           Usatistical in the interval i				SIC	8,799172	max	P[Q-stats]	0.935000	Pľ	Q-stats(1)]	0.026000	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$												
					5.0.0000			2.020000				
alph         316.1128         1.381132         0.807099         0.404651         0.7343569           es.alpha         3.503102         9.176753         4.211901         3.260439         5.682511           IAR roots         0.978919         0.642935         0.642935         0.000000         P[Q-stats[1]         0.000000           PW         0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats[2]]         0.000000           United         p =         3.00000         q =         2.00000         d =         0.000000         b =         0.000000           United         p =         3.00000         q =         2.00000         d =         0.00000         b =         0.00000           alpha         447.2741         0.677871         0.770504         0.459692         0.826295         s         0.00000         t =         0.00000           se.alpha         3.03780         0.83830         0.45838         0.43638         0.45838         0.426851         0.774000           PL         0.346414         SIC         9.179854         max P[Q-stats]         0.976000         P[Q-stats(1]]         0.00000           BA         0.985714         SIC         9.179854 </td <td>Northwest</td> <td></td> <td>n =</td> <td>3.000000</td> <td>= D</td> <td>1.000000</td> <td>= b</td> <td>0.000000</td> <td></td> <td></td> <td></td> <td>0.000000</td>	Northwest		n =	3.000000	= D	1.000000	= b	0.000000				0.000000
se_sipha 90.23796 0.150503 0.191624 0.124109 0.130852  AR roots] 0.743569 R <sup>2</sup> 0.917107 SIC 8.7653 4.211901 3.260439 5.682511  AR roots] 0.743569 R <sup>2</sup> 0.917107 SIC 8.765514 max P[Q-stats] 0.000000 P[Q-stats(1)] 0.000000 P[Q-stats(2)] 0.000000 P[Q-stats(2)] 0.000000 lunted p = 3.000000 q = 2.000000 d = 0.000000 b = 0.000000 t = 0.00000 Lestat(alpha 19.82655 6.778816 -7.151852 8.198566 4.326906 8.580440 I-stat(alpha 19.82655 6.778855 -7.151852 8.198566 4.326906 8.580440 P[Q-stats(3)] 0.946938 0.946938 0.859274 [MA roots] 0.946938 0.946938 0.859274 P-W 2.055159 JB 1.985714 max P[Q-stats] 0.976000 P[Q-stats(1)] 0.096000 R <sup>2</sup> 0.834814 SIC 9.178854 max P[Q-stats] 0.976000 P[Q-stats(1)] 0.096000 P[Q-stats(2)] 0.174000 P[Q-stats(2)] 0.174000 P[Q-stats(2)] 0.174000 P[Q-stats(2)] 0.261000 US p = 3.000000 q = 2.000000 d = 0.000000 b = 0.000000 t = 0.00000 alpha 37.3178 0.882953 -0.949188 0.880449 0.128578 0.951685 se_alpha 31.05663 0.06565 0.03258 0.060679 0.017726 0.017278 Lestat(alpha 12.02055 14.57853 2.8.53930 14.50994 7.253694 58.46315  AR roots] 0.985331 0.986331 0.908659 MA roots] 0.985331 0.986331 0.908659 MA roots] 0.985331 0.908659 R <sup>2</sup> 0.643318 SIC 9.019546 max P[Q-stats] 0.020000 P[Q-stats(2)] 0.003000 P[Q-stats(3)] 0.033000 P[Q-stats(3)] 0.033000 P[Q-stats(2)] 0.391000 P[Q-stats(3)] 0.033000 P[Q-stats(3)] 0.033000 P[Q-stats(3)] 0.033000 P[Q-stats(2)] 0.242000 P[Q-stats(3)] 0.050000 P[Q-stats(2)] 0.254000 P[Q-stats(2)] 0.054000 P[Q-stats(1)] 0.054000 P[Q-stats(1)] 0.054000 P[Q-stats(1)] 0.054000 P[Q-s		316,1128					<u> </u>		~ ~ ~			2.000000
t=start[apha]         3.503102         9.176753         4.211901         3.260439         5.682511           IAR rootsi         0.978919         0.642935         0.743568         0.743568           R <sup>2</sup> 0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats(3)]         0.000000           United         p=         3.00000         q=         2.00000         d=         0.000000         b=         0.000000         t=         0.00000           alpha         447.2741         0.677871-0.740817         0.770504         0.459692         0.826295         se         se         alpha         2.55935         0.09997         0.103584         0.03980         0.106240         0.096300         t=         0.00000         t=         0.00000           Vestatighta]         0.826538         0.946938         0.859274         min P[Q-stats]         0.976000         P[Q-stats(1)]         0.096000           MA roots1         0.946938         0.850253         0.949979         0.174000         P[Q-stats]         0.976000         P[Q-stats(2)]         0.174000           V         2.055159         JB         1.98571         min P[Q-stats]         0.976000         P[Q-stats(1)]         0.020000         <												
IAR roots          0.743569           R²         0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats(1)]         0.000000           United         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.00000           United         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.00000           United         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.00000           United         19.82655         6.778885 -7.151852         8.198566         4.326906         8.580440           IAR roots1         0.946338         0.849344         SIC         9.179854         max P[Q-stats]         0.976000         P[Q-stats(1)]         0.096000           V2.055159         JB         1.985714         min P[Q-stats]         0.976000         P[Q-stats(2)]         0.174000           P[C-stats[3]         0.265159         JB         1.985714         0.916625         b = 0.000000         t = 0.00000           IAR roots1         0.985331         0.985331         0.96639         0.01726         0.016278           L*stat[apha         12.02055         JS         JS         0.247000												
IMA roots]         0.743569           R <sup>2</sup> 0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats(1)]         0.000000           United         p =         3.00000         q =         2.00000         d =         0.00000         P[Q-stats(2)]         0.000000           United         p =         3.00000         q =         2.00000         d =         0.00000         b =         0.00000           United         p =         3.00000         q =         2.00000         d =         0.00000         b =         0.00000         t =         0.00000           es_alpha         447.2741         0.67741         0.740854         0.459692         0.826295         0.000000         t =         0.00000           Usatif         0.946938         0.349938         0.859274         max P[Q-stats]         0.976000         P[Q-stats(1)]         0.096000         P[Q-stats(3)]         0.261000           US         p =         3.00000         q =         2.00000         d =         0.00000         t =         0.00000           US         p =         3.000000         q =         2.000000         d =         0.000000         t =         0.00000         t =					0.200 100	0.002011						
R²         0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats(2]]         0.000000           United         p =         3.00000         q =         2.00000         d =         0.00000         P[Q-stats(2]]         0.000000           United         apa         447.2741         0.777017         SIC         8.76574         min P[Q-stats]         0.000000         b =         0.00000         t =         0.00000           United         447.2741         0.777017         0.73584         0.03580         0.06230         0.94538         0.00000         t =         0.00000         t =         0.00000           Last         (AT7781)         0.7705740         A55665         A55666         A580440         A566         A55644           AR         0.946338         0.84938         0.859274         max P[Q-stats]         0.976000         P[Q-stats(3]]         0.026000           B²         0.834814         SIC         9.179854         max P[Q-stats]         0.976000         P[Q-stats(3]]         0.261000           US         p =         3.000000         q =         2.000000         d =         0.000000         t =         0.00000           ge. ajpha         31.05663 </td <td></td> <td></td> <td>0.042000</td> <td>0.042000</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>			0.042000	0.042000								
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $				SIC	8 765514	max	PIO-stats1	0.000000	Pľ	$\Omega$ -stats(1)]	0.000000	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$												
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	0 11	2.047303		00	2.001021							
alpha         447.2741         0.677871         -0.740817         0.770504         0.459692         0.826295           se_alpha         22.55935         0.099997         0.103584         0.09380         0.106240         0.096300           IAR rootsl         0.946938         0.946938         0.859274												
se_alpha         22.55935         0.099997         0.103584         0.099800         0.106240         0.096300           L-stat(alpha)         19.8655         6.778885         7.151852         8.19856         4.326906         8.580440           IAR rootsi         0.946938         0.859274	United		n =	3 000000	n =	2 000000			P	Q-stats(3)]	0.000000	
t-statialpha         19.82655         6.778885         -7.151852         8.198566         4.326906         8.580440           IAR rootsi         0.946938         0.459938         0.859274         Image: Construction of the state o		447 2741					d =		P	Q-stats(3)]	0.000000	0.000000
AR roots]       0.949938       0.84938       0.859274          MA roots]       0.909008       0.909008       0.909008         R2       0.834814       SIC       9.179854       max P[Q-stats]       0.976000       P[Q-stats(2)]       0.174000         D-W       2.055159       JB       1.985714       min P[Q-stats]       0.096000       P[Q-stats(2)]       0.174000         alpha       373.3178       0.882953 -0.949198       0.880449       0.128578       0.951685       0.000000       b =       0.000000       t =       0.00000         using alpha       373.3178       0.882953 -0.949198       0.880449       0.128578       0.951685       0.000000       t =       0.000000       P[Q-stats(1)]       0.001000       P[Q-stats(1)]       0.001000       P[Q-stats(1)]       0.001000       P[Q-stats(1)]       0.003000       P[Q-stats(1)]       0.003000       P[Q-stats(2)]       0.003000       P[Q-stats(2)]       0.000000       t =       0.000000       t =       0.000000       t =	alpha		0.677871	-0.740817	0.770504	0.459692	d = 0.826295		P	Q-stats(3)]	0.000000	
IMA roots         0.999008         0.999008           R <sup>2</sup> 0.834814         SIC         9.179854         max P[Q-stats]         0.976000         P[Q-stats(1)]         0.096000           D-W         2.055159         JB         1.985714         min P[Q-stats]         0.096000         P[Q-stats(2)]         0.174000           US         p=         3.000000         q=         2.000000         d=         0.000000         b=         0.000000         t=         0.00000           US         p=         3.000000         q=         2.000000         d=         0.000000         b=         0.000000         t=         0.000000           US         p=         3.000000         q=         2.000000         d=         0.000000         b=         0.000000         t=         0.000000           JAR rootsl         0.985331         0.985331         0.985531         0.915543         0.915543         0.91556         JB         1.525157         min P[Q-stats]         0.001000         P[Q-stats(2)]         0.003000         P[Q-stats(2)]         0.003000         P[Q-stats(2)]         0.003000         P[Q-stats(2)]         0.003000         P[Q-stats(2)]         0.003000         P[Q-stats(2)]         0.003000         P[Q-stats(2)]         0.0	alpha se_alpha	22.55935	0.677871 0.099997	-0.740817 0.103584	0.770504 0.093980	0.459692 0.106240	d = 0.826295 0.096300		P	Q-stats(3)]	0.000000	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	alpha se_alpha t-stat(alpha)	22.55935 19.82655	0.677871 0.099997 6.778885	-0.740817 0.103584 -7.151852	0.770504 0.093980	0.459692 0.106240	d = 0.826295 0.096300		P	Q-stats(3)]	0.000000	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	alpha se_alpha <u>t-stat(alpha)</u>  AR roots	22.55935 19.82655 0.946938	0.677871 0.099997 6.778885 0.946938	-0.740817 0.103584 -7.151852	0.770504 0.093980	0.459692 0.106240	d = 0.826295 0.096300		P	Q-stats(3)]	0.000000	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	alpha se_alpha t-stat(alpha)  AR roots   MA roots	22.55935 19.82655 0.946938 0.909008	0.677871 0.099997 6.778885 0.946938	-0.740817 0.103584 -7.151852 0.859274	0.770504 0.093980 8.198566	0.459692 0.106240 4.326906	d = 0.826295 0.096300 8.580440	0.000000	<u>P</u> [ b =	Q-stats(3)] 0.000000	0.000000 t =	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	22.55935 19.82655 0.946938 0.909008 0.834814	0.677871 0.099997 6.778885 0.946938	-0.740817 0.103584 -7.151852 0.859274 SIC	0.770504 0.093980 8.198566 9.179854	0.459692 0.106240 4.326906 max	d = 0.826295 0.096300 8.580440 P[Q-stats]	0.000000	P[ b = P[	Q-stats(3)] 0.000000 Q-stats(1)]	0.000000 t = 0.096000	
alpha         373.3178         0.882953         -0.949198         0.880449         0.128578         0.951685           se_alpha         31.05663         0.06055         0.03229         0.060679         0.017726         0.016278           t-stat(alpha)         12.02055         14.57853         -28.53930         14.50994         7.253694         58.46315           IAR roots          0.985331         0.906859	alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	22.55935 19.82655 0.946938 0.909008 0.834814	0.677871 0.099997 6.778885 0.946938	-0.740817 0.103584 -7.151852 0.859274 SIC	0.770504 0.093980 8.198566 9.179854	0.459692 0.106240 4.326906 max	d = 0.826295 0.096300 8.580440 P[Q-stats]	0.000000	P[ b = P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)]	0.000000 t = 0.096000 0.174000	
se_alpha         31.05663         0.060565         0.033259         0.060679         0.017726         0.016278           t-stat(alpha)         12.02055         14.57853         -28.53300         14.50994         7.253694         58.46315           IAR roots          0.985331         0.9085331         0.9085331         0.9085331         0.90000         P[Q-stats]         0.020000         P[Q-stats(1)]         0.001000           D-W         2.031955         JB         1.525157         min P[Q-stats]         0.001000         P[Q-stats(2)]         0.003000           Southwest         p =         1.000000         q =         0.000000         d =         0.000000         t =         0.00000           alpha         242.5268         0.812377	alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W	22.55935 19.82655 0.946938 0.909008 0.834814	0.677871 0.099997 6.778885 0.946938 0.909008	-0.740817 0.103584 -7.151852 0.859274 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714	0.459692 0.106240 4.326906 max min	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats]	0.000000	P b = P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.096000 0.096000 0.174000 0.261000	0.000000
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159	0.677871 0.099997 6.778885 0.946938 0.909008	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000	0.770504 0.093980 8.198566 9.179854 1.985714 q =	0.459692 0.106240 4.326906 max min 2.000000	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d =	0.000000	P b = P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.096000 0.096000 0.174000 0.261000	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W US alpha	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178	0.677871 0.099997 6.778885 0.946938 0.909008 p = 0.882953	-0.740817 0.103584 -7.151852 0.859274 SIC JB <u>3.000000</u> -0.949198	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449	0.459692 0.106240 4.326906 max min 2.000000 0.128578	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685	0.000000	P b = P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.096000 0.096000 0.174000 0.261000	0.000000
IMA roots         0.975543         0.975543         0.975543           R <sup>2</sup> 0.843318         SIC         9.019546         max P[Q-stats]         0.02000         P[Q-stats(1)]         0.001000           D-W         2.031955         JB         1.525157         min P[Q-stats]         0.001000         P[Q-stats(2)]         0.003000           Southwest         p =         1.000000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.00000           alpha         242.5268         0.812377           0.812377           0.0122         8.827793           JAR roots          0.812377             0.999000         P[Q-stats(1)]         0.242000           D-W         1.796068         JB         0.559358         min P[Q-stats]         0.999000         P[Q-stats(2)]         0.391000           P[Q-stats(2)]         0.318778        820563         0.813071         0.203025              0.00000         t =         0.00000             0.318303         0.505000          P[Q-stats(3)] <t< td=""><td>alpha se_alpha i-stat(alpha)  AR roots   MA roots  R<sup>2</sup> D-W US alpha se_alpha</td><td>22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663</td><td>0.677871 0.099997 6.77885 0.946938 0.909008 <b>p =</b> 0.882953 0.060565</td><td>-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259</td><td>0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679</td><td>0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726</td><td>d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278</td><td>0.000000</td><td>P b = P[ P[ P[</td><td>Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]</td><td>0.096000 0.096000 0.174000 0.261000</td><td>0.000000</td></t<>	alpha se_alpha i-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663	0.677871 0.099997 6.77885 0.946938 0.909008 <b>p =</b> 0.882953 0.060565	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278	0.000000	P b = P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.096000 0.096000 0.174000 0.261000	0.000000
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055	0.677871 0.099997 6.778885 0.946938 0.909008 0.909008 0.882953 0.060565 14.57853	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278	0.000000	P b = P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.096000 0.096000 0.174000 0.261000	0.000000
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	alpha se_alpha  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331	0.677871 0.099997 6.778885 0.946938 0.909008 0.909008 0.882953 0.68565 14.57853 0.985331	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278	0.000000	P b = P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.096000 0.096000 0.174000 0.261000	0.000000
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	alpha se_alpha iAR rootsi MA rootsi MA rootsi R <sup>2</sup> D-W US alpha se_alpha se_alpha iAR rootsi MA rootsi	22.55935 19.82655 0.946938 0.99008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543	0.677871 0.099997 6.778885 0.946938 0.909008 0.909008 0.882953 0.68565 14.57853 0.985331	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278 58.46315	0.000000 0.976000 0.096000 0.000000	P[ b = P[ P[ b =	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000	0.000000 t = 0.096000 0.174000 0.261000 t =	0.000000
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	alpha se_alpha iAR rootsi iMA rootsi R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) iAR rootsi R <sup>2</sup>	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318	0.677871 0.099997 6.778885 0.946938 0.909008 0.909008 0.882953 0.68565 14.57853 0.985331	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278 58.46315 P[Q-stats]	0.000000	P[ b = P[ P[ b = P[ p]	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000	0.000000
alpha         242.5268         0.812377           se_alpha         7.462084         0.092025           t-stat(alpha)         32.50122         8.827793           [AR roots]         0.812377           [MA roots]         0.812377           [Ar roots]         0.99000         P[Q-stats(2)]           alpha         331.8736         0.837578           331.8736         0.837578         0.030853           alpha         331.8736         0.837578           329.42788         0.073421         0.053025           alpha         31.8736         0.837578           329.42788         0.073421         0.063025           4.12904         11.27752         11.40794           1.127752         11.40794         15.91456           [AR roots]         0.966353         0.9	alpha se_alpha iAR rootsi iMA rootsi R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) iAR rootsi R <sup>2</sup>	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318	0.677871 0.099997 6.778885 0.946938 0.909008 0.909008 0.882953 0.68565 14.57853 0.985331	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278 58.46315 P[Q-stats]	0.000000	P[ b = P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(1)] Q-stats(2)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000	0.000000
se_alpha         7.462084         0.092025           t_stat(alpha)         32.50122         8.827793           [AR roots]         0.812377           [MA roots]         0.812377           P         0.660816         SIC         7.252009         max P[Q-stats]         0.999000         P[Q-stats(1)]         0.242000           P/W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p =         3.000000         q =         2.000000         d =         0.000000         b =         0.000000         t =         0.00000           alpha         331.8736         0.837578         0.820563         0.813071         0.203911         0.333839         se_alpha         29.42788         0.073421         0.051561         0.063025         0.030858         0.028717         t-stat(alpha)         11.27752         11.40794         -15.91456         12.90081         6.608099         32.51844         IAR roots]         0.943393         0.943393         0.913573         IMA roots]         0.966353         0.966353         IMA roots]         0.966353         0.966353         IMA roots]         0.9663453         0.966353         IMA roots]         0.054000	alpha se_alpha [AR roots] [MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] [MA roots] R <sup>2</sup> D-W	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000	0.000000
t-stat(alpha)         32.50122         8.827793           [AR roots]         0.812377           [MA roots]         0.812377           R <sup>2</sup> 0.660816         SIC         7.252009         max P[Q-stats]         0.999000         P[Q-stats(1)]         0.242000           D-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p =         3.00000         q =         2.00000         d =         0.000000         b =         0.00000         t =         0.00000           alpha         331.8736         0.837578 -0.820563         0.813071         0.203911         0.933839         s <td>alpha se_alpha istat(alpha) iAR roots  MA roots  D-W US alpha se_alpha t-stat(alpha) iAR roots  IAR roots  R<sup>2</sup> D-W Southwest</td> <td>22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955</td> <td>0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.882953 0.060565 14.57853 0.985331 0.975543</td> <td>-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB</td> <td>0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157</td> <td>0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min</td> <td>d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]</td> <td>0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000</td> <td>P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[</td> <td>Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]</td> <td>0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000</td> <td>0.000000</td>	alpha se_alpha istat(alpha) iAR roots  MA roots  D-W US alpha se_alpha t-stat(alpha) iAR roots  IAR roots  R <sup>2</sup> D-W Southwest	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.882953 0.060565 14.57853 0.985331 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000	0.000000
IAR roots          0.812377           IMA roots	alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  MA roots  P-W Southwest alpha	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268	0.677871 0.099997 6.77885 0.946938 0.909008 0.909008 0.882953 0.060565 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000	0.000000
IMA roots         Name         P[Q-stats]         P[Q-stats]         0.999000         P[Q-stats(1)]         0.242000           D-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p =         3.000000         q =         2.000000         d =         0.000000         b =         0.000000         t =         0.00000           alpha         331.8736         0.837578         0.820563         0.813071         0.203911         0.933839         0.942788         0.073421         0.051561         0.063025         0.030858         0.028717           t-stat(alpha)         11.27752         11.40794         -15.91456         12.90081         6.608099         32.51844           [AR roots]         0.966353         0.966353         0.966353         0.966353         0.966353           R <sup>2</sup> 0.906410         SIC         8.007179         max P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000           D-W         1.754899         JB         1.075718         min P[Q-stats]         0.054000         P[Q-stats(2)]         0.121000	alpha se_alpha t-stat(alpha) [AR roots] [MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] R <sup>2</sup> D-W Southwest alpha se_alpha	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000	0.000000
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	alpha se_alpha istat(alpha) i_AR roots 	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000	0.000000
D-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p =         3.00000         q =         2.00000         d =         0.00000         b =         0.00000         t =         0.00000           alpha         331.8736         0.837578         -0.820563         0.813071         0.203911         0.933839         s =         0.00000         t = <td>alpha se_alpha iAR roots] MA roots] R<sup>2</sup> D-W US alpha se_alpha t-stat(alpha) IAR roots] R<sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) iAR roots] AR roots]</td> <td>22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122</td> <td>0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543</td> <td>-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB</td> <td>0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157</td> <td>0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min</td> <td>d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]</td> <td>0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000</td> <td>P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[</td> <td>Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]</td> <td>0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000</td> <td>0.000000</td>	alpha se_alpha iAR roots] MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) IAR roots] R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) iAR roots] AR roots]	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.000000 0.020000 0.001000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000	0.000000
Av. fares         p =         3.00000         q =         2.00000         d =         0.00000         b =         0.00000         t =         0.00000           alpha         331.8736         0.837578         -0.820563         0.813071         0.203911         0.933839         =         0.000000         t =         0.00000         t =<	alpha se_alpha t-stat(alpha) [AR roots] MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) [AR roots] JAR roots] JAR roots] JAR roots]	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.985331 0.975543 0.943318 2.031955 242.5268 7.462084 32.50122 0.812377	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q</b> =	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] d = 0.951685 0.016278 58.46315 P[Q-stats] P[Q-stats] d =	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000	P[ b = P[ P[ b = P[ P[ P[ b =	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000 t =	0.000000
Av. fares         p =         3.00000         q =         2.00000         d =         0.00000         b =         0.00000         t =         0.00000           alpha         331.8736         0.837578         0.820563         0.813071         0.203911         0.933839         0.90000         t =         0.00000         t =         0.00	alpha se_alpha t-stat(alpha) [AR roots] [AR roots] [AR roots] D-W US alpha se_alpha t-stat(alpha) [AR roots] [MA roots] Boutwest alpha se_alpha t-stat(alpha) [AR roots] [AR roo	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 SIC	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q</b> = 7.252009	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           d =           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.000000 0.001000 0.000000	P[ b = P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(2)] Q-stats(2)] 0.000000 Q-stats(1)] Q-stats(1)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000	0.000000
alpha         331.8736         0.837578         -0.820563         0.813071         0.203911         0.933839           se_alpha         29.42788         0.073421         0.051561         0.063025         0.030858         0.028717           t-stat(alpha)         11.27752         11.40794         -15.91456         12.90081         6.608099         32.51844            AR roots          0.943393         0.913573	alpha se_alpha t-stat(alpha) [AR roots] [AR roots] [AR roots] D-W US alpha se_alpha t-stat(alpha) [AR roots] [MA roots] Boutwest alpha se_alpha t-stat(alpha) [AR roots] [AR roo	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816	0.677871 0.099997 6.778855 0.946938 0.909008 0.909008 0.90505 14.57853 0.985331 0.975543 0.975543	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 SIC	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q</b> = 7.252009	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000	d =           0.826295           0.096300           8.580440           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           d =           0.951685           0.016278           58.46315           P[Q-stats]           d =           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.000000 0.001000 0.000000	P[ b = P[ P[ b = P[ P[ p[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(3)] Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(3)] 0.000000	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000 t = 0.242000 0.391000	0.000000
se_alpha         29.42788         0.073421         0.051561         0.063025         0.030858         0.028717           t-stat(alpha)         11.27752         11.40794         15.91456         12.90081         6.608099         32.51844           IAR roots          0.943393         0.913573               IMA roots          0.966353         0.966353            P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000         P[Q-stats(2)]         0.121000           D-W         1.754899         JB         1.075718         min P[Q-stats]         0.054000         P[Q-stats(2)]         0.121000	alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  AR roots  lAR roots   AR roots	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816	0.677871 0.099997 6.778855 0.946938 0.909008 <b>P</b> = 0.882953 0.060565 14.57853 0.985331 0.975543 <b>P</b> = 0.812377 0.092025 8.827793	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 SIC JB	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q</b> =	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.001000 0.000000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000 0.391000 0.505000	0.000000
t-stat(alpha)         11.27752         11.40794         -15.91456         12.90081         6.608099         32.51844           [AR roots]         0.943393         0.943393         0.913573           [MA roots]         0.943393         0.96353         0.966353           R <sup>2</sup> 0.906410         SIC         8.007179         max P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000           D-W         1.754899         JB         1.075718         min P[Q-stats]         0.054000         P[Q-stats(2)]         0.121000	alpha se_alpha t-stat(alpha) [AR roots] [AR roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] [MA roots] AR roots] [AR root	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816 1.796068	0.677871 0.099997 6.77885 0.946938 0.909008 0.90008 0.900565 14.57853 0.985331 0.975543 0.975543 0.982025 8.827793	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 SIC JB 3.000000 3.000000	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q =</b> 7.252009 0.559358 <b>q =</b>	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000	d = 0.826295 0.096300 8.580440 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] d = P[Q-stats] p[Q-stats] d = P[Q-stats] d =	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.001000 0.000000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000 0.391000 0.505000	0.000000
AR roots          0.943393         0.913573            MA roots          0.966353         0.966353           R <sup>2</sup> 0.906410         SIC         8.007179         max P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000           D-W         1.754899         JB         1.075718         min P[Q-stats]         0.054000         P[Q-stats(2)]         0.121000	alpha se_alpha t-stat(alpha) [AR roots] [AR roots] [AR roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] [MA roots] [AR roo	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816 1.796068 331.8736	0.677871 0.099997 6.778855 0.946938 0.909008 0.90553 0.060565 14.57853 0.985331 0.975543 0.975543 0.92025 8.827793	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 0.033259 0.906859 SIC JB 1.000000 SIC JB 3.000000 -0.820563	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q</b> = 7.252009 0.559358 <b>q</b> = 0.813071	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911	d =           0.826295           0.096300           8.580440           P[Q-stats]           P[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           d =           0.951685           0.016278           58.46315	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.001000 0.000000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000 0.391000 0.505000	0.000000
IMA roots         0.966353         0.966353           R²         0.906410         SIC         8.007179         max P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000           D-W         1.754899         JB         1.075718         min P[Q-stats]         0.054000         P[Q-stats(2)]         0.121000	alpha se_alpha <u>t-stat(alpha)</u> [AR roots] [MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) [AR roots] [AR roots] [AR roots] [AR roots] R <sup>2</sup> D-W Southwest alpha se_alpha se_alpha se_alpha	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.985331 0.975543 0.843318 2.031955 242.5268 3.462084 3.2.50122 0.812377 0.660816 1.796068 331.8736 29.42788	0.677871 0.099997 6.778855 0.946938 0.909008 <b>p =</b> 0.882953 0.060565 14.57853 0.985331 0.975543 <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.975543</b> <b>0.9755430.97576</b> <b>0.0773421</b>	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.03259 -28.53930 0.906859 SIC JB 1.0000000 SIC JB 3.000000 -0.820563 0.051561	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q =</b> 7.252009 0.559358 <b>q =</b> 0.813071 0.063025	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911 0.030858	d =           0.826295           0.096300           8.580440           P[Q-stats]           P[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           d =           0.933839           0.028717	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.001000 0.000000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000 0.391000 0.505000	0.000000
R²         0.906410         SIC         8.007179         max P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000           D-W         1.754899         JB         1.075718         min P[Q-stats]         0.054000         P[Q-stats(2)]         0.121000	alpha se_alpha t-stat(alpha) [AR roots] [MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] [MA roots] AR roots] [AR root	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 3.250122 0.812377 0.660816 1.796068 331.8736 29.42788 11.27752	0.677871 0.099997 6.77885 0.946938 0.909008 0.90008 0.882953 0.060565 14.57853 0.985331 0.975543 0.975543 0.92025 8.827793 0.092025 8.827793 0.092025 8.827793 0.073421 11.40794	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 -0.820563 3.000000 -0.820563 -15.91456	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q =</b> 7.252009 0.559358 <b>q =</b> 0.813071 0.063025	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911 0.030858	d =           0.826295           0.096300           8.580440           P[Q-stats]           P[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           d =           0.933839           0.028717	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.001000 0.000000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000 0.391000 0.505000	0.000000
D-W 1.754899 JB 1.075718 min P[Q-stats] 0.054000 P[Q-stats(2)] 0.121000	alpha se_alpha t-stat(alpha) [AR roots] [AR roots] D-W US alpha se_alpha t-stat(alpha) [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] Av. fares alpha se_alpha t-stat(alpha) [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots] [AR roots]	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816 1.796068 331.8736 29.42788 11.27752 0.943393	0.677871 0.099997 6.77885 0.946938 0.909008 0.90008 0.90008 0.90008 14.57853 0.985331 0.975543 0.975543 0.975543 0.975543 0.92025 8.827793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.9279 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 0.092025 0.092025 0.092025 0.092025 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 -0.820563 3.000000 -0.820563 -15.91456	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q =</b> 7.252009 0.559358 <b>q =</b> 0.813071 0.063025	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911 0.030858	d =           0.826295           0.096300           8.580440           P[Q-stats]           P[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           d =           0.933839           0.028717	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.001000 0.000000	P[ b = P[ P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 t = 0.242000 0.391000 0.505000	0.000000
	alpha se_alpha t-stat(alpha)  AR roots   AR roots   AR roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots   AR roots	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 7.462084 32.50122 0.812377 0.660816 1.796068 331.8736 29.42788 11.27752 0.943393 0.966353	0.677871 0.099997 6.77885 0.946938 0.909008 0.90008 0.90008 0.90008 14.57853 0.985331 0.975543 0.975543 0.975543 0.975543 0.92025 8.827793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.9279 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 0.092025 0.092025 0.092025 0.092025 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 0.906859 SIC JB 1.000000 SIC JB 3.000000 -0.820563 0.051561 -15.91456 0.913573	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q</b> = 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q</b> = 7.252009 0.559358 <b>q</b> = 0.813071 0.063025 12.90081	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911 0.30858 6.608099	d =           0.826295           0.096300           8.580440           P[Q-stats]           p[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           0.933839           0.028717           32.51844	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.000000 0.0999000 0.242000 0.000000	P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] Q-stats(3)] Q-stats(3)] Q-stats(3)] 0.000000	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000 0.003000 t = 0.242000 0.391000 0.505000 t =	0.000000
PIQ-stats(3)1 0.210000	alpha se_alpha <u>t-stat(alpha)</u> [AR roots] MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] MA roots] R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) [AR roots] R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Av. fares alpha se_alpha se_alpha t-stat(alpha) [AR roots] [AR root	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 3.462084 3.2.50122 0.812377 0.660816 1.796068 331.8736 29.42788 11.27752 0.943393 0.966353 0.906410	0.677871 0.099997 6.77885 0.946938 0.909008 0.90008 0.90008 0.90008 14.57853 0.985331 0.975543 0.975543 0.975543 0.975543 0.92025 8.827793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.9279 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 0.092025 0.092025 0.092025 0.092025 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 -0.920563 0.051561 -15.91456 0.913573 SIC	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q =</b> 7.252009 0.559358 <b>q =</b> 0.813071 0.063025 12.90081 8.007179	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911 0.203911 0.203911 0.203911	d =           0.826295           0.096300           8.580440           P[Q-stats]           P[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           0.933839           0.028717           32.51844           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.0242000 0.242000 0.000000 0.242000 0.000000	P[ b = P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(3)] 0.000000	0.000000 t = 0.096000 0.174000 0.261000 t = 0.001000 0.003000 0.003000 0.003000 t = 0.242000 0.391000 0.505000 t = 0.054000	0.000000
	alpha se_alpha <u>t-stat(alpha)</u> [AR roots] MA roots] R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) [AR roots] MA roots] R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) [AR roots] R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Av. fares alpha se_alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W	22.55935 19.82655 0.946938 0.909008 0.834814 2.055159 373.3178 31.05663 12.02055 0.985331 0.975543 0.843318 2.031955 242.5268 3.462084 3.2.50122 0.812377 0.660816 1.796068 331.8736 29.42788 11.27752 0.943393 0.966353 0.906410	0.677871 0.099997 6.77885 0.946938 0.909008 0.90008 0.90008 0.90008 14.57853 0.985331 0.975543 0.975543 0.975543 0.975543 0.92025 8.827793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.82793 0.092025 8.9279 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.92795 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 8.9275 0.092025 0.092025 0.092025 0.092025 0.092025 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205 0.09205	-0.740817 0.103584 -7.151852 0.859274 SIC JB 3.000000 -0.949198 0.033259 -28.53930 0.906859 SIC JB 1.000000 -0.920563 0.051561 -15.91456 0.913573 SIC	0.770504 0.093980 8.198566 9.179854 1.985714 <b>q =</b> 0.880449 0.060679 14.50994 9.019546 1.525157 <b>q =</b> 7.252009 0.559358 <b>q =</b> 0.813071 0.063025 12.90081 8.007179	0.459692 0.106240 4.326906 max min 2.000000 0.128578 0.017726 7.253694 max min 0.000000 0.203911 0.203911 0.203911 0.203911	d =           0.826295           0.096300           8.580440           P[Q-stats]           P[Q-stats]           0.951685           0.016278           58.46315           P[Q-stats]           P[Q-stats]           P[Q-stats]           P[Q-stats]           0.933839           0.028717           32.51844           P[Q-stats]	0.000000 0.976000 0.096000 0.000000 0.001000 0.001000 0.001000 0.0242000 0.242000 0.000000 0.242000 0.000000	P[ b = P[ P[ P[ b = P[ P[ b = P[ P[ b = P[ P[ P[ P[ P[ P[ P[ P[ P[ P[	Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(3)] 0.000000 Q-stats(3)] 0.000000	0.000000 t = 0.096000 0.174000 0.261000 t = 0.261000 t = 0.003000 t = 0.242000 0.391000 0.505000 t = 0.054000 0.121000	0.000000

Figure 134: Best ARMA models for filtered data.

		p =	3.000000	q =	0.000000	d =	0.000000	b = 0.0000	00 t =	0.000000
American alpha	378 9510		-0.359443		0.000000	u =	0.000000	0.0000	<u> </u>	0.000000
se alpha			0.173427							
	2.737878	8.091277	-2.072591	2.615185						
AR roots	0.971148	0.562868	0.562868							
MA roots										
R <sup>2</sup>	0.918852		SIC	9.294522		P[Q-stats]			)] 0.120000	
D-W	1.997686		JB	1.594823	min	P[Q-stats]	0.120000		0.284000	
Continental		n –	1 000000	a –	0 000000	d =	0 000000	P[Q-stats(3)] b = 0.0000	b)] 0.466000 00 t =	0.000000
alpha	434 2499	0.756818	1.000000	<u> </u>	0.000000	u =	0.000000	D = 0.0000	<u> </u>	0.00000
se_alpha		0.073189								
	33.79967	10.34066								
AR roots	0.756818								-	
MA roots										
R <sup>2</sup>	0.632982		SIC	9.301369		P[Q-stats]			)] 0.614000	
D-W	1.847370		JB	3.407983	mın	P[Q-stats]	0.026000		0.684000	
Delta		p =	4.000000	a –	3.000000	d =	0.000000	P[Q-stats(3)] b = 0.0000	0.026000 00 t =	0.00000
alpha	362 4295					-0.408297			<u> </u>	0.00000
se_alpha						0.054459				
						-7.497300				
AR roots			0.877047							
MA roots		0.997486								
R <sup>2</sup>	0.935396		SIC	8.853235		P[Q-stats]			)] 0.037000	
D-W	1.815138		JB	1.689929	min	P[Q-stats]	0.037000		0.112000	
Northwest		-	2 000000	-	2 000000	-	0.000000		<u>)] 0.219000</u>	0.00000
Northwest alpha	265 0175	p =	2.000000 0.466547	q =	3.000000		0.000000	b = 0.0000	00 t =	0.00000
se alpha			0.466547							
			3.315209							
AR roots	0.984587								-	
MA roots		0.892281	0.892281							
R <sup>2</sup>	0.943088		SIC	8.432495		P[Q-stats]			)] 0.002000	-
D-W	2.394593		JB	3.759989	min	P[Q-stats]	0.000000		)] 0.002000	
ا ب ا ما ا			2 000000		0.000000		0.000000		0.000000	0.00000
United alpha	151 2016	p =	3.000000 -0.335958	q = 0.217294	0.000000	d =	0.000000	b = 0.0000	00 t =	0.00000
se_alpha			0.129389							
			-2.596497							
AR roots			0.488977						-	
MA roots		0.400011								
		0.400077								
R <sup>2</sup>	0.835812	0.400077	SIC	9.264390		P[Q-stats]			)] 0.002000	
		0.400377	SIC JB	9.264390 2.908669		P[Q-stats] P[Q-stats]		P[Q-stats(2	0.010000	
R² D-W	0.835812		JB	2.908669	min	P[Q-stats]	0.002000	P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000	0.00000
R² D-W US	0.835812 2.148459	p =	JB 3.000000	2.908669 q =	min 3.000000	P[Q-stats] d =	0.002000	P[Q-stats(2	)] 0.010000 )] 0.027000	0.00000
R <sup>2</sup> D-W US alpha	0.835812 2.148459 314.7620	<u>p =</u> 0.470643	JB <u>3.000000</u> 0.937356	2.908669 q = -0.436102	min <u>3.000000</u> 0.424501	P[Q-stats] d = -0.980222	0.002000 0.000000 -0.437103	P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000	0.00000
R <sup>2</sup> D-W US alpha se_alpha	0.835812 2.148459 314.7620 39.46172	p = 0.470643 0.166977	JB 3.000000 0.937356 0.029355	2.908669 q = -0.436102 0.145251	min 3.000000 0.424501 0.183268	P[Q-stats] d = -0.980222 0.046190	0.002000 0.000000 -0.437103 0.146426	P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000	0.00000
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)	0.835812 2.148459 314.7620 39.46172 7.976390	p = 0.470643 0.166977 2.818616	JB <u>3.000000</u> 0.937356 0.029355 31.93220	2.908669 q = -0.436102 0.145251	min 3.000000 0.424501 0.183268	P[Q-stats] d = -0.980222	0.002000 0.000000 -0.437103 0.146426	P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000	0.00000
R <sup>2</sup> D-W US alpha se_alpha	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354	p = 0.470643 0.166977	JB 3.000000 0.937356 0.029355 31.93220 0.463641	2.908669 q = -0.436102 0.145251	min 3.000000 0.424501 0.183268	P[Q-stats] d = -0.980222 0.046190	0.002000 0.000000 -0.437103 0.146426	P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354	p = 0.470643 0.166977 2.818616 0.966352	JB 3.000000 0.937356 0.029355 31.93220 0.463641	2.908669 q = -0.436102 0.145251	min 3.000000 0.424501 0.183268 2.316281 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000	P[Q-stats(2 P[Q-stats(3 b = 0.0000	)] 0.010000 )] 0.027000 00 t = )] 0.002000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491	p = 0.470643 0.166977 2.818616 0.966352	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549	2.908669 q = -0.436102 0.145251 -3.002413	min 3.000000 0.424501 0.183268 2.316281 max	P[Q-stats] d = -0.980222 0.046190 -21.22161	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(1	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778	p = 0.470643 0.166977 2.818616 0.966352 0.970443	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Southwest	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p =	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min 3.000000 0.424501 0.183268 2.316281 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(1	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha) [AR roots] [MA roots] R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 3.31195	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 3.31195	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 <b>9.202308</b> 0.458602	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.002000 )] 0.001000 )] 0.002000	
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   AR roots	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.973354 0.864778 1.813794 247.7865 7.438368 <u>33.31195</u> 0.808502	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000	2.908669 q = -0.436102 0.145251 -3.002413 9.202308 0.458602 q =	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max	P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.0000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 00 t = )] 0.188000 )] 0.347000	
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.0000000 SIC JB	2.908669 q = -0.436102 0.145251 -3.002413 9.202308 0.458602 q = 7.295035 0.638795	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000 0.188000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha Na roots   AR roots   AR roots  seadba	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773	p = 0.470643 0.166977 2.818616 0.966352 0.970443 p = 0.808502 0.092221 8.767014	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000	2.908669 q = -0.436102 0.145251 -3.002413 9.202308 0.458602 q = 7.295035 0.638795 q =	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max min 2.000000	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.0000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(1	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Ar roots  R <sup>2</sup> D-W Av. fares alpha	0.835812 2.148459 314.7620 0.973354 0.97491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616	p = 0.470643 2.818616 0.966352 0.970443 p = 0.808502 0.092221 8.767014 p = 0.829496	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000 -0.815538	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max min 2.000000 0.208508	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000 0.188000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots  MA roots  D-W Southwest alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Av. fares alpha se_alpha	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685	p = 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.092221 8.767014 p = 0.829496 0.074183	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.0000000 SIC JB 3.0000000 -0.815538 0.053686	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000 0.188000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000
R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228	p = 0.470643 0.166977 2.818616 0.966352 0.970443 0.808502 0.092221 8.767014 8.767014 0.829496 0.074183 11.18170	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000 -0.815538 0.053686 -15.19086	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000 0.188000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha) IAR roots  MA roots  B <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) IAR roots  MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha se_alpha se_alpha se_alpha t-stat(alpha) IAR roots  IAR roots  IAR roots	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.943006	p = 0.470643 0.166977 2.818616 0.966352 0.970443 0.808502 0.092221 8.767014 p = 0.829496 0.074183 11.18170 0.943006	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000 -0.815538 0.053686 -15.19086	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000 0.188000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(2 P[Q-stats(3	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha) IAR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) IAR roots  IMA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) Se_alpha t-stat(alpha) IAR roots  IAR roots	0.835812 2.148459 314.7620 0.973354 0.974390 0.973354 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.943006 0.964502	p = 0.470643 0.166977 2.818616 0.966352 0.970443 0.808502 0.092221 8.767014 8.767014 0.829496 0.074183 11.18170	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000 -0.815538 0.053686 -15.19086 0.910468	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342 12.78216	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310 6.077257	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000 0.188000 0.000000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(3 b = 0.00000	)] 0.010000 )] 0.027000 )] 0.027000 )] 0.027000 )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 )] 0.02000 )] 0.1880000 )] 0.1880000 )] 0.493000 )] 0.493000 )] 0.493000 )] 0.493000 )] 0.493000 )] 0.493000 )] 0.493000 ]] 0.4930000 ]] 0.49300000000000000000000000000000000000	0.00000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots  MA roots  BP D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha (AR roots) [AR roots] [AR roots]	0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.943006	p = 0.470643 0.166977 2.818616 0.966352 0.970443 0.808502 0.092221 8.767014 p = 0.829496 0.074183 11.18170 0.943006	JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000 -0.815538 0.053686 -15.19086	2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310 6.077257 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000 0.188000 0.188000 0.0536000	P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(1 P[Q-stats(2 P[Q-stats(3 b = 0.0000 P[Q-stats(2 P[Q-stats(3 b = 0.0000 b = 0.0000	)] 0.010000 )] 0.027000 00 t = )] 0.002000 )] 0.001000 )] 0.002000 )] 0.002000 00 t = )] 0.188000 )] 0.347000 )] 0.347000 )] 0.493000	0.00000

Figure 135: Best ARMA models for non filtered data.

			0.000000		0.000000	-1	0.000000	Ŀ	0.000000		0.000000
American alpha	378 9510	p = 1.015036	3.000000	q = 0.307679	0.000000	d =	0.000000	b =	0.000000	t =	0.000000
se_alpha			0.173427								
t-stat(alpha)			-2.072591								
AR roots	0.971148	0.562868	0.562868								
MA roots											
R <sup>2</sup>	0.918852		SIC	9.294522		P[Q-stats]			Q-stats(1)]		
D-W	1.997686		JB	1.594823	mın	P[Q-stats]	0.120000		Q-stats(2)		
Continental		p =	1.000000	a –	0.000000	d =	0.000000	b =	<u>2-stats(3)]</u> 0.000000		0.000000
alpha	434.2499		1.000000	<u> </u>	0.000000	u =	0.000000	D =	0.000000	ι=	0.000000
se_alpha	12.84776										
t-stat(alpha)	33.79967	10.34066									
AR roots	0.756818										
MA roots											
R <sup>2</sup>	0.632982		SIC	9.301369		P[Q-stats]			Q-stats(1)]		
D-W	1.847370		JB	3.407983	min	P[Q-stats]	0.026000		Q-stats(2)]		
Dolto		n	4 000000	~	2 000000	d	0.000000		<u>2-stats(3)]</u>		0.00000
Delta alpha	362 / 205	p =	4.000000		3.000000			b =	0.000000	t =	0.000000
se alpha			0.163324								
t-stat(alpha)			-6.868886								
AR roots			0.877047								
MA roots			0.986820								
R <sup>2</sup>	0.935396		SIC	8.853235		P[Q-stats]			Q-stats(1)]		
D-W	1.815138		JB	1.689929	min	P[Q-stats]	0.037000		Q-stats(2)]		
									Q-stats(3)]		
Northwest	005 0475		2.000000		3.000000		0.000000	b =	0.000000	t =	0.000000
alpha			0.466547 0.140729								
se_alpha t-stat(alpha)											
AR roots	0.984587		3.315209	3.400077	-7.177000	-0.730397					
MA roots		0.892281	0 892281								
R <sup>2</sup>	0.943088	0.002201	SIC	8.432495	max	P[Q-stats]	0.002000	PIC	Q-stats(1)]	0.002000	
D-W	2.394593		JB	3.759989		P[Q-stats]			Q-stats(2)]		
									Q-stats(3)		
United		p =	3.000000	q =	0.000000	d =	0.000000	b =	0.000000	t =	0.000000
alpha			-0.335958								
se_alpha t-stat(alpha)	32.65618										
I I-Statrainna				0.090678							
	13.81918	9.022379	-2.596497								
AR roots	13.81918		-2.596497								
AR roots	13.81918 0.908804	9.022379	-2.596497 0.488977	2.396330	max	P[Q-stats]	0.191000	PIC	Q-stats(1)]	0.002000	
AR roots	13.81918 0.908804 0.835812	9.022379	-2.596497			P[Q-stats] P[Q-stats]			Q-stats(1)] Q-stats(2)]		
AR roots   MA roots  R <sup>2</sup>	13.81918 0.908804	9.022379	-2.596497 0.488977 SIC	2.396330 9.264390		P[Q-stats] P[Q-stats]		P[C	Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.010000	
AR roots   MA roots  R <sup>2</sup> D-W	13.81918 0.908804 0.835812 2.148459	9.022379 0.488977	-2.596497 0.488977 SIC JB 3.000000	2.396330 9.264390 2.908669 q =	min 3.000000	P[Q-stats] d =	0.002000	P[C	Q-stats(2)] Q-stats(3)]	0.010000 0.027000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W US alpha	13.81918 0.908804 0.835812 2.148459 314.7620	9.022379 0.488977 <b>p =</b> 0.470643	-2.596497 0.488977 SIC JB 3.000000 0.937356	2.396330 9.264390 2.908669 q = -0.436102	min <u>3.000000</u> 0.424501	P[Q-stats] <u>d =</u> -0.980222	0.002000 0.000000 -0.437103	P[0 P[0	Q-stats(2)] Q-stats(3)]	0.010000 0.027000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172	9.022379 0.488977 <b>p =</b> 0.470643 0.166977	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251	min 3.000000 0.424501 0.183268	P[Q-stats] d = -0.980222 0.046190	0.002000 0.000000 -0.437103 0.146426	P[0 P[0	Q-stats(2)] Q-stats(3)]	0.010000 0.027000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390	9.022379 0.488977 <b>p =</b> 0.470643 0.166977 2.818616	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251	min 3.000000 0.424501 0.183268	P[Q-stats] d = -0.980222 0.046190	0.002000 0.000000 -0.437103 0.146426	P[0 P[0	Q-stats(2)] Q-stats(3)]	0.010000 0.027000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354	9.022379 0.488977 0.470643 0.166977 2.818616 0.966352	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251	min 3.000000 0.424501 0.183268	P[Q-stats] d = -0.980222 0.046190	0.002000 0.000000 -0.437103 0.146426	P[0 P[0	Q-stats(2)] Q-stats(3)]	0.010000 0.027000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491	9.022379 0.488977 <b>p =</b> 0.470643 0.166977 2.818616	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413	min 3.000000 0.424501 0.183268 2.316281	P[Q-stats] d = -0.980222 0.046190 -21.22161	0.002000 0.000000 -0.437103 0.146426 -2.985151	P[C P[C b =	Q-stats(2)] Q-stats(3)] 0.000000	0.010000 0.027000 t =	0.000000
AR roots   MA roots  R <sup>2</sup> D-W us alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup>	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778	9.022379 0.488977 0.470643 0.166977 2.818616 0.966352	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308	min 3.000000 0.424501 0.183268 2.316281 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000	P[0 P[0 b = P[0	Q-stats(2)] Q-stats(3)] 0.000000 0.000000	0.010000 0.027000 t = 0.002000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491	9.022379 0.488977 0.470643 0.166977 2.818616 0.966352	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413	min 3.000000 0.424501 0.183268 2.316281 max	P[Q-stats] d = -0.980222 0.046190 -21.22161	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000	P[0 P[0 b = P[0 P[0	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)]	0.010000 0.027000 t = 0.002000 0.002000 0.001000	0.000000
AR roots   MA roots  R <sup>2</sup> D-W us alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup>	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308 0.458602	min 3.000000 0.424501 0.183268 2.316281 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000	P[0 P[0 b = P[0 P[0	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.010000 0.027000 t = 0.002000 0.002000 0.001000 0.002000	
AR roots MA roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots MA roots R <sup>2</sup> D-W	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308 0.458602	min 3.000000 0.424501 0.183268 2.316281 max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[0 P[0 b = P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.010000 0.027000 t = 0.002000 0.002000 0.001000 0.002000	
AR roots MA roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots IMA roots IMA roots R <sup>2</sup> D-W Southwest alpha se_alpha	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 <u>P =</u> 0.808502 0.092221	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308 0.458602	min 3.000000 0.424501 0.183268 2.316281 max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[0 P[0 b = P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.010000 0.027000 t = 0.002000 0.002000 0.001000 0.002000	
AR roots MA roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots MA roots MA roots MA roots D-W Southwest alpha se_alpha t-stat(alpha)	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 3.31195	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 <u>P =</u> 0.808502 0.092221	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[0 P[0 b = P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.010000 0.027000 t = 0.002000 0.002000 0.001000 0.002000	
AR roots AR roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) AR roots A	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 <u>P =</u> 0.808502 0.092221	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308 0.458602	min <u>3.000000</u> 0.424501 0.183268 <u>2.316281</u> max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000	P[0 P[0 b = P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.010000 0.027000 t = 0.002000 0.002000 0.001000 0.002000	
AR roots AR roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots JAR roots R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) IAR roots JAR roots JMA roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 <u>P =</u> 0.808502 0.092221	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> =	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000	P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000	P[C P[C b = P[C P[C p[C b =	Q-stats(2)] <u>D-stats(3)]</u> 0.000000 0.000000 0-stats(2)] <u>D-stats(3)]</u> 0.000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t =	
AR roots MA roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots MA roots D-W Southwest alpha se_alpha t-stat(alpha) AR roots MA roots MA roots MA roots R <sup>2</sup> D-W	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 <u>P =</u> 0.808502 0.092221	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000	2.396330 9.264390 2.908669 <b>q =</b> -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q =</b> 7.295035	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max	P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000	P[C P[C b = P[C P[C P[C b = P[C	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(1)] 2-stats(3)] 0.000000 0.000000 0.stats(1)]	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000	0.000000
AR roots AR roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots JAR roots R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) IAR roots JAR roots JMA roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 <u>P =</u> 0.808502 0.092221	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> =	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max	P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(1)] 2-stats(3)] 0.000000 0.000000 0.stats(1)] 2-stats(2)]	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000	
AR roots         MA roots        R²       D-W       US       alpha       se_alpha       t-stat(alpha)        MA roots         MA roots        Bouthwest       alpha       se_alpha       t-stat(alpha)        AR roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.970443 0.970443	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.0000000	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max min	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 b = P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0-stats(2)] 2-stats(3)] 0.0000000 0.0000000 0.000000 0.000000 0.000000 0.0000000 0.0000000 0.0000000 0.0000000 0.00000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.493000	0.000000
AR roots         MA roots        R²       D-W       US       alpha       se_alpha       t-stat(alpha)        AR roots         MA roots        R²       D-W       Southwest       alpha       se_alpha       t-stat(alpha)        AR roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.966352 0.970443 0.092221 8.767014 p =	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000	2.396330 9.264390 2.908669 q = -0.436102 0.145251 -3.002413 9.202308 0.458602 q = 7.295035 0.638795 q =	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max min 2.000000	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d =	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 1.000000	P[0 P[0 P[0 P[0 P[0 b = P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(1)] 2-stats(3)] 0.000000 0.000000 0.stats(1)] 2-stats(2)]	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000	0.000000
AR roots         MA roots        R²       D-W       US       alpha       se_alpha       t-stat(alpha)        MA roots         MA roots        R²       D-W       Southwest       alpha       se_alpha       t-stat(alpha)        AR roots         AR roots         AR roots         AR roots         AR roots         AR roots         AR roots        -W	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 3.31195 0.808502 0.657712 1.754773 341.0616	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.960352 0.970443 0.960352 0.970443 0.960352 0.92221 8.767014	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 max min 2.000000 0.208508	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 b = P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0-stats(2)] 2-stats(3)] 0.0000000 0.0000000 0.000000 0.000000 0.000000 0.0000000 0.0000000 0.0000000 0.0000000 0.00000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.493000	0.000000
AR roots MA roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots MA roots P-W Southwest alpha se_alpha t-stat(alpha) AR roots AR roots A	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.970443 0.970443 0.92221 8.767014 8.767014	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 SIC JB 3.000000 -0.815538	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = 0.930264 0.031935	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 b = P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0-stats(2)] 2-stats(3)] 0.0000000 0.0000000 0.000000 0.000000 0.000000 0.0000000 0.0000000 0.0000000 0.0000000 0.00000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.493000	0.000000
AR roots         MA roots        R²       D-W       US       alpha       se_alpha       t-stat(alpha)        AR roots         MA roots        P-W       Southwest       alpha       se_alpha       t-stat(alpha)        AR roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.97354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.943006	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.970443 0.092221 8.767014 0.092221 8.767014 1.18170 0.943006	-2.596497 0.488977 SIC JB 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.0000000 -0.815538 0.053686	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = 0.930264 0.031935	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 b = P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0-stats(2)] 2-stats(3)] 0.0000000 0.0000000 0.000000 0.000000 0.000000 0.0000000 0.0000000 0.0000000 0.0000000 0.00000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.493000	0.000000
AR roots AR roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots IMA roots R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) AR roots IMA	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 3.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.944300 0.964502	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.970443 0.970443 0.970443 0.92221 8.767014 0.808502 0.092221 8.767014 0.808502 0.092221 8.767014	-2.596497 0.488977 0.488977 0.488977 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 -0.815538 0.053686 -15.19086 0.910468	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342 12.78216	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310 6.077257	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats]	0.002000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000 0.188000 0.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(2)] 2-stats(3)] 0.000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.493000 t =	
AR roots AR roots R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha) AR roots R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) AR roots AR ro	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 33.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.964502 0.906978	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.970443 0.092221 8.767014 0.092221 8.767014 1.18170 0.943006	-2.596497 0.488977 0.488977 3.000000 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.0000000 -0.815538 0.053686 -15.19086 0.910468 SIC	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342 12.78216 8.076970	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310 6.077257 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats] d = 0.930264 0.031935 29.13037 P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000 0.188000 0.000000 0.0536000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(2)] 2-stats(2)] 2-stats(2)] 2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(3)] 0.000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.493000 t = 0.012000	0.000000
AR roots         MA roots        R²       D-W       US       alpha       se_alpha       t-stat(alpha)        AR roots         MA roots        P-W       Southwest       alpha       se_alpha       t-stat(alpha)        AR roots         MA roots         AR roots	13.81918 0.908804 0.835812 2.148459 314.7620 39.46172 7.976390 0.973354 0.997491 0.864778 1.813794 247.7865 7.438368 3.31195 0.808502 0.657712 1.754773 341.0616 29.44685 11.58228 0.944300 0.964502	<u>9.022379</u> 0.488977 0.488977 0.470643 0.166977 2.818616 0.966352 0.970443 0.970443 0.970443 0.092221 8.767014 0.092221 8.767014 1.18170 0.943006	-2.596497 0.488977 0.488977 0.488977 0.937356 0.029355 31.93220 0.463641 0.451549 SIC JB 1.000000 -0.815538 0.053686 -15.19086 0.910468	2.396330 9.264390 2.908669 <b>q</b> = -0.436102 0.145251 -3.002413 9.202308 0.458602 <b>q</b> = 7.295035 0.638795 <b>q</b> = 0.809642 0.063342 12.78216	min 3.000000 0.424501 0.183268 2.316281 max min 0.000000 0.000000 0.208508 0.034310 6.077257 max	P[Q-stats] d = -0.980222 0.046190 -21.22161 P[Q-stats] P[Q-stats] d = P[Q-stats]	0.002000 0.000000 -0.437103 0.146426 -2.985151 0.007000 0.000000 0.000000 0.000000 0.188000 0.000000 0.0536000	P[0 P[0 P[0 P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	2-stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(2)] 2-stats(3)] 0.000000 0.000000 0.stats(2)] 2-stats(3)] 0.000000	0.010000 0.027000 t = 0.002000 0.001000 0.002000 t = 0.188000 0.347000 0.347000 0.347000 0.347000 0.347000 0.012000 0.0493000	0.000000

Figure 136: Best ARMA models for non filtered data.

American											
Timencal		p =	1.000000	q =	1.000000	d =	0.000000	b = 0.0	00000	t =	1.000000
alpha	593.2849	-3.535029	0.671194	0.346384							
se_alpha			0.112386								
t-stat(alpha)		-5.453966	5.972250	2.400232							
	0.671194										
MA roots	0.346384										
R <sup>2</sup>	0.917817		SIC	9.335251		P[Q-stats]				0.728000	
D-W	1.985877		JB	6.799107	min	P[Q-stats]	0.095000			0.155000	
										0.247000	
Continental	5 40 50 47	p =	2.000000		1.000000	d =	0.000000	b = 0.0	00000	t =	1.000000
alpha			1.624996								
se_alpha			0.084832								
t-stat(alpha)		0.815820	19.15547	-7.939019	-40.74037						
MA roots	0.973604	0.015020									
R <sup>2</sup>	0.716003		SIC	9.376505	max	P[Q-stats]	0.525000	PIO-sta	ats(1)]	0.006000	
D-W	2.015614		JB	1.977543		P[Q-stats]				0.017000	
0 11	2.010014		00	1.577040			0.000000			0.040000	
Delta		p =	1.000000	a =	1.000000	= b	0.000000	b = 0.0		t =	1.000000
alpha	462.6359		0.705859			~					
se_alpha			0.085449								
			8.260588								
AR roots	0.705859										
MA roots	0.493513										
R <sup>2</sup>	0.907808		SIC	8.832874			0.378000			0.267000	
D-W	1.983053		JB	0.712007	min	P[Q-stats]	0.053000	P[Q-sta	ats(2)]	0.130000	
										0.252000	
Northwest			4.000000		3.000000		0.000000			t =	1.000000
alpha								1.267999 0.8			
se_alpha								0.126274 0.0			
					-3.501584	3.501986	15.61875	10.04164 11.	13032		
AR roots			0.955920	0.482131							
MA roots		0.923287		0.40407			0.000000	DIO 1	1-(4)]	0.450000	
R <sup>2</sup>	0.954315		SIC	8.404671		P[Q-stats]				0.158000	
D-W	1.895132		JB	5.503595	min	P[Q-stats]	0.158000			0.334000 0.393000	
United		p =	0.000000	~	2.000000	d =	0.000000		00000	<u>0.393000</u> t =	1.000000
alpha	520 7252		1.052495		2.000000	u =	0.000000	D = 0.0	00000	τ=	1.000000
se_alpha			0.107265								
			9.812121								
AR roots	00.20000	0.044014	5.012121	5.204040							
MA roots	0.753117	0 752117									
R <sup>2</sup>		0.755117		9.192407							
	0.836502	0.755117	SIC	9.192407	max	P[Q-stats]	0.131000	PIQ-sta	ats(1)]	0.062000	
D-W		0.755117	SIC JB	1.109041						0.062000	
	0.836502	0.755117				P[Q-stats] P[Q-stats]		P[Q-sta	ats(2)]	0.062000 0.058000 0.046000	
	0.836502	p=				P[Q-stats]	0.013000	P[Q-sta P[Q-sta	ats(2)]	0.058000	1.000000
D-W	0.836502 1.858286	p =	JB	1.109041 q =	min	P[Q-stats]	0.013000	P[Q-sta P[Q-sta	ats(2)] ats(3)]	0.058000 0.046000	1.000000
D-W US alpha se_alpha	0.836502 1.858286 465.1703 12.42576	p = -2.064267 0.327728	JB 0.000000 1.007156 0.073972	1.109041 <u>q =</u> 0.611885 0.053711	min	P[Q-stats]	0.013000	P[Q-sta P[Q-sta	ats(2)] ats(3)]	0.058000 0.046000	1.000000
D-W US alpha se_alpha <u>t-stat(alpha)</u>	0.836502 1.858286 465.1703 12.42576	p = -2.064267 0.327728	JB 0.000000 1.007156 0.073972	1.109041 <u>q =</u> 0.611885 0.053711	min	P[Q-stats]	0.013000	P[Q-sta P[Q-sta	ats(2)] ats(3)]	0.058000 0.046000	1.000000
D-W US alpha se_alpha <u>t-stat(alpha)</u>  AR roots	0.836502 1.858286 465.1703 12.42576 37.43596	p = -2.064267 0.327728 -6.298722	JB 0.000000 1.007156 0.073972	1.109041 <u>q =</u> 0.611885 0.053711	min	P[Q-stats]	0.013000	P[Q-sta P[Q-sta	ats(2)] ats(3)]	0.058000 0.046000	1.000000
D-W alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231	p = -2.064267 0.327728 -6.298722	JB 0.000000 1.007156 0.073972 13.61534	1.109041 <u>q =</u> 0.611885 0.053711 11.39222	min 2.000000	P[Q-stats]	0.013000	P[Q-staP[Q-stab = 0.0	ats(2)] ats(3)] 00000	0.058000 0.046000 t =	1.000000
D-W US alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup>	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305	p = -2.064267 0.327728 -6.298722	JB 0.000000 1.007156 0.073972 13.61534 SIC	1.109041 <b>q =</b> 0.611885 0.053711 11.39222 8.898536	min 2.000000 max	P[Q-stats] d = P[Q-stats]	0.013000 0.000000 0.514000	P[Q-sta P[Q-sta b = 0.0	ats(2)] ats(3)] 00000 ats(1)]	0.058000 0.046000 t = 0.514000	1.000000
D-W alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231	p = -2.064267 0.327728 -6.298722	JB 0.000000 1.007156 0.073972 13.61534	1.109041 <u>q =</u> 0.611885 0.053711 11.39222	min 2.000000 max	P[Q-stats]	0.013000 0.000000 0.514000	P[Q-sta P[Q-sta b = 0.0	ats(2)] ats(3)] 00000 ats(1)] ats(2)]	0.058000 0.046000 t = 0.514000 0.171000	1.000000
D-W alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305	p = -2.064267 0.327728 -6.298722 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB	1.109041 <u>q</u> = 0.611885 0.053711 11.39222 8.898536 0.198258	min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000	P[Q-sta P[Q-sta b = 0.0 P[Q-sta P[Q-sta P[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000	
D-W US alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299	p = -2.064267 0.327728 -6.298722 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000	1.109041 <u>q</u> = 0.611885 0.053711 11.39222 8.898536 0.198258	min 2.000000 max	P[Q-stats] d = P[Q-stats]	0.013000 0.000000 0.514000	P[Q-sta P[Q-sta b = 0.0 P[Q-sta P[Q-sta P[Q-sta	ats(2)] ats(3)] 00000 ats(1)] ats(2)]	0.058000 0.046000 t = 0.514000 0.171000	1.000000
D-W US alpha se_alpha t-stat(alpha)  AR roots] R <sup>2</sup> D-W Southwest alpha	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432	p = -2.064267 0.327728 -6.298722 0.782231 p = 0.905507	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742	1.109041 <u>q</u> = 0.611885 0.053711 11.39222 8.898536 0.198258	min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000	P[Q-sta P[Q-sta b = 0.0 P[Q-sta P[Q-sta P[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000	
D-W US alpha se_alpha <u>t-stat(alpha)</u>  AR roots  IMA roots  R <sup>2</sup> D-W Southwest alpha se_alpha	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989	p = -2.064267 0.327728 -6.298722 0.782231 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208	1.109041 <u>q</u> = 0.611885 0.053711 11.39222 8.898536 0.198258	min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000	P[Q-sta P[Q-sta b = 0.0 P[Q-sta P[Q-sta P[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000	
D-W US alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989	p = -2.064267 0.327728 -6.298722 0.782231 p = 0.905507	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208	1.109041 <u>q</u> = 0.611885 0.053711 11.39222 8.898536 0.198258	min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000	P[Q-sta P[Q-sta b = 0.0 P[Q-sta P[Q-sta P[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000	
D-W US alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha <u>t-stat(alpha)</u>  AR roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182	p = -2.064267 0.327728 -6.298722 0.782231 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208	1.109041 <u>q</u> = 0.611885 0.053711 11.39222 8.898536 0.198258	min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000	P[Q-sta P[Q-sta b = 0.0 P[Q-sta P[Q-sta P[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000	
D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   MA roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742	p = -2.064267 0.327728 -6.298722 0.782231 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q =	min 2.000000 max min 1.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d =	0.013000 0.000000 0.514000 0.011000 0.000000	P[Q-staP[Q-stab = 0.0 P[Q-staP[Q-staP[Q-stab = 0.0	ats(2)] ats(3)] 00000 ats(1)] ats(2)] ats(2)] ats(3)] 00000	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t =	
D-W US alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> R <sup>2</sup>	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806	p = -2.064267 0.327728 -6.298722 0.782231 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q = 7.120740	min 2.000000 max min 1.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000	P[Q-staP[Q-staD = 0.0 $P[Q-staP[Q-staD = 0.0$ $P[Q-staD = 0.0$	ats(2)] ats(3)] 00000 ats(1)] ats(2)] ats(2)] ats(3)] 00000 ats(1)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000	
D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   MA roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742	p = -2.064267 0.327728 -6.298722 0.782231 0.782231	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q =	min 2.000000 max min 1.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d =	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000	
D-W alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W R <sup>2</sup> D-W	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806	p = -2.064267 0.327728 -6.298722 0.782231 0.782231 p = 0.905507 0.144790 6.253938	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q = 7.120740 1.609048	min 2.000000 max min 1.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000 0.134000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.221000	1.000000
D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  IMA roots  R <sup>2</sup> D-W Av. fares	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143	p = -2.064267 0.327728 -6.298722 0.782231 0.905507 0.144790 6.253938	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q = 7.120740 1.609048 q =	min 2.000000 max min 1.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000 0.134000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000	
D-W US alpha se_alpha <u>t-stat(alpha)</u>  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha <u>t-stat(alpha)</u>  AR roots  R <sup>2</sup> D-W Av. fares alpha	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143	p = -2.064267 0.327728 -6.298722 0.782231 0.782231 0.905507 0.144790 6.253938 -2.553938	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q = 7.120740 1.609048 q = 0.994654	min 2.000000 max min 1.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000 0.134000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.221000	1.000000
D-W US alpha se_alpha <u>i-stat(alpha</u> ) JAR roots] R <sup>2</sup> D-W Southwest alpha se_alpha <u>i-stat(alpha</u> ) JAR roots] R <sup>2</sup> D-W Av. fares alpha se_alpha se_alpha	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143 472.9621 15.18855	p = -2.064267 0.327728 -6.298722 0.782231 0.782231 0.144790 6.253938 -2.552314 0.309422	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027 0.062126	1.109041 <b>q</b> = 0.611885 0.053711 11.39222 8.898536 0.198258 <b>q</b> = 7.120740 1.609048 <b>q</b> = 0.994654 0.083156	min 2.000000 max min 1.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000 0.134000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.221000	1.000000
D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143 472.9621 15.18855	p = -2.064267 0.327728 -6.298722 0.782231 0.782231 0.144790 6.253938 -2.552314 0.309422	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027	1.109041 <b>q</b> = 0.611885 0.053711 11.39222 8.898536 0.198258 <b>q</b> = 7.120740 1.609048 <b>q</b> = 0.994654 0.083156	min 2.000000 max min 1.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000 0.134000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.221000	1.000000
D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) t-stat(alpha) [AR roots] R <sup>2</sup> D-W	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143 472.9621 15.18855 31.13939	p = -2.064267 0.327728 -6.298722 0.782231 0.905507 0.144790 6.253938 -2.552314 0.309422 -8.248660	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027 0.062126	1.109041 <b>q</b> = 0.611885 0.053711 11.39222 8.898536 0.198258 <b>q</b> = 7.120740 1.609048 <b>q</b> = 0.994654 0.083156	min 2.000000 max min 1.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.000000 0.134000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)] 000000 ats(1)] ats(2)] ats(3)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.221000	1.000000
D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143 472.9621 15.18855 31.13939	p = -2.064267 0.327728 -6.298722 0.782231 0.782231 0.144790 6.253938 -2.552314 0.309422	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027 0.062126	1.109041 <b>q</b> = 0.611885 0.053711 11.39222 8.898536 0.198258 <b>q</b> = 7.120740 1.609048 <b>q</b> = 0.994654 0.083156	min 2.000000 max min 1.000000 max min 2.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.990000 0.134000 0.000000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ts(2)] ts(3)] 00000 ats(1)] ats(2)] ts(3)] 00000 ats(1)] ats(2)] ts(3)] 00000	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.221000	1.000000
D-W US alpha se_alpha <u>t-stat(alpha</u> ) IAR roots  IMA roots  R <sup>2</sup> D-W Southwest alpha se_alpha <u>t-stat(alpha</u> ) IAR roots  IMA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha) IAR roots  IMA roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143 472.9621 15.18855 31.13939 0.997323	p = -2.064267 0.327728 -6.298722 0.782231 0.905507 0.144790 6.253938 -2.552314 0.309422 -8.248660	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027 0.062126 25.20711	1.109041 <b>q</b> = 0.611885 0.053711 11.39222 8.898536 0.198258 <b>q</b> = 7.120740 1.609048 <b>q</b> = 0.994654 0.083156 11.96123	min 2.000000 max min 1.000000 max min 2.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d =	0.013000 0.000000 0.514000 0.011000 0.000000 0.990000 0.134000 0.000000 0.000000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ts(2)] ts(3)] 000000 ats(1)] ats(2)] ats(3)] 00000 ats(1)] ats(3)] 00000 ats(1)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.288000 t =	1.000000
D-W alpha se_alpha <u>t-stat(alpha)</u>  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha <u>t-stat(alpha)</u> AR roots   MA roots  AR roots  JAR roots	0.836502 1.858286 465.1703 12.42576 37.43596 0.782231 0.884305 2.147299 198.7432 6.502989 30.56182 0.542742 0.733806 1.722143 472.9621 15.18855 31.13939 0.997323 0.912782	p = -2.064267 0.327728 -6.298722 0.782231 0.905507 0.144790 6.253938 -2.552314 0.309422 -8.248660	JB 0.000000 1.007156 0.073972 13.61534 SIC JB 0.000000 0.542742 0.138208 3.927000 SIC JB 0.000000 1.566027 0.062126 25.20711 SIC	1.109041 q = 0.611885 0.053711 11.39222 8.898536 0.198258 q = 7.120740 1.609048 q = 0.994654 0.083156 11.96123 7.871818	min 2.000000 max min 1.000000 max min 2.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] d = P[Q-stats]	0.013000 0.000000 0.514000 0.011000 0.000000 0.990000 0.134000 0.000000 0.000000	P[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-staP[Q-sta	ts(2)] ts(3)] 00000 ats(1)] ats(2)] ats(3)] 00000 ats(2)] ats(3)] 00000 ats(1)] ats(2)]	0.058000 0.046000 t = 0.514000 0.171000 0.275000 t = 0.134000 0.221000 0.288000 t = 0.115000	1.000000

Figure 137: Best ARMA models for filtered data with the use of a trend variable.

se_alpha t-stat(alpha) 5  AR roots  C  MA roots  C R <sup>2</sup> C D-W 1 Continental alpha 4 se_alpha 2 t-stat(alpha) 4  AR roots  C R <sup>2</sup> C D-W 2 D-W 2 Delta alpha 4 se_alpha 1	9.954581 53.84805 0.836501 0.798486 0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	12.95449	0.142610 10.75293 0.701960 SIC JB 0.000000 0.940090	0.195948	max	-1.014149 0.168547	0.154672 4.122128		1.000000	t =	0.000000
se_alpha t-stat(alpha) 5  AR roots  C  MA roots  C R <sup>2</sup> C D-W 1 Continental alpha 4 se_alpha 2 t-stat(alpha) 4  AR roots  C R <sup>2</sup> C D-W 2 D-W 2 Delta alpha 4 se_alpha 1	9.954581 53.84805 0.836501 0.798486 0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	12.95449 -10.05680 0.836501 0.798486 	0.142610 10.75293 0.701960 SIC JB 0.000000 0.940090	0.195948 -6.549824 9.263774 11.11698	0.109847 4.471542 max	0.168547 -6.017027 P[Q-stats]	0.154672 4.122128				
se_alpha t-stat(alpha) 5  AR roots  C  MA roots  C R <sup>2</sup> C D-W 1 Continental alpha 4 se_alpha 2 t-stat(alpha) 4  AR roots  C R <sup>2</sup> C D-W 2 D-W 2 Delta alpha 4 se_alpha 1	9.954581 53.84805 0.836501 0.798486 0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	12.95449 -10.05680 0.836501 0.798486 	0.142610 10.75293 0.701960 SIC JB 0.000000 0.940090	0.195948 -6.549824 9.263774 11.11698	0.109847 4.471542 max	0.168547 -6.017027 P[Q-stats]	0.154672 4.122128				
t-stat(alpha)         £            AR roots          C            MA roots          C           R2         C           D-W         1           Continental         alpha           alpha         4           se_alpha         4           IAR roots          C           IAR roots          C           DAR roots          C           IAR roots          C           R2         C           D-W         2           D-W         2           Delta         alpha           alpha         4           se_alpha         4	53.84805 0.836501 0.798486 0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	-10.05680 0.836501 0.798486 <b>p =</b> -51.42751 13.91948	10.75293 0.701960 SIC JB 0.000000 0.940090	-6.549824 9.263774 11.11698	4.471542 max	-6.017027 P[Q-stats]	4.122128				
AR roots      C        MA roots      C       R²     C       D-W     1       alpha     4       se_alpha     4        AR roots      C       R²     C       D-W     2       D-W     2       D-W     2       Delta     alpha       alpha     4	0.836501 0.798486 0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	0.836501 0.798486 <b>p =</b> -51.42751 13.91948	0.701960 SIC JB 0.000000 0.940090	9.263774 11.11698	max	P[Q-stats]					
IMA roots         C           R²         C           D-W         1           Continental         alpha           alpha         4           se_alpha         4           IAR roots         C           R²         C           OD-W         2           Par roots         C           D-W         2           Delta         alpha           alpha         4           se_alpha         4	0.798486 0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	0.798486 p = -51.42751 13.91948	SIC JB 0.000000 0.940090	11.11698			0.778000				
R <sup>2</sup> D-W 1 Continental alpha 4 se_alpha 5 t-stat(alpha) 4  AR roots   MA roots  0 R <sup>2</sup> 0 D-W 2 Delta alpha 4 se_alpha 4 se_alph	0.936769 1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	p = -51.42751 13.91948	JB 0.000000 0.940090	11.11698			0.778000				
D-W 1 Continental alpha 4 se_alpha 5 t-stat(alpha) 4  AR roots   MA roots  0 R <sup>2</sup> 0 D-W 2 Delta alpha 4 se_alpha 4	1.799072 463.9405 9.934567 46.69962 0.753209 0.739066	-51.42751 13.91948	JB 0.000000 0.940090	11.11698			0.778000		0 -1 -1 - (4)1	0.040000	
Continental       alpha       alpha       se_alpha       t-stat(alpha)        AR roots         MA roots        C       R <sup>2</sup> D-W       2       Delta       alpha       alpha       se_alpha	463.9405 9.934567 46.69962 0.753209 0.739066	-51.42751 13.91948	0.000000		min	PI()-statel			Q-stats(1)]		
alpha 4 se_alpha 9  AR roots  0 R <sup>2</sup> 0 D-W 2 Delta alpha 4 se_alpha 1	9.934567 46.69962 0.753209 0.739066	-51.42751 13.91948	0.940090	<u>q =</u>			0.040000		Q-stats(2)]		
alpha 4 se_alpha 9  AR roots  0 R <sup>2</sup> 0 D-W 2 Delta alpha 4 se_alpha 1	9.934567 46.69962 0.753209 0.739066	-51.42751 13.91948	0.940090	q =					Q-stats(3)]		
se_alpha s t-stat(alpha) 4  AR roots   MA roots  0 R <sup>2</sup> 0 D-W 2 Delta alpha 4 se_alpha 1	9.934567 46.69962 0.753209 0.739066	13.91948			2.000000	d =	0.000000	b =	1.000000	t =	0.000000
t-stat(alpha) 4  AR roots   MA roots  0 R <sup>2</sup> 0 D-W 2 Delta alpha 4 se_alpha 1	46.69962 0.753209 0.739066		0 077040	0.567324							
AR roots MA roots C D-W 2 Delta alpha 4 se_alpha	0.753209 0.739066	-3.694642	U.U//616	0.083775							
IMA rootsiCR2CD-W2Delta4alpha4se_alpha1	0.739066		12.11209	6.771970							
IMA rootsiCR2CD-W2Delta4alpha4se_alpha1	0.739066										
R²     C       D-W     2       Delta     2       alpha     4       se_alpha     1	0.739066	0.753209									
D-W 2 Delta alpha 4 se_alpha 1			SIC	9.350545	max	P[Q-stats]	0.000000	PI	Q-stats(1)]	0.000000	
Delta alpha 4 se_alpha 1	2.121524		JB	2.325072		P[Q-stats]			Q-stats(2)]		
alpha 4 se_alpha 1	2.121524		50	2.525072		[@-31813]	0.000000		Q-stats(2)]		
alpha 4 se_alpha 1		-	0.000000	~	2 000000	ط	0.000000				0.000000
se_alpha 1	400 7700		0.000000		3.000000	u =	0.000000	D =	1.000000	t =	0.000000
		-53.97678									
		15.94027									
t-stat(alpha) 3	34.91588	-3.386190	13.21755	9.660275	5.089788						
AR roots											
		0.812360									
R <sup>2</sup> (	0.912791		SIC	9.009704	max	P[Q-stats]	0.383000	P[0	Q-stats(1)]	0.010000	
D-W 2	2.010130		JB	0.045651	min	P[Q-stats]	0.010000		Q-stats(2)]		
									Q-stats(3)]		
Northwest		p =	0.000000	a =	2.000000	d =	0.000000		1.000000		0.000000
	501,4677	-88.03957						~			
		12.31818									
t-stat(alpha) 5											
IAR roots	00.01021	1.17/122	10.40307	0.000211							
	0 707007	0 707007									
		0.797287	010	0.007004			0.440000	DI	2 - 1 - 1 - (4)1	0.440000	
	0.898308		SIC	8.987061		P[Q-stats]			Q-stats(1)]		
D-W 1	1.800074		JB	10.11324	min	P[Q-stats]	0.006000		Q-stats(2)]		
									<u>Q-stats(3)]</u>		
United		p =	0.000000		2.000000	d =	0.000000	b =	1.000000	t =	0.000000
		-77.86129									
se_alpha	9.798012	13.35465	0.092880	0.092301							
t-stat(alpha) 5	51.65446	-5.830275	11.46275	7.293217							
AR roots											
	0.820470	0.820470									
	0.847939		SIC	9.119888	max	P[Q-stats]	0.668000	PI	Q-stats(1)]	0.256000	
	1.981516		JB	4.486529		P[Q-stats]			Q-stats(2)]		
							2		Q-stats(3)]		
US		p =	0.000000	q =	2.000000	d =	0.000000	b =			0.000000
	128 2452	-64.92823			2.000000	u =	0.000000	0=	1.000000		0.000000
		12.14641									
t-stat(alpha) 4	49.20672	-0.340468	14.4//68	11.58860							
AR roots		o ==== o :									
		0.777984									
	0.869696		SIC	9.017450		P[Q-stats]			Q-stats(1)]		
D-W 2	2.157277		JB	1.029562	min	P[Q-stats]	0.071000		Q-stats(2)]		
									Q-stats(3)]	0.477000	
Southwest		p =	0.000000	q =	1.000000	d =	0.000000	b =	1.000000	t =	0.000000
alpha 2	227.4043	14.78263	0.665652								
		5.285021									
		2.797081									
AR roots										· · · · · · · · · · · · · · · · · · ·	
	0.665652										
	0.582633		SIC	7.570481	mov	P[Q-stats]	0.852000	DI	Q-stats(1)]	0.004000	
									Q-stats(1)]		
D-W 1	1.370375		JB	1.442743	min	P[Q-stats]	0.004000			0.017000	
A 6.			0.000000		0.000000		0.000000		Q-stats(3)]	0.016000	0.000000
Av. fares	105 655	p =	0.000000	= p	2.000000	d =	0.000000	b =	1.000000	t =	0.000000
		-59.84282									
		9.674431									
	46.64588	-6.185668	11.58440	7.807508							
AR roots											
	0.864859	0.864859									
	0.898424		SIC	8.024214	max	P[Q-stats]	0.122000	PI	Q-stats(1)]	0.122000	
	2.113458		JB	4.476622		P[Q-stats]			Q-stats(2)]		
							2.000000		Q-stats(3)]		
D-VV 2								1.16	ແ ວເຜເວ(ປ/]	5.110000	

Figure 138: Best ARMA models for filtered data with the use of a dummy variable at period 35.

American         p = 3.000000         q = 0.000000         d = 0.000000         b = 0.000000         t = 0.001           aipha         31009         1.05713         0.115644         0.118074         0.55544         0.118074           tstatidpha         30090         1.0677         0.175544         0.118074         0.559530           IAR rootsl         0.969058         4.70027         2.86994         2.895530         0.000000         P[Q-stats]         0.21000         P[Q-stats]         0.241000         P[Q-stats]         0.200000         P[Q-stats]         0.20000         P[Q-stats]         0.200000         P[Q-stats]         0.20000         P[Q-stats]         0.200000         P[Q-stats]
se. atpha         123.3027         0.124757         0.175544         0.118374           testat(a)na         3096053         4.70007         2.669630         Cebeson           RR         0.97653         SIC         9.328462         max P(Q-stats]         0.108000         P[Q-stats(2)]         0.241000           D-W         2.015333         JB         1.389676         min P[Q-stats]         0.108000         tel         0.000000         tel         0.00000 </td
Lstaticiphal         3.090693         8.470207         2.686904         2.695930           IAR rootsi         0.917633         SIC         9.328462         max P[Q-stats]         0.629000         P[Q-stats](2)         0.41000           D-W         2.015333         JB         1.389676         min P[Q-stats]         0.108000         P[Q-stats](2)         0.41000           Consinental         p.p.         1.000000         q.         0.000000         L         0.000000         L         0.000000           Se, alpha         14.35092         0.073432
IAR rootsi MA rootsi R <sup>2</sup> 0.947633         SiC         9.328462         max P[Q-stats]         0.629000         P[Q-stats(1)]         0.108000         P[Q-stats(2)]         0.241000           D-W         2.017633         JB         1.389676         min P[Q-stats]         0.108000         P[Q-stats(2)]         0.241000           alpha         431.1574         0.773432         q         0.000000         d         0.000000         b         0.000000         t         0.000           Rev         0.660123         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats(1)]         0.751000           P-W         1.837109         0.660123         SIC         9.380507         max P[Q-stats]         0.020000         b=         0.00000         t=         0.000           Belta         p=         3.000000         q=         2.002000         d=         0.00000         b=         0.00000         t=         0.000           Ibits         p=         3.000000         q=         2.002080         0.863044         [Q-stats(1)]         0.02600         F[Q-stats(2)]         0.863044           Jainta         1.61261         3.11357         0.382309         0.027600         P[Q-stats(2)]         0.02600<
IMA rootsi R2         0.917633         SIC         9.328462         max P[Q-stats]         0.629000         P[Q-stats(1)]         0.108000         P[Q-stats(2)]         0.241000           Continental         p =         1.000000         q =         0.000000         d =         0.000000         b =         0.00000         t =         0.00           Gentinental         p =         1.000000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.00           IgAT         0.660123         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats(2)]         0.881000         P[Q-stats(3)]         0.029000         t =         0.00000         t =         0.000000         t =         0.00000
R2         0.917633         SiC         9.328462         max P[Q-stats]         0.629000         P[C-stats[2]]         0.241000           D-W         2.015383         JB         1.389676         min P[Q-stats]         0.108000         P[C-stats[2]]         0.241000           alpha         431.1574         0.773432         0.415000         d=         0.000000         b=         0.000000         t=         0.001           R         0.660123         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats(1)]         0.751000           P-W         1.837109         JB         5.986324         min P[Q-stats]         0.281000         P[Q-stats(2]]         0.881000           D-W         1.837109         JB         5.986324         0.428687         0.428687         0.881000         P[Q-stats(2]]         0.881000           D-W         1.837109         0.13157         0.094230         0.13680         0.13550         0.132000           Estatiatignal         1.1774         77.4232         0.88000         P[Q-stats(3]         0.22800         1         0.00000         1         0.00000         1         0.00000         1         0.00000         1         0.000         1         0.00000 <th< td=""></th<>
D-W         2.015383         JB         1.389676         min P[Q-stats]         0.100000         P[Q-stats]2]         0.241000           Continental         D =         1.000000         q =         0.000000         d =         0.000000         b =         0.000000         1 =         0.000           alpha         43.1574         0.773432         0.77342         0.77342         0.00000         q =         0.000000         p =         0.000000         p =         0.000000         p =         0.00000         t =         0.000000         t =         0.000000
$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$
Continental         p =         1.000000         q =         0.000000         b =         0.000000         t =         0.000           se_alpha         14.35092         0.077432
alpha         431.1574         0.773432           se.alpha         143.0502         0.070481           Lstaticiphal         30.04388         10.97355           JAR rootsi         0.660123         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats/1)         0.751000           D-W         1.837109         JB         5.986324         min P[Q-stats]         0.020000         be         0.000000         t=         0.000000         t=         0.000000         be         0.000000         t=         0.0000000         t=
se. alpha         14.35092         0.070481           i-statidpha         0.04388         0.97355           IAR rootsi         0.773452           IAR rootsi         0.770492         0.881000         P[O-stats(1)]         0.751000           D-W         1.837109         JB         5.986324         min P[O-stats]         0.881000         P[O-stats(2)]         0.881000           abpla         378.8326         0.380180         0.476863         0.447871         0.97860           se. alpha         26.7139         0.179860         0.11950         0.099760         0.97860           I-statidipha         14.17741         7.742305         6.167449         7.758092         3.898309         8.683040           I-AR rootsi         0.922503         0.922803         0.92630         0.922809         P[O-stats(2)]         0.085000           R*         0.905418         SIC         8.79917         max P[O-stats]         0.90000         t=         0.000           JAR rootsi         0.921803         0.921803         0.321803         1.87863         min P[O-stats]         0.90000         t=         0.000           JAR rootsi         0.774354         JAR rootsi         0.7743569         R*         0.917107         <
t-staticiphel         30.04388         10.97355           IAR rootsi         0.60773432         0.60723         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats(2)]         0.881000           D-W         1.837109         JB         5.986324         min P[Q-stats]         0.000000         b         0.0
IAR rootsi IMA rootsi D-W         0.773432           Detta         p = 3.000000         q = 2.000000         d = 0.000000         p[Q-stats(1)]         0.751000           Detta         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.000           alpha         379.8326         0.836018 - 0.811370         0.769838         0.426887         0.849721           se_alpha         26.791205         6.167449         7.756082         0.838009         6.633400           PAR rootsi         0.921803 <td< td=""></td<>
IMA rootsi R²         O E60123 0.02000         SiC         9.380507         max P[Q-stats]         0.881000 0.29000         P[Q-stats(1)]         0.751000           D-W         1.837109         JB         5.986324         min P[Q-stats]         0.000000         P[Q-stats(2)]         0.881000           Deta         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.000           alpha         26.79139         0.107800         0.131557         0.090230         0.1026830         0.821803         0.20000         t = 0.000           H-stat(alph)         14.17741         7.742305-6.6174449         7.758092         3.898309         8.683040           R*         0.9025418         SiC         8.799172         max P[Q-stats]         0.935000         P[Q-stats(1)]         0.0268000           Northwest         p = 3.000000         q = 1.000000         d = 0.000000         b = 0.000000         t = 0.000000         t = 0.000000           alpha         316.1128         1.381132-0.807099         0.404651         0.743569         0.000000         t = 0.000000
R²         0.660123         SIC         9.380507         max P[Q-stats]         0.881000         P[Q-stats(1)]         0.751000           D-W         1.837109         JB         5.986324         min P[Q-stats]         0.029000         P[Q-stats(2)]         0.81000         P[Q-stats(2)]         0.81000         P[Q-stats(2)]         0.81000         L         0.00000         t =         0.000000
D-W         1.837109         JB         5.986324         min P[Q-stats]         0.029000         P[Q-stats[2]]         0.81000           Detata         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         l = 0.000000           alpha         279.8326         0.86018         0.811370         0.769838         0.426887         0.849721           se_alpha         26.79139         0.107580         0.11557         0.099280         0.097860           I-stattalpha         14.17741         7.742305         c.6167449         7.758032         3.88309         8.633040           JAR         roots         0.926530         0.922830         0.922830         0.922830         0.922830         0.92000           PU         1.898956         JB         9.078859         min P[Q-stats]         0.026000         P[Q-stats(1)]         0.026000           PIO-stats         J.81132<-0.807990         0.404651         0.743052         1.898956         JB         0.07893         0.421610         1.300000           Northwest         p = 3.000000         q = 1.000000         d = 0.000000         b = 0.000000         t = 0.000000         t = 0.000000           R2         0.317107         SiC         8.765514         max P[Q-
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
Deta         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.000           alpha         26.79139         0.107980         0.101570         0.799230         0.489271         0.489271         0.489271         0.489271         0.489271         0.489271         0.489271         0.489270         0.499280         0.499280         0.489270         0.489210         0.42151         0.221803         0.521803         0.522500         0.522530         0.5922909         0.46151         0.521803         0.521825         0.535530         0.521803
alpha         379.8326         0.836018         0.769838         0.426887         0.44721           se_alpha         26.79139         0.107980         0.113557         0.099200         0.997800           IAR rootsi         0.921803         0.828530         0.82850         0.82850         0.82850         0.921803         0.82850         0.921803         0.82850         0.921803         0.0281803         0.82850         D.90000         P[Q-stats]         0.035000         P[Q-stats]         0.000000         D         D.2786         0.85000         P[Q-stats]         0.000000         L         0.000000         D         D         0.000000         L         0.000000         D         L         0.000000         D         D         0.000000         D
se_aipha         26.79139         0.107980         0.131557         0.099230         0.109506         0.097860           t-stat/alpha1         14.17741         7.742305         6.617449         7.758092         3.898309         8.683040           JAR rootsi         0.9221803         0.9221803         0.9221803         0.9221803         0.926110         0.00000         P[Q-stats]         0.026000         P[Q-stats]         0.026000         P[Q-stats]         0.026000         P[Q-stats]         0.03000         P[Q-stats]         0.03000         P[Q-stats]         0.03000         D         P[Q-stats]         0.03000         Te 0.000         abpa         3.013002         9.176753         4.211911         3.260439         5.682511         IAR roots]         0.73369         0.462235         6.42235         0.42235         IAR roots]         0.000000         P[Q-stats]         0.000000         I= 0.000         0.000000         I= 0.000         0.
t=startapha 14.17741         7.742305         6.167449         7.758092         3.898309         8.683040            AR roots]         0.928530         0.928530         0.892630         0.928530         0.928530         0.928530         0.928530         0.928530         0.928530         0.928530         0.928530         0.921803         PIC-stats[0]         0.002000         PIC-stats[2]         0.0085000         PIC-stats[2]         0.0085000         PIC-stats[2]         0.0085000         PIC-stats[2]         0.0085000         PIC-stats[2]         0.00000         t =         0.001         alpha         316.1128         1.381132         0.807099         0.404651         0.743569         FIC-stats[2]         0.000000         t =         0.00000         FIC-stats[2]         0.000000         FIC-stats[2]         0.000000         FIC-stats[2]         0.000000         PIC-stats[2]         0.000000         PIC-stats[2]         0.000000         FIC-stats[2]
IAR rootsi         0.928530         0.928300         0.921803           R²         0.905418         SIC         8.799172         max P[Q-stats]         0.035000         P[Q-stats(1)]         0.026000           D-W         1.898956         JB         9.078859         min P[Q-stats]         0.020000         P[Q-stats(2)]         0.085000           Northwest         p = 3.000000         q = 1.000000         d = 0.000000         b = 0.000000         t = 0.000           alpha         316.1128         1.381132         0.80799         0.40461         0.743569           se_alpha         90.23796         0.150503         0.191624         0.124109         0.130852           I-statalpha         3.03102         J.716753         4.211901         3.260439         5.682511           IAR rootsi         0.978919         0.642935         0.642935         0.642935         0.000000         P[Q-stats(1)]         0.000000           B?         Q.917107         SIC         8.765514         max P[Q-stats]         0.000000         b = 0.000000         t = 0.000           alpha         47.2741         0.677817         0.740817         0.77504         0.459692         0.826295         se_alpha         0.200000         t = 0.000         1 = 0.000 </td
IMA rootsi         0.921803         0.921803           R2         0.905418         SIC         8.799172         max P[Q-stats]         0.935000         P[Q-stats(2)]         0.08000           D-W         1.898956         JB         9.078859         min P[Q-stats]         0.026000         P[Q-stats(2)]         0.080000           Northwest         p = 3.000000         q = 1.000000         d = 0.000000         b = 0.000000         t = 0.001           alpha         316.1128         1.381132         0.80709         0.404651         0.743569           se_alpha         0.515030         0.19624         0.124109         0.130852           t-statalalpha         3.503102         9.176753         4.211901         3.260439         5.682511           IAA rootsi         0.978919         0.642935         0.642935         0.000000         P[Q-stats]         0.000000         P[Q-stats(2)]         0.000000           D-W         2.047965         JB         2.857827         min P[Q-stats]         0.000000         b = 0.000000         t = 0.000           alpha         447.2741         0.677811         0.77504         0.45892         0.826295         s = 0.000000         t = 0.0000         b = 0.000000         t = 0.00000         P[Q-stats(3)]
R²         0.905418         SIC         8.799172         max P[C+stats]         0.930000         P[C+stats(2)]         0.085000           Northwest         p =         3.00000         q =         1.00000         d =         0.00000         b =         0.00000         t =         0.00000           Northwest         p =         3.000000         q =         1.00000         d =         0.00000         b =         0.00000         t =         0.00000           IAm roots1         0.978919         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335           IAR roots1         0.978919         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335           IMA roots1         0.978919         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335           IMA roots1         0.978919         0.642335         0.642335         0.642335         0.642335         0.642335         0.642335           IMA roots1         0.978965         JB         2.857627         min P[C-stats]         0.000000         t =         0.000000         t =         0.00000 <t< td=""></t<>
D-W         1.898956         JB         9.078859         min P[Q-stats]         0.026000         P[Q-stats[2]]         0.085000           Northwest         p =         3.000000         q =         1.000000         d =         0.000000         t =         0.00000           alpha         316.1128         1.381132         0.807099         0.404651         0.743569         b =         0.000000         t =         0.00000           se_alpha         3.051102         9.176753         4.211901         3.208439         -5.682511           IAR rootsi         0.743569         R         0.0191624         0.124109         0.130852           R2         0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats(2])         0.000000           D-W         2.047965         JB         2.857827         min P[Q-stats]         0.000000         P[Q-stats(2])         0.00000         t =         0.00000           United         p =         3.000000         q =         2.00000         d =         0.000000         t =         0.00000           Listal(alpha]         447.2741         0.6778485         0.773564         0.482692         0.826255         0.277413         0.778298         0.424217
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
Introvest         p = 3.000000         q = 1.00000         d = 0.00000         b = 0.00000         t = 0.000           alpha         316.1128         1.381132         -0.807099         0.404651         -0.743569         .
alpha       316.1128       1.381132       -0.807099       0.404651       -0.743569         se_alpha       90.23796       0.150503       0.191624       0.124109       0.130852         I-stat(alpha)       3.503102       9.176753       -4.211901       3.260439       -5.682511         IAR rootsi       0.789819       0.642935       0.642935       0.642935       0.642935         R <sup>2</sup> 0.917107       SIC       8.765514       max P[Q-stats]       0.000000       P[Q-stats(2)]       0.000000         D-W       2.047965       JB       2.857827       min P[Q-stats]       0.000000       b       0.000000       t=       0.00000         United       p =       3.000000       q =       2.000000       d =       0.000000       b =       0.000000       t =       0.000         JAr zords       0.677710       70504       0.459692       0.826255       0.99997       0.103584       0.099808       0.106240       0.096300       t =       0.000       t =
se_alpha       90.23796       0.150503       0.191624       0.124109       0.130852         t-stat(alpha)       3.503102       9.176753       -4.211901       3.260439       -5.682511         IAR rootsi       0.978919       0.642935       0.642935       -         R2       0.917107       SIC       8.765514       max P[Q-stats]       0.000000       P[Q-stats(2)]       0.000000         D-W       2.047965       JB       2.857827       min P[Q-stats]       0.000000       P[Q-stats(2)]       0.000000         alpha       447.2741       0.677871       -0.740847       0.770504       0.459692       0.826295         se_alpha       12.55935       0.099997       0.103584       0.093980       0.106240       0.096000       t=       0.000         IAR rootsi       0.946938       0.946938       0.859274       max P[Q-stats]       0.976000       P[Q-stats(1)]       0.096000       P[Q-stats(2)]       0.174000         D-W       2.055159       JB       1.985714       min P[Q-stats]       0.909000       t=       0.000         alpha       392.7677       0.843125       0.639845       0.672718       1.078298       0.542170         se_alpha       10.902544       10.03867
t-stat(alpha)       3.503102       9.176753       4.211901       3.260439       -5.682511          AR rootsi       0.978919       0.642935       0.642935       0.000000       P[Q-stats(1)]       0.000000         D-W       2.047965       JB       2.857827       min P[Q-stats]       0.000000       P[Q-stats(2)]       0.000000         United       p =       3.000000       q =       2.000000       d =       0.000000       b =       0.000000         alpha       447.2741       0.677871       0.740817       0.770564       0.459692       0.826295       se_alpha       2.55935       0.099907       0.103584       0.00240       0.096300       -       -       0.000000       t =       0.000         IAR rootsi       0.999008       0.589274       imax P[Q-stats]       0.976000       P[Q-stats(1)]       0.096000       P[Q-stats(2)]       0.174000         D-W       2.055159       JB       1.985714       max P[Q-stats]       0.976000       P[Q-stats(2)]       0.174000         P[Q-stats(1)]       0.946938       0.659274       imax P[Q-stats]       0.996000       P[Q-stats(1)]       0.00000       t =       0.000         US       p =       0.000000       q =       5.000000
IAR roots         0.978919         0.642935           IMA roots         0.743569
IMA rootsi         0.743569           R²         0.917107         SIC         8.765514         max P[Q-stats]         0.000000         P[Q-stats(1)]         0.000000           United         p =         3.000000         q =         2.000000         d =         0.000000         P[Q-stats(3)]         0.000000           United         p =         3.000000         q =         2.000000         d =         0.000000         b =         0.000000         t =         0.00000           United         p =         3.000000         q =         2.000000         d =         0.000000         b =         0.000000         t =         0.00000           United         p =         3.000000         q =         2.000000         d =         0.000000         b =         0.00000         t =         0.000           Listat(alpha)         19.82655         6.778885         7.151852         8.19856         4.326906         8.580440           IAR rootsi         0.999008         0.999008         8.589274         min P[Q-stats]         0.976000         P[Q-stats(3)]         0.261000           U         2.055159         JB         1.985714         min P[Q-stats]         0.976000         P[Q-stats(3)]         0.261000      <
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
alpha         447.2741         0.677871         0.740817         0.770504         0.459692         0.826295           se_alpha         22.55935         0.099997         0.103584         0.093800         0.106240         0.096300           I-stat(alpha)         19.82655         6.7788585         7.151852         8.198566         4.326906         8.580440           IAR rootsi         0.946938         0.946938         0.859274         max P[Q-stats]         0.976000         P[Q-stats(1)]         0.096000           D-W         2.055159         JB         1.985714         min P[Q-stats]         0.976000         P[Q-stats(2)]         0.174000           US         p =         0.00000         q =         5.00000         d =         0.00000         t =         0.000           US         p =         0.00000         q =         5.00000         d =         0.00000         t =         0.000           US         p =         0.00867         0.053818         0.044884         0.079665         t =         0.000000         t =         0.000           I-Arta(alpha)         36.02544         10.05828         JB         0.535803         max P[Q-stats]         0.048000         P[Q-stats(1)]         0.014000
se_alpha         22.55935         0.099997         0.103584         0.093980         0.106240         0.096300           t-stat(alpha)         19.82655         6.778855         7.151852         8.198566         4.326906         8.580440            AR roots]         0.946938         0.946938         0.859274
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
IMA rootsi         0.909008         0.909008           R²         0.834814         SIC         9.179854         max P[Q-stats]         0.976000         P[Q-stats(1)]         0.096000           D-W         2.055159         JB         1.985714         min P[Q-stats]         0.096000         P[Q-stats(2)]         0.174000           US         p =         0.000000         q =         5.000000         d =         0.000000         b =         0.000000         t =         0.000           alpha         392.7677         0.843125         0.633845         0.672718         1.078298         0.542170           se_alpha         10.90251         0.083821         0.030867         0.053818         0.044884         0.079565           t-stat(alpha)         36.02544         10.05858         20.72897         12.49986         24.02425         6.814178           IAR rootsi         0.997421         0.997421         0.927401         0.633642         P[Q-stats]         0.048000         P[Q-stats(1)]         0.014000           P-W         1.758185         JB         0.535803         min P[Q-stats]         0.048000         P[Q-stats(2)]         0.048000           P[Q-stats(3)]         0.000000         q =         0.000000         d
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
alpha         392.7677         0.843125         0.639845         0.672718         1.078298         0.542170           se_alpha         10.90251         0.083821         0.030867         0.053818         0.044884         0.079565           t-stat(alpha)         36.02544         10.05858         20.72897         12.49986         24.02425         6.814178            AR roots
se_alpha         10.90251         0.083821         0.030867         0.053818         0.044884         0.079565           t-stat(alpha)         36.02544         10.05858         20.72897         12.49986         24.02425         6.814178           IAR roots          0.997421         0.997421         0.927401         0.633642         Pice
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
$\begin{array}{  l l l l l l l l l l l l l l l l l l $
IMA roots         0.997421         0.997421         0.927401         0.633642           R <sup>2</sup> 0.892250         SIC         8.955838         max P[Q-stats]         0.048000         P[Q-stats(1)]         0.014000           D-W         1.758185         JB         0.535803         min P[Q-stats]         0.00000         P[Q-stats(2)]         0.048000           Southwest         p =         1.00000         q =         0.00000         d =         0.00000         b =         0.00000         t =         0.000           Southwest         p =         1.00000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.000           Iapha         242.5268         0.812377         se_alpha         7.462084         0.092025         t =         0.00000         t =         0.000         t =         0.000           IAR rootsi         0.812377
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
D-W         1.758185         JB         0.535803         min P[Q-stats]         0.000000         P[Q-stats(2)]         0.048000           Southwest         p =         1.00000         q =         0.000000         d =         0.000000         b =         0.000000           Southwest         p =         1.00000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.000           Southwest         p =         1.000000         q =         0.000000         d =         0.000000         b =         0.000000         t =         0.000           alpha         242.5268         0.812377         se_alpha         7.462084         0.092025         se_alpha         7.462084         0.092025         se_alpha         0.812377           JAR rootsl         0.812377         0.812377         0.812377         0.812377         0.242000         P[Q-stats(1)]         0.242000         P[Q-stats(2)]         0.391000         P[Q-stats(2)]         0.391000         P[Q-stats(2)]         0.391000         P[Q-stats(2)]         0.391000         P[Q-stats(2)]         0.505000         P[Q-stats(2)]         0.505000         P[Q-stats(2)]         0.505000         P[Q-stats(2)]         0.505000         P[Q-stats(2)]         0.50
Southwest         p =         1.00000         q =         0.00000         description         description
$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$
alpha         242.5268         0.812377           se_alpha         7.462084         0.092025           t-stat(alpha)         32.50122         8.827793           JAR roots]         0.812377           IMA roots]         0.812377           D-W         1.796068         SIC         7.252009         max P[Q-stats]         0.999000         P[Q-stats(1)]         0.242000           P-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           P(Q-stats)         0.99000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.0000
se_alpha         7.462084         0.092025           t-stat(alpha)         32.50122         8.827793            AR roots
t-stat(alpha)         32.50122         8.827793            AR roots          0.812377            MA roots          0.660816         SIC         7.252009         max P[Q-stats]         0.999000         P[Q-stats(1)]         0.242000           P-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p = 3.00000         q = 2.00000         d = 0.000000         b = 0.000000         t = 0.0000
IAR roots  IMA roots          0.812377           IMA roots          R <sup>2</sup> 0.660816         SIC         7.252009         max P[Q-stats]         0.999000         P[Q-stats(1)]         0.242000           D-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p = 3.00000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.0000
Image: Marcots         Pice
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $
D-W         1.796068         JB         0.559358         min P[Q-stats]         0.242000         P[Q-stats(2)]         0.391000           Av. fares         p = 3.00000         q = 2.00000         d = 0.000000         b = 0.000000         t = 0.000
P[Q-stats(3)]         0.505000           Av. fares         p = 3.000000         q = 2.000000         d = 0.000000         b = 0.000000         t = 0.000
Av. fares p = 3.000000 q = 2.000000 d = 0.000000 b = 0.000000 t = 0.000
aipha 1001.0100 0.001010 -0.020000 0.010011 0.200011 0.300000
se_alpha 29.42788 0.073421 0.051561 0.063025 0.030858 0.028717
se_apria 23-42706 0.075421 0.001501 0.005002 0.0050606 0.020717 t-stat(a)pha) 11.27752 11.40794 -15.91456 12.90081 6.608099 32.51844
AR roots  0.943393 0.943393 0.913573
IMA rootsi 0.966353 0.966353
R2         0.906410         SIC         8.007179         max P[Q-stats]         0.877000         P[Q-stats(1)]         0.054000
IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII
D-W 1.754899 JB 1.075718 min P[Q-stats] 0.054000 P[Q-stats(2)] 0.121000 P[Q-stats(3)] 0.210000

Figure 139: Best ARMA models for filtered data (allowing 5 lags for p,q in ARMA(p,q)).

American	2 202200	p =	2.000000	q =	0.000000	d =	1.000000	b =	0.000000	t =	0.000000
alpha	-3.203286										
se_alpha	2.359659										
t-stat(alpha)	0.575116		-2.005155								
MA roots	0.575116	0.575116									
R <sup>2</sup>	0.120584		SIC	9.280247	may		0.656000	DI	Q-stats(1)]	0.116000	
D-W	2.024401		JB	0.267391			0.116000		Q-stats(1)]		
D-vv	2.024401		JB	0.207391	111111	-[Q-sidis]	0.110000		Q-stats(2)]		
Continental		n –	1.000000	a –	1.000000	d –	1.000000		0.000000		0.000000
	-0.444827			Ч-	1.000000	u =	1.000000	<u> </u>	0.000000	ι-	0.000000
se alpha		0.190875									
t-stat(alpha)											
MA roots	0.807316										
R <sup>2</sup>	0.106457		SIC	9.435288	max F	P[Q-stats]	0.707000	P[	Q-stats(1)]	0.280000	
D-W	1.880401		JB	2.018102	min F	P[Q-stats]	0.056000	P[	Q-stats(2)]	0.056000	
								P[	Q-stats(3)]	0.098000	
Delta		p =	1.000000	q =	2.000000	d =	1.000000	b =	0.000000	t =	0.000000
alpha			-0.689018								
se_alpha			0.155433								
t-stat(alpha)		18.15837	-4.432886	-4.101462							
AR roots	0.722343	0 500000									
MA roots	1.212250	0.523232	010	0.500505	_		0.447000		0 -1-1 (1)	0.040000	-
R <sup>2</sup>	0.455961		SIC	8.593528			0.117000		Q-stats(1)]		
D-W	2.188764		JB	1.353955	min H	~[Q-stats]	0.009000		Q-stats(2)]		
Northungt		-	2 000000	-	1 000000	-	1 000000		Q-stats(3)]		0.000000
Northwest	2 974007	p =	3.000000 -0.544163	q =	1.000000	d =	1.000000	b =	0.000000	t =	0.000000
			0.119173								
se_alpha t-stat(alpha)											
	0.947275			-1.400233	0.035557						
MA roots	0.733168	0.000000	0.000000								
R <sup>2</sup>	0.525940		SIC	8.467463	max	P[O-stats]	0.621000	PI	Q-stats(1)]	0.208000	
D-W	1.934719		JB	0.507886			0.075000		Q-stats(2)]		
5	1.001110		02	0.007000			0.070000		Q-stats(3)]		
United		p =	1.000000	q =	2.000000	d =	1.000000	b =		t =	0.000000
alpha	-1.907227	0.589190	-0.570465								
se_alpha	0.558330	0.125946	0.146020	0.145502							
t-stat(alpha)		4.678132	-3.906761	-2.838309							
AR roots											
MA roots	0.988324	0.417859									
R²	0.212440		SIC	9.231869			0.052000		Q-stats(1)]		
D-W	1.999970		JB	4.964875	min F	P[Q-stats]	0.003000		Q-stats(2)]		
									Q-stats(3)]		
US	0.075000	p =	1.000000	q =	2.000000	d =	1.000000	b =	0.000000	t =	0.000000
alpha			-0.641213								
se_alpha			0.152563								
t-stat(alpha) AR roots	0.369489	2.00007	-4.202940	-2.04000/							
AR roots   MA roots											
	0 007/0/	0 356281									
	0.997494	0.356281	SIC	9 125922	may	P[()-state1	0.011000	DI	$\Omega$ -state(1)	0 002000	
R <sup>2</sup>	0.261398	0.356281	SIC	9.125922			0.011000		Q-stats(1)]		
		0.356281	SIC JB	9.125922 0.582535			0.011000 0.000000	P[	Q-stats(2)]	0.006000	
R² D-W	0.261398		JB	0.582535		P[Q-stats]	0.000000	P[ P[	Q-stats(2)] Q-stats(3)]	0.006000	0.000000
R <sup>2</sup> D-W Southwest	0.261398 1.873029	p =	JB 0.000000	0.582535	min F	P[Q-stats]		P[	Q-stats(2)] Q-stats(3)]	0.006000	0.000000
R² D-W	0.261398 1.873029 0.902712		JB 0.000000 -0.535261	0.582535	min F	P[Q-stats]	0.000000	P[ P[	Q-stats(2)] Q-stats(3)]	0.006000	0.000000
R <sup>2</sup> D-W Southwest alpha se_alpha	0.261398 1.873029 0.902712 0.119819	p = -0.460501 0.144173	JB 0.000000 -0.535261 0.141872	0.582535	min F	P[Q-stats]	0.000000	P[ P[	Q-stats(2)] Q-stats(3)]	0.006000	0.000000
R <sup>2</sup> D-W Southwest alpha	0.261398 1.873029 0.902712 0.119819	p = -0.460501 0.144173	JB 0.000000 -0.535261 0.141872	0.582535	min F	P[Q-stats]	0.000000	P[ P[	Q-stats(2)] Q-stats(3)]	0.006000	0.000000
R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)	0.261398 1.873029 0.902712 0.119819 7.533984	p = -0.460501 0.144173	JB 0.000000 -0.535261 0.141872	0.582535	min F	P[Q-stats]	0.000000	P[ P[	Q-stats(2)] Q-stats(3)]	0.006000	0.000000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots	0.261398 1.873029 0.902712 0.119819 7.533984	p = -0.460501 0.144173 -3.194086	JB 0.000000 -0.535261 0.141872	0.582535	min F 2.000000	P[Q-stats] d =	0.000000	P[ P[ b =	Q-stats(2)] Q-stats(3)]	0.006000 0.007000 t =	0.000000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242	p = -0.460501 0.144173 -3.194086	JB -0.535261 0.141872 -3.772847	0.582535 q =	min F 2.000000 max F	P[Q-stats] d = P[Q-stats]	0.000000	P[ P[ b =	Q-stats(2)] Q-stats(3)] 0.000000	0.006000 0.007000 t =	0.000000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560	p = -0.460501 0.144173 -3.194086	JB 0.000000 -0.535261 0.141872 -3.772847 SIC	0.582535 q = 7.152773	min F 2.000000 max F	P[Q-stats] d = P[Q-stats]	0.000000 1.000000 0.985000	P[ P[ b = P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.006000 0.007000 t = 0.080000	0.000000
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208	p = -0.460501 0.144173 -3.194086 0.536741 p =	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000	0.582535 q = 7.152773 1.560897 q =	min F 2.000000 max F	P[Q-stats] d = P[Q-stats]	0.000000 1.000000 0.985000	P[ P[ b = P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)]	0.006000 0.007000 t = 0.080000 0.154000	
R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Av. fares alpha	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300	<u>p =</u> -0.460501 0.144173 -3.194086 0.536741 <u>p =</u> 0.573635	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 -0.571335	0.582535 q = 7.152773 1.560897 q = -0.930671	min F 2.000000 max F min F	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.000000 1.000000 0.985000 0.080000	P[ P[ b = P[ P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.006000 0.007000 t = 0.080000 0.154000 0.192000	
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300 0.497620	p = -0.460501 0.144173 -3.194086 0.536741 p = 0.573635 0.043487	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 0.571335 0.032299	0.582535 q = 7.152773 1.560897 q = -0.930671 0.053338	min F 2.000000 max F min F	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.000000 1.000000 0.985000 0.080000	P[ P[ b = P[ P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.006000 0.007000 t = 0.080000 0.154000 0.192000	
R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300 0.497620	p = -0.460501 0.144173 -3.194086 0.536741 p = 0.573635 0.043487	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 -0.571335	0.582535 q = 7.152773 1.560897 q = -0.930671 0.053338	min F 2.000000 max F min F	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.000000 1.000000 0.985000 0.080000	P[ P[ b = P[ P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.006000 0.007000 t = 0.080000 0.154000 0.192000	
R <sup>2</sup> D-W Southwest alpha se_alpha [AR roots] MA roots] R <sup>2</sup> D-W Av. fares alpha t-stat(alpha) t-stat(alpha) [AR roots]	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300 0.497620 -5.177241	p = -0.460501 0.144173 -3.194086 0.536741 p = 0.573635 0.043487 13.19084	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 -0.571335 0.032299 -17.68901	0.582535 q = 7.152773 1.560897 q = -0.930671 0.053338	min F 2.000000 max F min F	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.000000 1.000000 0.985000 0.080000	P[ P[ b = P[ P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.006000 0.007000 t = 0.080000 0.154000 0.192000	
R <sup>2</sup> D-W Southwest alpha se_alpha iAR roots MA roots R <sup>2</sup> D-W Av. fares alpha se_alpha se_alpha iAR roots MA roots MA roots	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300 0.497620 -5.177241 0.979554	p = -0.460501 0.144173 -3.194086 0.536741 p = 0.573635 0.043487	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 -0.571335 0.032299 -17.68901 0.974729	0.582535 q = 7.152773 1.560897 q = -0.930671 0.053338 -17.44854	min F 2.000000 max F min F 3.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] d =	0.000000 1.000000 0.985000 0.080000 1.000000	P[ P] b = P[ P[ P] b =	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000	0.006000 0.007000 t = 0.080000 0.154000 0.192000 t =	
R <sup>2</sup> D-W alpha se_alpha t-stat(alpha)  AR roots   MA roots  B-W Av. fares alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300 0.497620 -5.177241 0.979554 0.431063	p = -0.460501 0.144173 -3.194086 0.536741 p = 0.573635 0.043487 13.19084	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 -0.571335 0.032299 -17.68901 0.974729 SIC	0.582535 q = 7.152773 1.560897 q = -0.930671 0.053338 -17.44854 7.981590	min F 2.000000 max F min F 3.000000 max F	P[Q-stats] d = P[Q-stats] P[Q-stats] d = d = P[Q-stats]	0.000000 1.000000 0.985000 0.080000 1.000000 0.0374000	P[ P] b = P[ P[ P[ b =	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)]	0.006000 0.007000 t = 0.080000 0.154000 0.192000 t = 0.011000	
R <sup>2</sup> D-W Southwest alpha se_alpha iAR roots MA roots R <sup>2</sup> D-W Av. fares alpha se_alpha se_alpha iAR roots MA roots MA roots	0.261398 1.873029 0.902712 0.119819 7.533984 0.997242 0.249560 1.688208 -2.576300 0.497620 -5.177241 0.979554	p = -0.460501 0.144173 -3.194086 0.536741 p = 0.573635 0.043487 13.19084	JB 0.000000 -0.535261 0.141872 -3.772847 SIC JB 0.000000 -0.571335 0.032299 -17.68901 0.974729	0.582535 q = 7.152773 1.560897 q = -0.930671 0.053338 -17.44854	min F 2.000000 max F min F 3.000000 max F	P[Q-stats] d = P[Q-stats] P[Q-stats] d = d = P[Q-stats]	0.000000 1.000000 0.985000 0.080000 1.000000	P[ P] b = P[ P[ P[ b = P[ P[ P[	Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000	0.006000 0.007000 t = 0.080000 0.154000 0.192000 t = 0.011000 0.027000	0.000000

Figure 140: Best ARMA models for differentiated dependant variable (i.e. best ARIMA(p,1,q) models) in filtered data.

American		p =	0.000000	q =	2.000000	d =	0.000000	b =	1.000000	t =	1.000000
alpha	574.6830		-1.640269								
se_alpha			0.589527								
	42.37462	-4.124070	-2.782348	9.205166	4.128723						
AR roots	0 004040	0 004040									
R <sup>2</sup>	0.934305	0.621048	SIC	9.217373	max	P[Q-stats]	0.950000	DI	Q-stats(1)]	0.259000	
D-W	2.176079		JB	6.687768		P[Q-stats]			Q-stats(1)]		
2 11	2.170075		00	0.007700			0.000000		Q-stats(3)]		
Continental		p =	0.000000	q =	2.000000	d =	0.000000		1.000000		0.000000
alpha		-51.42751	0.940090	0.567324							
se_alpha			0.077616								
	46.69962	-3.694642	12.11209	6.771970							
AR roots	0 750000	0 750000									
MA roots  R <sup>2</sup>	0.739066	0.753209	SIC	9.350545	may	P[Q-stats]	0.000000	DI	Q-stats(1)]	0.000000	
D-W	2.121524		JB	2.325072		P[Q-stats]			Q-stats(1)]		
5	2.121021		02	2.020072		i [de otato]	0.000000		Q-stats(3)]		
Delta		p =	3.000000	q =	2.000000	d =	0.000000	b =			0.000000
alpha	379.8326	0.836018	-0.811370	0.769838	0.426887	0.849721					
se_alpha			0.131557								
			-6.167449	7.758092	3.898309	8.683040					
AR roots		0.928530	0.892909								
MA roots  R <sup>2</sup>	0.921803	0.921803	SIC	8.799172	may	P[Q-stats]	0 935000	DI	Q-stats(1)]	0.026000	
D-W	1.898956		JB	9.078859		P[Q-stats]			Q-stats(1)]		
2 **			00	5.010000		. [ a siais]	0.020000		Q-stats(2)]		
Northwest		p =	0.000000	q =	4.000000	d =	1.000000		1.000000		1.000000
alpha		-6.108298	0.196231	-0.602622	-0.945106	-0.271605	0.826250				
se_alpha						0.094669					
t-stat(alpha)	-10.17573	-6.245564	5.932793	-6.154409	-9.027595	-2.868982	11916.88				
AR roots	0 007404	0 007404	0.011266	0.011266							
R <sup>2</sup>	0.653362	0.997494	0.911266 SIC	8.336151	may	P[Q-stats]	0.082000	PI	Q-stats(1)]	0.050000	
D-W	1.799905		JB	2.102372		P[Q-stats]			Q-stats(1)]		
2	1.100000		00	2.102012			0.002000		Q-stats(3)]		
United		p =	0.000000	q =	2.000000	d =	0.000000	b =	1.000000	t =	0.000000
alpha			1.064661								
se_alpha			0.092880								
	51.65446	-5.830275	11.46275	7.293217							
AR roots	0 820/70	0.820470									
R <sup>2</sup>	0.847939	0.020470	SIC	9.119888	max	P[Q-stats]	0.668000	Pľ	Q-stats(1)]	0 256000	
D-W	1.981516		JB	4.486529		P[Q-stats]			Q-stats(2)]		
									Q-stats(3)]		
US		p =	0.000000		2.000000	d =	0.000000	b =	0.000000	t =	1.000000
alpha			1.007156								
se_alpha			0.073972								
t-stat(alpha)	31.43596	-0.298/22	13.61534	11.39222							
MA roots	0 782231	0.782231									
R <sup>2</sup>	0.884305	5 52201	SIC	8.898536	max	P[Q-stats]	0.514000	Pſ	Q-stats(1)]	0.514000	
D-W	2.147299		JB	0.198258		P[Q-stats]			Q-stats(2)]		
								P[	Q-stats(3)]	0.275000	
Southwest							0.000000	b =	1.000000	t =	1.000000
alpha			1.321151								
se_alpha			0.084972								
	00.13402	-3.031542	15.54803	12.52921	-13.13021	-10.44740					
		0.000055	0.964392								
AR roots	0.966255	0.900255			may	P[Q-stats]	0.840000	Pſ	Q-stats(1)]	0.043000	
	0.966255	0.966255	SIC	6.844582							
AR roots   MA roots		0.966255		6.844582 0.399937		P[Q-stats]	0.043000	PI	Q-stats(2)]	0.075000	
AR roots   MA roots  R <sup>2</sup> D-W	0.844654		SIC JB	0.399937	min			P[	Q-stats(3)]	0.149000	
AR roots   MA roots  R <sup>2</sup> D-W Av. fares	0.844654 1.629990	p =	SIC JB 1.000000	0.399937 q =	min 3.000000	d =	0.000000		Q-stats(3)]		1.000000
AR roots   MA roots  R <sup>2</sup> D-W Av. fares alpha	0.844654 1.629990 437.6050	<u>p =</u> -46.32937	SIC JB <u>1.0000000</u> -1.011687	0.399937 q = 0.545707	min <u>3.000000</u> 0.414444	d = -0.365279	0.000000	P[	Q-stats(3)]	0.149000	1.000000
AR roots   MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha	0.844654 1.629990 437.6050 7.892496	p = -46.32937 7.343300	SIC JB 1.000000 -1.011687 0.223626	0.399937 <u>q =</u> 0.545707 0.151554	min 3.000000 0.414444 0.037636	d = -0.365279 0.033268	0.000000 -0.972371 0.062872	P[	Q-stats(3)]	0.149000	1.000000
AR roots   MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)	0.844654 1.629990 437.6050 7.892496 55.44571	p = -46.32937 7.343300	SIC JB 1.000000 -1.011687 0.223626	0.399937 <u>q =</u> 0.545707 0.151554	min 3.000000 0.414444 0.037636	d = -0.365279	0.000000 -0.972371 0.062872	P[	Q-stats(3)]	0.149000	1.000000
AR roots   MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)  AR roots	0.844654 1.629990 437.6050 7.892496 55.44571 0.545707	p = -46.32937 7.343300 -6.309066	SIC JB -1.000000 -1.011687 0.223626 -4.524019	0.399937 <u>q =</u> 0.545707 0.151554	min 3.000000 0.414444 0.037636	d = -0.365279 0.033268	0.000000 -0.972371 0.062872	P[	Q-stats(3)]	0.149000	1.000000
AR roots   MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)	0.844654 1.629990 437.6050 7.892496 55.44571 0.545707 0.997463	p = -46.32937 7.343300	SIC JB 1.000000 -1.011687 0.223626 -4.524019 0.977325	0.399937 q = 0.545707 0.151554 3.600737	min <u>3.000000</u> 0.414444 0.037636 11.01198	d = -0.365279 0.033268 -10.97989	0.000000 -0.972371 0.062872 -15.46599	P[ b =	Q-stats(3)]	0.149000 t =	1.000000
AR roots   MA roots  R <sup>2</sup> D-W Av. fares alpha se_alpha t-stat(alpha)  AR roots   MA roots	0.844654 1.629990 437.6050 7.892496 55.44571 0.545707	p = -46.32937 7.343300 -6.309066	SIC JB -1.000000 -1.011687 0.223626 -4.524019	0.399937 <u>q =</u> 0.545707 0.151554	min 3.000000 0.414444 0.037636 11.01198 max	d = -0.365279 0.033268	0.000000 -0.972371 0.062872 -15.46599 0.855000	P[ b = P[	Q-stats(3)] 1.000000	0.149000 t = 0.164000	1.000000

Figure 141: Best ARIMA models for filtered data (with possible use of a trend variable and a dummy variable).

• · ·			0.000000		0.000000		0.000000		4 000000		1 00000
American	590 2625	p =	0.000000			d =	0.000000	b =	1.000000	t =	1.000000
alpha se alpha			0.574834								
			-2.872104								
AR roots	44.00070	-4.173042	-2.072104	3.120131	4.020100						
	0.608788	0 608788									
R <sup>2</sup>	0.934410	0.0007.00	SIC	9.195063	max	P[Q-stats]	0.841000	PI	Q-stats(1)]	0.268000	
D-W	2.220186		JB	4.988802		P[Q-stats]			Q-stats(2)]		
5	2.220100		02	1.000002			0.200000		Q-stats(3)]		
Continental		p =	0.000000	a =	2.000000	d =	0.000000		1.000000		0.00000
alpha	466.3134		0.926233		2.000000	<u> </u>	0.000000	~		•	0.00000
se_alpha			0.076501								
	50.63983	-4.015049	12.10751	6.547973							
AR roots											
MA roots	0.740508	0.740508									
R <sup>2</sup>	0.734066		SIC	9.222188	max	P[Q-stats]	0.506000	P[0	Q-stats(1)]	0.212000	
D-W	2.202367		JB	2.128731	min	P[Q-stats]	0.046000	PÍO	Q-stats(2)]	0.046000	
								PÌQ	Q-stats(3)	0.098000	
Delta		p =	4.000000	q =	3.000000	d =	0.000000	b =	0.000000	t =	0.00000
alpha	362.4295	1.419925	-1.121853	1.119001	-0.458336	-0.408297	0.424080	-0.981864			
se_alpha						0.054459					
					-4.077817	-7.497300	10.32773	-21.85263			
AR roots			0.877047	0.632820							
		0.997486									
R <sup>2</sup>	0.935396		SIC	8.853235		P[Q-stats]			Q-stats(1)]		
D-W	1.815138		JB	1.689929	min	P[Q-stats]	0.037000		Q-stats(2)]		
									Q-stats(3)]		
Northwest		p =	4.000000		3.000000		0.000000		0.000000	t =	1.00000
						0.469012					
						0.133880					
					-3.164100	3.503215	13.58651	8.556115	10.02267		
AR roots			0.948656	0.528292							
MA roots		0.912535		0.0000.40			0.050000			0.054000	
R <sup>2</sup>	0.961141		SIC	8.208349	max	PIO-stats1	0.852000	PIC	J-stats(1)	0.251000	
D-W			10								
0 11	1.887232		JB	2.507287		P[Q-stats]		PĮ	Q-stats(2)]	0.494000	
	1.887232			2.507287	min	P[Q-stats]	0.147000	P[( P[(	Q-stats(2)] Q-stats(3)]	0.494000 0.587000	0.00000
United			1.000000	2.507287 q =	min 2.000000	P[Q-stats]		P[( P[(	Q-stats(2)]	0.494000	0.00000
United alpha	522.3056	-88.50288	1.000000 -0.297339	2.507287 q = 1.176809	min 2.000000 0.780686	P[Q-stats]	0.147000	P[( P[(	Q-stats(2)] Q-stats(3)]	0.494000 0.587000	0.00000
United alpha se_alpha	522.3056 8.217776	-88.50288 11.49746	1.000000 -0.297339 0.064204	2.507287 q = 1.176809 0.090384	min 2.000000 0.780686 0.088512	P[Q-stats]	0.147000	P[( P[(	Q-stats(2)] Q-stats(3)]	0.494000 0.587000	0.00000
United alpha se_alpha t-stat(alpha)	522.3056 8.217776 63.55802	-88.50288 11.49746	1.000000 -0.297339 0.064204	2.507287 q = 1.176809 0.090384	min 2.000000 0.780686 0.088512	P[Q-stats]	0.147000	P[( P[(	Q-stats(2)] Q-stats(3)]	0.494000 0.587000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots	522.3056 8.217776 63.55802 0.297339	-88.50288 11.49746 -7.697605	1.000000 -0.297339 0.064204	2.507287 q = 1.176809 0.090384	min 2.000000 0.780686 0.088512	P[Q-stats]	0.147000	P[( P[(	Q-stats(2)] Q-stats(3)]	0.494000 0.587000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots	522.3056 8.217776 63.55802 0.297339 0.883564	-88.50288 11.49746	1.000000 -0.297339 0.064204 -4.631183	2.507287 q = 1.176809 0.090384 13.02007	min 2.000000 0.780686 0.088512 8.820084	P[Q-stats]	0.147000	P[( P[( b =	Q-stats(2)] Q-stats(3)] 1.000000	0.494000 0.587000 t =	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745	-88.50288 11.49746 -7.697605	1.000000 -0.297339 0.064204 -4.631183 SIC	2.507287 q = 1.176809 0.090384 13.02007 9.190899	min 2.000000 0.780686 0.088512 8.820084 max	P[Q-stats] d = P[Q-stats]	0.147000 0.000000 0.655000	P[( P[( b =	Q-stats(2)] <u>Q-stats(3)]</u> 1.000000	0.494000 0.587000 t = 0.135000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots	522.3056 8.217776 63.55802 0.297339 0.883564	-88.50288 11.49746 -7.697605	1.000000 -0.297339 0.064204 -4.631183	2.507287 q = 1.176809 0.090384 13.02007	min 2.000000 0.780686 0.088512 8.820084 max	P[Q-stats]	0.147000 0.000000 0.655000	P[( P[( b = P[( P[(	Q-stats(2)] <u>Q-stats(3)]</u> 1.000000 <u>Q-stats(1)]</u> Q-stats(2)]	0.494000 0.587000 t = 0.135000 0.159000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745	-88.50288 11.49746 -7.697605 0.883564	1.000000 -0.297339 0.064204 -4.631183 SIC JB	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801	min 2.000000 0.780686 0.088512 8.820084 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000	P[( 	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066	-88.50288 11.49746 -7.697605 0.883564 p =	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> =	min 2.000000 0.780686 0.088512 8.820084 max min	P[Q-stats] d = P[Q-stats]	0.147000 0.000000 0.655000 0.069000	P[( 	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 -2.784931	-88.50288 11.49746 -7.697605 0.883564 p = 0.457360	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972	min 2.000000 0.780686 0.088512 8.820084 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000	P[( 	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 -2.784931 1.209650	-88.50288 11.49746 -7.697605 0.883564 <u>p =</u> 0.457360 0.044404	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174	min 2.000000 0.780686 0.088512 8.820084 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000	P[( 	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 -2.784931 1.209650	-88.50288 11.49746 -7.697605 0.883564 <u>p =</u> 0.457360 0.044404	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174	min 2.000000 0.780686 0.088512 8.820084 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000	P[( 	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha se_alpha t-stat(alpha)  AR roots	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 -2.784931 1.209650 2.302261 0.457360	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.883564 0.04404 10.29997	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174	min 2.000000 0.780686 0.088512 8.820084 max min	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000	P[( 	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha se_alpha t-stat(alpha)  AR roots	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 -2.784931 1.209650 -2.302261	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.883564 0.04404 10.29997	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000	P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000	P[0 P[0 b = P[0 P[0 b =	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t =	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 -2.784931 1.209650 -2.302261 0.457360 0.457360	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.883564 0.04404 10.29997	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 max	P[Q-stats] d = P[Q-stats] P[Q-stats] d =	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000	P[0 P[0 b = P[0 P[0 b = P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 2-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  2D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 2.302261 0.457360 1.178538 1.178538	-88.50288 11.49746 -7.697605 0.883564 0.457360 0.044404 10.29997 0.370774	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000	P[0 P[0 D = P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(1)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000	
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  2D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup>	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 2.302261 0.457360 1.178538 1.178538	-88.50288 11.49746 -7.697605 0.883564 0.457360 0.044404 10.29997 0.370774	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000	P[0 P[0 D = P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest	522.3056 8.217776 63.55802 0.297339 0.883564 0.887745 1.720066 2.302261 0.457360 0.457360 0.457360 0.457360 0.457360 0.457360	-88.50288 11.49746 -7.697605 0.883564 0.457360 0.044404 10.29997 0.370774	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> =	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 max min 3.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d =	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000	P[0 P[0 D = P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots   MA roots  MA roots  R <sup>2</sup> D-W	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 2.784931 1.209650 2.302261 0.457360 1.178538 0.4507360 1.178538 0.40008 2.234239	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.044404 10.29997 0.370774 p = -16.46539 3.057518	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000	P[0 P[0 D = P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  D-W US alpha se_alpha se_alpha t-stat(alpha)  AR roots   MA roots   MA roots  MA roots  R <sup>2</sup> D-W	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 2.784931 1.209650 2.302261 0.457360 1.178538 0.4507360 1.178538 0.40008 2.234239	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.044404 10.29997 0.370774 p = -16.46539 3.057518	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000	P[0 P[0 D = P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  D-W US alpha se_alpha se_alpha t-stat(alpha)  AR roots   MA roots   MA roots  MA roots  R <sup>2</sup> D-W	522.3056 8.217776 63.55802 0.297339 0.883564 0.857745 1.720066 2.784931 1.209650 2.302261 0.457360 1.178538 0.4507360 1.178538 0.40008 2.234239	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.044404 10.29997 0.370774 p = -16.46539 3.057518	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000	P[0 P[0 D = P[0 P[0 D = P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(2)] Q-stats(2)] Q-stats(2)] Q-stats(3)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)	522.3056 8.217776 63.55802 0.297339 0.883564 0.883564 1.720066 2.302261 0.457360 0.457360 0.457360 0.457360 0.457360 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.044404 10.29997 0.370774 p = -16.46539 3.057518	1.000000 0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627	min 2.00000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] 20.915340 0.043895 -20.85293	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.001000 0.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 D =	Q-stats(2)] <u>Q-stats(3)]</u> 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 1.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000 t =	0.00000
United alpha se_alpha t-stat(alpha)  AR roots  MA roots  BA alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   AR roots   MA roots  R <sup>2</sup>	522.3056 8.217776 63.55802 0.29739 0.883564 0.885745 1.720066 2.784931 1.200650 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484	-88.50288 11.49746 -7.697605 0.883564 0.457360 0.044404 10.29997 0.370774 0.370774 <u>p =</u> -16.46539 3.057518 -5.385216	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.003868 14.14012 0.952656 SIC	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480 6.886999	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253 -6.236935 max	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] d = -0.915340 0.043895 -20.85293 P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] Q-stats(1)] Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(3)] Q-stats(1)] Q-stats(1)]	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha se_alpha se_alpha se_alpha t-stat(alpha)  AR roots   AR roots	522.3056 8.217776 <u>63.55802</u> 0.297339 0.883564 0.887365 1.720066 2.302261 0.457360 2.302261 0.457360 2.302261 0.450083 2.234239 197.1474 2.356047 83.67721 0.980219	-88.50288 11.49746 -7.697605 0.883564 0.457360 0.044404 10.29997 0.370774 0.370774 <u>p =</u> -16.46539 3.057518 -5.385216	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253 -6.236935 max	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] P[Q-stats] 20.915340 0.043895 -20.85293	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] <u>Q-stats(3)]</u> 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 1.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000 t =	0.00000
United alpha se_alpha t-stat(alpha)  AR roots  MA roots  BA alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   AR roots   MA roots  R <sup>2</sup>	522.3056 8.217776 63.55802 0.29739 0.883564 0.885745 1.720066 2.784931 1.200650 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484	-88.50288 11.49746 -7.697605 0.883564 0.457360 0.044404 10.29997 0.370774 0.370774 <u>p =</u> -16.46539 3.057518 -5.385216	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656 SIC JB	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480 6.886999 1.648904	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253 -6.236935 max min	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] d = -0.915340 0.043895 -20.85293 P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] 2.stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  BP US alpha se_alpha t-stat(alpha)  AR roots  MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha se_alpha se_alpha se_alpha t-stat(alpha) [AR roots]  AR roots   AR roots	522.3056 8.217776 63.55802 0.297339 0.883564 0.883564 1.720066 2.302261 0.457745 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484 1.706585	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.044404 10.29997 0.370774 0.370774 -5.385216 0.980219 p =	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656 SIC JB 1.000000	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480 <b>6</b> .886999 1.648904 <b>q</b> =	min 2.00000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253 -6.236935 max min 3.000000	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] d =	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.001000 0.000000 0.000000 0.000000 0.036000 0.000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] 2.stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000 t =	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  P US alpha se_alpha t-stat(alpha)  AR roots   MA roots   MA roots  AR roots   MA roots  AR roots   MA roots	522.3056 8.217776 63.55802 0.297339 0.883564 0.883564 0.883564 1.720066 2.784931 1.200650 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 2.356047 2.356047 2.356047 8.367721 0.980219 0.843484 1.706585	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 0.370774 0.370774 0.3057518 -5.385216 0.980219 0.980219	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.093868 14.14012 0.952656 SIC JB 1.000000 -0.978832	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 0.531715 0.085253 -6.236935 max min 3.000000 0.410159	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 -0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.000000 0.000000 0.000000 0.036000 0.000000 0.0978057	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] 2.stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000 t = 0.036000 0.070000 0.070000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha se_alpha se_alpha	522.3056 8.217776 63.55802 0.297339 0.883564 1.720066 -2.784931 1.200650 2.302261 0.457360 0.457360 0.457360 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 197.1474 3.67721 0.843484 1.706585	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 <b>p</b> = -16.4653 3.057518 -5.385216 0.980219 <b>p</b> = -47.37277 7.507944	1.000000 0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656 SIC JB 1.000000 -0.978832 0.226122	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>0.614065</b> 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304 0.154522	min 2.00000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935 -6.236935 max min 3.000000 0.410159 0.048518	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] 0.047533 0.032738	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.0717000 0.036000 0.036000 0.0978057 0.067188	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] 2.stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000 t = 0.036000 0.070000 0.070000 0.116000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  mAr roots  D-W US alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) AV, fares alpha se_alpha t-stat(alpha)	522.3056 8.217776 63.55802 0.297339 0.883564 0.883564 0.887745 1.720066 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484 1.706585 447.0397 8.492168	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 <b>p</b> = -16.4653 3.057518 -5.385216 0.980219 <b>p</b> = -47.37277 7.507944	1.000000 0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656 SIC JB 1.000000 -0.978832 0.226122	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>0.614065</b> 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304 0.154522	min 2.00000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935 -6.236935 max min 3.000000 0.410159 0.048518	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 -0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.0717000 0.036000 0.036000 0.0978057 0.067188	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] 2.stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000 t = 0.036000 0.070000 0.070000 0.116000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  BA roots   MA roots   MA roots   MA roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha)  AR roots  R <sup>2</sup> D-W Southwest alpha se_alpha t-stat(alpha) [AR roots] R <sup>2</sup> D-W [MA roots] R <sup>2</sup> D-W [AR roots] [AR roots]	522.3056 8.217776 <u>63.55802</u> 0.297339 0.883564 0.883564 1.720066 2.302261 0.4577360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484 1.706585 447.0397 8.492168 52.64141	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 -16.46539 3.057518 -5.385216 0.980219 p = -47.37277 7.507944 -6.309686	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656 SIC JB 1.000000 -0.978832 0.226122 -4.328773	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>0.614065</b> 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304 0.154522	min 2.00000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935 -6.236935 max min 3.000000 0.410159 0.048518	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] 0.047533 0.032738	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.0717000 0.036000 0.036000 0.0978057 0.067188	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] 2.stats(3)] 0.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.000000 t = 0.036000 0.070000 0.070000 0.116000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  mAroots  BAR roots  mAroots	522.3056 8.217776 63.55802 0.297339 0.883564 0.885745 1.720066 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484 1.706585 447.0397 8.492168 52.64141 0.545304 0.997475	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 <b>p</b> = -16.4653 3.057518 -5.385216 0.980219 <b>p</b> = -47.37277 7.507944	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.093868 14.14012 0.952656 SIC JB 1.000000 -0.978832 0.226122 -4.328773 0.983015	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304 0.154522 3.528977	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935 -6.236935 max min 3.000000 0.410159 0.048518 8.453678	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 -0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] -20.374553 0.032738 -11.44095	0.147000 0.000000 0.655000 0.069000 1.000000 0.000000 0.000000 0.000000 0.036000 0.0000000 0.0000000 0.0000000 0.00000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(2)] Q-stats(2)] Q-stats(3)] 1.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000 t = 0.036000 0.070000 0.116000 t =	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots   MA roots   MA roots   AR roots	522.3056 8.217776 63.55802 0.297339 0.883564 0.883564 1.720066 2.302261 0.857745 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.843484 1.706585 447.0397 8.492168 52.64141 0.545304 0.997475 0.937661	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 -16.46539 3.057518 -5.385216 0.980219 p = -47.37277 7.507944 -6.309686	1.000000 0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.000000 1.327309 0.093868 14.14012 0.952656 SIC JB 1.000000 0.978832 0.226122 -4.328773 0.983015 SIC	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>0.614065</b> 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304 0.154522 3.528977 <b>7.875666</b>	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935 -6.236935 max min 3.000000 0.410159 0.048518 8.453678 max	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats]	0.147000 0.000000 0.655000 0.069000 1.000000 0.001000 0.000000 0.000000 0.000000 0.036000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.00000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(3)] 1.000000 Q-stats(3)] Q-st	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 t = 0.036000 0.070000 0.070000 0.116000 t = 0.146000	0.00000
United alpha se_alpha t-stat(alpha)  AR roots   MA roots  mAr coots  BAR roots  mAr coots	522.3056 8.217776 63.55802 0.297339 0.883564 0.885745 1.720066 2.302261 0.457360 1.178538 0.400083 2.234239 197.1474 2.356047 83.67721 0.980219 0.843484 1.706585 447.0397 8.492168 52.64141 0.545304 0.997475	-88.50288 11.49746 -7.697605 0.883564 0.883564 0.04404 10.29997 0.370774 0.370774 -16.46539 3.057518 -5.385216 0.980219 p = -47.37277 7.507944 -6.309686	1.000000 -0.297339 0.064204 -4.631183 SIC JB 1.000000 -0.807764 0.160582 -5.030231 SIC JB 0.093868 14.14012 0.952656 SIC JB 1.000000 -0.978832 0.226122 -4.328773 0.983015	2.507287 <b>q</b> = 1.176809 0.090384 13.02007 9.190899 4.900801 <b>q</b> = -0.436972 0.145174 -3.009992 8.928315 2.103985 <b>q</b> = 0.614065 0.074627 8.228480 6.886999 1.648904 <b>q</b> = 0.545304 0.154522 3.528977	min 2.000000 0.780686 0.088512 8.820084 max min 2.000000 -0.531715 0.085253 -6.236935 -6.236935 max min 3.000000 0.410159 0.048518 8.453678 max	P[Q-stats] d = P[Q-stats] P[Q-stats] d = P[Q-stats] P[Q-stats] d = -0.915340 -0.043895 -20.85293 P[Q-stats] P[Q-stats] P[Q-stats] P[Q-stats] -20.374553 0.032738 -11.44095	0.147000 0.000000 0.655000 0.069000 1.000000 0.000000 0.000000 0.000000 0.000000 0.036000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.00000000	P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0 P[0	Q-stats(2)] Q-stats(3)] 1.000000 1.000000 Q-stats(1)] Q-stats(2)] Q-stats(3)] 0.000000 Q-stats(2)] Q-stats(3)] 1.000000 Q-stats(2)] Q-stats(2)] Q-stats(3)] 1.000000	0.494000 0.587000 t = 0.135000 0.159000 0.266000 t = 0.000000 0.000000 0.000000 t = 0.036000 0.070000 0.070000 0.116000 t = 0.146000 0.188000	0.00000

Figure 142: Best ARIMA models for non-filtered data (with possible use of a trend variable and a dummy variable).

### A.2 EViews6 Code

This code prepares some pre-treated DOT and some economic data for use by the authors. All EViews6 code for further data treatment, modelling building; and analysis/forecasting was written exclusively by the authors. The first code is a tool to sort the Coupon database in order to get the quarterly average fares and number of passengers per carrier. The second program was used to perform the ARIMA regressions on these data of fares and passengers, and to pick up the best one according to the Schwarz Information Criterion.

```
wfopen complete_coupon_text.wf1
```

```
scalar nb_carriers=7
matrix(65,nb_carriers+1) pax
matrix(65,nb_carriers+1) fares
```

```
for !k=1 to nb_carriers
for !t=1 to 65
sample paxfares @all if carriercode=!k and time=!t
smpl paxfares
series pax_q=group01(7)
series fares_q=group01(14)
pax(!t,!k)=@sum(pax_q)
series mult=pax_q*fares_q
fares(!t,!k)=@sum(mult)/pax(!t,!k)
delete paxfares
next
next
```

for !t=1 to 65
scalar sumpax=0
scalar avfares=0
for !k=1 to nb\_carriers
sumpax=sumpax+pax(!t,!k)
avfares=avfares+fares(!t,!k)\*pax(!t,!k)
next
pax(!t,nb\_carriers+1)=sumpax
fares(!t,nb\_carriers+1)=avfares/sumpax
next

fares.write fares.txt

pax.write pax.txt

wfcreate u 65

'.....VARIABLES...... scalar nb\_carriers=8 '{1,2,...8,...} scalar maxlags=4 '{0,1,...4,...} scalar maxdifferencing=0 '{0,1,2,...} scalar trend=0 '{0,1} 1: use of a trend variable scalar breakdown=0 '{0,1} 1: use of break var. at t=35 scalar filter=1 '{0: no filter; 1:filtered data} '..... MATRIX OF RESULTS..... table(10\*nb\_carriers+1,20) results\_bestARMA matrix(65,nb\_carriers) matrix\_fares '.....CREATION OF continuous SERIES fare!k..... if filter=1 then matrix\_fares.read(t=txt,dropstrings) fares.txt matrix\_fares(1,5)=NA 'missing data from Northwest else matrix\_fares.read(t=txt,dropstrings) fares2.txt matrix\_fares(12,7)=NA matrix\_fares(13,7)=NA matrix\_fares(12,8)=NA matrix\_fares(13,8)=NA endif 

for !k=1 to nb\_carriers vector vect=@columnextract(matrix\_fares,!k) series fare!k mtos(vect,fare!k) scalar opt\_sic=100 scalar tstat=10 scalar opt\_p=0 scalar opt\_q=0 scalar opt\_d=0 scalar opt\_b=0 scalar opt\_t=0 scalar opt\_qprob\_min=0 matrix(50,1) opt\_correl for !p=0 to maxlags %ar="" if !p>0 then for !p2=1 to !p %ar=%ar+"ar("+@str(!p2)+") " next endif for !q=0 to maxlags %ma="" if !q>0 then for !q2=1 to !q

%ma=%ma+"ma("+@str(!q2)+") " next endif for !b=0 to breakdown %break="" if !b>0 then series dummy=(@trend>33) dummy(35) = 0.22%break="dummy " endif for !t=0 to trend %trend="" if !t>0 then %trend="@trend " endif %arma= %break + %trend +%ar + %ma for !d=0 to maxdifferencing %fare="fare!k" if !d>0 then %fare="d(fare!k,!d)" endif equation fare\_!k!p!d!q!b!t.ls {%fare} c {%arma} 'ARMA(p,q) for !r=1 to !p+!q+!t+!b+1 if fare\_!k!p!d!q!b!t.@stderrs(!r,1)<>NA then if Cabs(fare\_!k!p!d!q!b!t.Ctstats(!r))>1.96 then

174

```
else
tstat=tstat-1
endif
else
tstat=0
endif
next
scalar qprob_min=0
matrix(50,1) temp2
if (filter=1 and (!k!p!d!q!b!t=711001 or !k!p!d!q!b!t=430411
        or !k!p!d!q!t=80001 or !k!p!d!q!b!t=200210)) then
else
freeze(temp) fare_!k!p!d!q!b!t.correl
for !i=1 to 50
temp2(!i,1)=@val(temp(!i,7))
next
qprob_min=@min (temp2)
endif
if opt_sic>fare_!k!p!d!q!b!t.@schwarz and tstat=10 then 'min{SIC_k}
opt_sic=fare_!k!p!d!q!b!t.@schwarz
opt_p=!p
opt_q=!q
opt_d=!d
opt_b=!b
opt_t=!t
```

opt\_qprob\_min=qprob\_min opt\_correl=temp2 endif tstat=10 delete temp\* next next next next next **,** !p=opt\_p !q=opt\_q !d=opt\_d !b=opt\_b !t=opt\_t matrix root\_ar matrix root\_ma if maxlags>0 and (opt\_p>0 or opt\_q>0) then fare\_!k!p!d!q!b!t.arma(type=root,save=root) close fare\_!k!p!d!q!b!t endif fare\_!k!p!d!q!b!t.makeresids residuals freeze(residu) residuals.stats

```
'.....RESULTS BEST_ARMA.....
results_bestARMA((!k-1)*10+1,4)=!p 'p_opt
results_bestARMA((!k-1)*10+1,6)=!q 'q_opt
results_bestARMA((!k-1)*10+1,8)=!d 'q_opt
results_bestARMA((!k-1)*10+1,10)=!b 'q_opt
results_bestARMA((!k-1)*10+1,12)=!t 'q_opt
for !r=1 to !p+!q+!b+!t+1
results_bestARMA(((!k-1)*10+2,!r+1)=fare_!k!p!d!q!b!t.@coefs(!r,1) 'apha
results_bestARMA((!k-1)*10+3,!r+1)=fare_!k!p!d!q!b!t.@stderrs(!r,1) 'se_apha
if fare_!k!p!d!q!b!t.@stderrs(!r,1)>0 then
results_bestARMA((!k-1)*10+4,!r+1)=fare_!k!p!d!q!b!t.@tstats(!r) 't-stat(alpha)
endif
next
for !r=1 to !p
results_bestARMA((!k-1)*10+5,!r+1)=root_ar(!r,3) 'AR roots
next
for !r=1 to !q
results_bestARMA((!k-1)*10+6,!r+1)=root_ma(!r,3) 'MA roots
next
results_bestARMA((!k-1)*10+7,2)=fare_!k!p!d!q!b!t.@r2 'R
results_bestARMA((!k-1)*10+7,5)=opt_sic 'SIC
results_bestARMA((!k-1)*10+8,2)=fare_!k!p!d!q!b!t.@dw 'Durbin-Watson
results_bestARMA((!k-1)*10+8,5)=residu(14,2) 'Jarque-Bera
!i=1
```

```
while opt_correl(!i,1)=NA
!i=!i+1
wend
results_bestARMA((!k-1)*10+7,11)=opt_correl(!i,1) 'Q_stat(1)
results_bestARMA((!k-1)*10+8,11)=opt_correl(!i+1,1) 'Q_stat(2)
results_bestARMA((!k-1)*10+9,11)=opt_correl(!i+2,1) 'Q_stat(3)
results_bestARMA((!k-1)*10+7,8)=@max(opt_correl) 'Q_stat max
results_bestARMA((!k-1)*10+8,8)=@min(opt_correl) 'Q_stat minimum
'.....LEGENDS and FORMATTING.....
results_bestARMA(1,1)="American"
results_bestARMA(11,1)="Continental"
results_bestARMA(21,1)="Delta"
results_bestARMA(31,1)="Northwest"
results_bestARMA(41,1)="United"
results_bestARMA(51,1)="US"
results_bestARMA(61,1)="Southwest"
results_bestARMA(71,1)="Av. fares"
!coord = (!k-1)*10+2
!coord2=(!k-1)*10+1
!coord3=(!k-1)*10+5
!coord4=(!k-1)*10+7
!coord5=(!k-1)*10+10
results_bestARMA.setlines(!coord2) +t
results_bestARMA.setlines(!coord) +t
```

178

results\_bestARMA.setlines(!coord3) +t results\_bestARMA.setlines(!coord4) +t results\_bestARMA.setlines(a) +r results\_bestARMA.setfillcolor(!coord2) @rgb(50,255,0) results\_bestARMA.settextcolor(!coord,2) @rgb(0,0,255) results\_bestARMA.setwidth(2:20) 9 results\_bestARMA.setheight(!coord5) 0 results\_bestARMA(!coord,1)="alpha" results\_bestARMA(!coord+1,1)="se\_alpha" results\_bestARMA(!coord+2,1)="t-stat(alpha)" results\_bestARMA(!coord+3,1)="|AR roots|" results\_bestARMA(!coord+4,1)="|MA roots|" results\_bestARMA(!coord+5,1)="R" results\_bestARMA(!coord+5,4)="SIC" results\_bestARMA(!coord+6,1)="D-W" results\_bestARMA(!coord+6,4)="JB" max P[Q-stats]" results\_bestARMA(!coord+5,6)=" min P[Q-stats]" results\_bestARMA(!coord+6,6)=" P[Q-stats(1)]" results\_bestARMA(!coord+5,9)=" results\_bestARMA(!coord+6,9)=" P[Q-stats(2)]" P[Q-stats(3)]" results\_bestARMA(!coord+7,9)=" p =" results\_bestARMA(!coord-1,3)=" q =" results\_bestARMA(!coord-1,5)=" results\_bestARMA(!coord-1,7)=" d =" results\_bestARMA(!coord-1,9)=" b ="

results\_bestARMA(!coord-1,11)=" t =" , pagestruct(end=73) series dummy=(@trend>33) dummy(35)=0.22rename fare\_!k!p!d!q!b!t carrier\_!k smpl 66 73 carrier\_!k.forecast ffare!k ffare\_se!k smpl 58 65 carrier\_!k.forecast ffare2!k ffare2\_se!k smpl @all graph gr!k.line ffare2!k ffare!k ffare!k ffare!k+ffare\_se!k ffare!k-ffare\_se!k 'gr!k.legend -display gr!k.name(3) gr!k.name(4) gr!k.name(5) gr!k.name(6) gr!k.name(7) gr!k.name(1) forecast!k1 gr!k.name(2) forecast!k2 %gr=%gr+" gr" + @str(!k) %f1=%f1+" ffare" + @str(!k) %f2=%f2+" ffare2" + @str(!k) group fare\_g1 {%f1}

180

group fare\_g2 {%f2} ۶ ..... delete opt\* delete residu\* delete qprob\_min delete tstat delete root\_\* delete vect next graph forecast.merge {%gr} matrix matrix\_faresf=@convert(fare\_g1) matrix matrix\_faresf2=@convert(fare\_g2) delete gr\* delete ffare\* delete fare\_\* show forecast show results\_bestarma

181

## A.3 Excel VBA-code for Form 41 data treatment

The following VBA programs were written exclusively by the authors, and were used to treat and convert the Form 41 data into a format that could be used for modeling in EViews6.

Sub spaltensort()

Dim i As Integer, w As Integer Dim letztespalte As Integer, namespalte As Integer, \_ yearspalte As Integer, quarterspalte As Integer Dim name As String

For w = 1 To Worksheets.Count

```
letztespalte = 0
```

'Carriername verschieben

For i = 1 To 99

If Worksheets(w).Cells(1, i).Value = "UNIQUE\_CARRIER\_NAME" Then
 namespalte = i

End If

Next

```
If Not namespalte = 1 Then
Worksheets(w).Columns(namespalte).Cut
Worksheets(w).Columns(1).Insert Shift:=xlToRight
```

```
End If
namespalte = 3
'letzte Spalte finden
For i = 1 To 99
    If Worksheets(w).Cells(1, i).Value = "" Then
        letztespalte = i - 1
    End If
Next i
' Quarter verschieben
For i = 1 To 99
    If Worksheets(w).Cells(1, i).Value = "QUARTER" Then
        quarterspalte = i
    End If
Next
If Not quarterspalte = 1 Then
    Worksheets(w).Columns(quarterspalte).Cut
    Worksheets(w).Columns(1).Insert Shift:=xlToRight
End If
quarterspalte = 2
'Jahr verschieben
For i = 1 To 99
    If Worksheets(w).Cells(1, i).Value = "YEAR" Then
```

```
yearspalte = i
End If
Next
If Not yearspalte = 1 Then
Worksheets(w).Columns(yearspalte).Cut
Worksheets(w).Columns(1).Insert Shift:=xlToRight
End If
yearspalte = 1
```

'worksheet next:

Next

-----

End Sub

Sub employquarter()

Dim w As Integer, i As Integer, z As Integer

For w = 1 To Worksheets.Count
If Left(Worksheets(w).name, 4) = "EMPL" Then
For i = 1 To 99
If Worksheets(w).Cells(1, i).Value = "" Then

```
Worksheets(w).Cells(1, i).Value = "QUARTER"
             For z = 2 To Worksheets(w).Cells(Rows.Count, 1).End(xlUp).row
                 Worksheets(w).Cells(z, i).Value = "1"
             Next
          End If
      Next
   End If
End Sub
-----
Sub entfquarter()
For w = 1 To Worksheets.Count
   If Left(Worksheets(w).name, 4) = "EMPL" Then
          Worksheets(w).Columns("J:CU").ClearContents
   End If
End Sub
-----
```

Next

```
Sub headercheck()
Dim w As Integer
Dim i As Integer, breite As Integer
For w = 2 To Worksheets.Count
    If Left(Worksheets(w).name, 4) = Left(Worksheets(w - 1).name, 4) Then
        breite = 1
        Do While Worksheets(w).Cells(1, breite).Value <> ""
            breite = breite + 1
       Loop
        For i = 1 To breite
            If Worksheets(w).Cells(1, i).Value <> _
Worksheets(w - 1).Cells(1, i).Value Then
                Debug.Print Worksheets(w).name; _
Worksheets(w).Cells(1, i).Value; Worksheets(w - 1).Cells(1, i).Value
            End If
       Next
   End If
Next
End Sub
```

\_\_\_\_\_

Sub identitycheck()

Dim lastrow As Integer, i As Integer

lastrow = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row

For i = 2 To lastrow

```
If Worksheets(1).Cells(i, 3).Value <> Worksheets(1).Cells(i, 29).Value _
Or Worksheets(1).Cells(i, 3).Value <> Worksheets(1).Cells(i, 38).Value _
Or Worksheets(1).Cells(i, 2).Value <> Worksheets(1).Cells(i, 28).Value _
Or Worksheets(1).Cells(i, 2).Value <> Worksheets(1).Cells(i, 37).Value _
Or Worksheets(1).Cells(i, 1).Value <> Worksheets(1).Cells(i, 27).Value _
Or Worksheets(1).Cells(i, 1).Value <> Worksheets(1).Cells(i, 36).Value Inter
```

End If

Next

End Sub

------

Sub zusammenfassen()

Dim i As Integer, w As Integer, z As Integer, lastrow As Integer, y As Integer Dim letztespalte As Integer, namespalte As Integer, yearspalte As Integer,\_ quarterspalte As Integer Dim name As String, year As Integer, quarter As Integer Dim gesuchtespalte As String

```
For w = 2 To Worksheets.Count
Debug.Print Worksheets(w).name
'letzte freie zeile finden
lastrow = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row
```

For i = 2 To lastrow

If Worksheets(w).Cells(i, 1).Value <> "" \_

And Worksheets(w).Cells(i, 2).Value <> "" Then

z = 2

```
name = Worksheets(w).Cells(i, 3).Value
quarter = Worksheets(w).Cells(i, 2).Value
year = Worksheets(w).Cells(i, 1).Value
```

```
If name = "" Then
z = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row + 1
'namespalte = Worksheets(w).Cells(1, 4).Value
```

```
If Left(Worksheets(w).name, 4) = "EMPL" Then
Worksheets(w).Range(Worksheets(w).Cells(i, 1), _
```

```
Worksheets(w).Cells(i, 3)).Copy Destination:=Worksheets(1).Cells(z, 1)
Worksheets(w).Range(Worksheets(w).Cells(i, 1), _
Worksheets(w).Cells(i, 9)).Cut Destination:=Worksheets(1).Cells(z, 27)
ElseIf Left(Worksheets(w).name, 4) = "ACCR" Then
Worksheets(w).Range(Worksheets(w).Cells(i, 1), _
Worksheets(w).Cells(i, 3)).Copy Destination:=Worksheets(1).Cells(z, 1)
Worksheets(w).Range(Worksheets(w).Cells(i, 1), _
Worksheets(w).Cells(i, 9)).Cut Destination:=Worksheets(1).Cells(z, 36)
Else
Debug.Print Worksheets(w).name
MsgBox ("Fehler!")
End If
```

```
End If
```

```
Do Until z > lastrow Or Worksheets(1).Cells(z, 2).Value = quarter_
And Worksheets(1).Cells(z, 1).Value = year And Worksheets(1).Cells(z, 3).Value = name
Do While Worksheets(1).Cells(z, 1).Value <> year And z < lastrow + 1
z = z + 1
Loop
Do While Worksheets(1).Cells(z, 2).Value <> quarter And z < lastrow + 1
z = z + 1
Loop
```

Do While Worksheets(1).Cells(z, 3).Value <> name And z < lastrow + 1

```
z = z + 1
                Loop
                If Left(Worksheets(w).name, 4) = "EMPL" Then
                    Do While Worksheets(1).Cells(z, 27).Value <> "" And z < lastrow + 1
                        z = z + 1
                    Loop
                ElseIf Left(Worksheets(w).name, 4) = "ACCR" Then
                    Do While Worksheets(1).Cells(z, 36).Value <> "" And z < lastrow + 1
                        z = z + 1
                    Loop
                End If
            Loop
            'Debug.Print z, Worksheets(1).Cells(z, 3).Value, name, year, quarter
            If Worksheets(1).Cells(z, 2).Value <> quarter Or _
Worksheets(1).Cells(z, 1).Value <> year Or Worksheets(1).Cells(z, 3).Value <> name Then
                If z \iff \text{lastrow} + 1 Then
                    Debug.Print z, Worksheets(1).Cells(z, 2).Value, _
quarter, Worksheets(1).Cells(z, 1).Value, year, Worksheets(1).Cells(z, 3).Value, name
                Else
                    z = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row + 1
                    'namespalte = Worksheets(w).Cells(1, 4).Value
```

190

```
If Left(Worksheets(w).name, 4) = "EMPL" Then
```

```
Worksheets(w).Range(Worksheets(w).Cells(i, 1), _
```

Worksheets(w).Cells(i, 3)).Copy Destination:=Worksheets(1).Cells(z, 1)

Worksheets(w).Range(Worksheets(w).Cells(i, 1), \_

Worksheets(w).Cells(i, 9)).Cut Destination:=Worksheets(1).Cells(z, 27)
ElseIf Left(Worksheets(w).name, 4) = "ACCR" Then

Worksheets(w).Range(Worksheets(w).Cells(i, 1), \_

Worksheets(w).Cells(i, 3)).Copy Destination:=Worksheets(1).Cells(z, 1)

Worksheets(w).Range(Worksheets(w).Cells(i, 1), \_

Worksheets(w).Cells(i, 9)).Cut Destination:=Worksheets(1).Cells(z, 36)

Else

Debug.Print Worksheets(w).name

MsgBox ("Fehler!")

End If

End If

'Debug.Print z, Worksheets(1).Cells(z, 2).Value, \_

quarter, Worksheets(1).Cells(z, 1).Value, year, Worksheets(1).Cells(z, 3).Value, name

'MsgBox ("Error. nicht richtige zeile erwischt. " & \_

name & " nicht gleich " & Worksheets(1).Cells(z, 3).Value)

ElseIf name <> "" Then

If Left(Worksheets(w).name, 4) = "EMPL" Then

Worksheets(w).Range(Worksheets(w).Cells(i, 1), \_

Worksheets(w).Cells(i, 9)).Cut Destination:=Worksheets(1).Cells(z, 27)

ElseIf Left(Worksheets(w).name, 4) = "ACCR" Then

```
Worksheets(w).Range(Worksheets(w).Cells(i, 1), _
```

```
Worksheets(w).Cells(i, 9)).Cut Destination:=Worksheets(1).Cells(z, 36)
```

Else

Debug.Print Worksheets(w).name

MsgBox ("Error")

End If

End If

End If

If w = Worksheets.Count And i = lastrow Then
 Debug.Print i, lastrow, Worksheets.Count, w
 Exit Sub

End If

Next

Next

End Sub

\_\_\_\_\_

Sub financialzusammenfuegen()

Dim breite As Integer, hoehe As Integer

```
For w = 2 To Worksheets.Count
If Left(Worksheets(w).name, 4) = "FINA" Then
breite = 1
hoehe = 1
Do While Worksheets(w).Cells(1, breite).Value <> ""
breite = breite + 1
Loop
hoehe = Worksheets(w).Cells(Rows.Count, 1).End(xlUp).row
```

```
Worksheets(w).Range(Worksheets(w).Cells(2, 1), _
```

```
Worksheets(w).Cells(hoehe, breite - 1)).Cut _
```

```
Destination:=Worksheets(1).Cells(Worksheets(1)._
```

```
Cells(Rows.Count, 1).End(xlUp).row + 1, 1)
```

End If

Next

End Sub

\_\_\_\_\_

Sub spaltensort()

Dim w As Integer

```
For w = 1 To Worksheets.Count
```

Worksheets(w).Range("A1:ZZ999").Sort Key1:=Worksheets(w).Range("A1"),\_

Order1:=xlAscending, Orientation:=xlColumns

Next

End Sub

-----

Sub spaltsort2()

With ActiveWorkbook.Worksheets(3).Sort
 .SetRange Range("A1:Z350")
 .Header = xlYes
 .MatchCase = False
 .Orientation = xlLeftToRight
 .SortMethod = xlPinYin
 .Apply
 End With
End Sub

-----

Sub sum\_regions()

```
Dim i As Integer, s As Integer
Dim row As Integer
row = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row
i = 2
Do Until i > row
    If Cells(i, 1).Value = Cells(i + 1, 1).Value And Cells(i, 2).Value = _
    Cells(i + 1, 2).Value And Cells(i, 3).Value = Cells(i + 1, 3).Value Then
        For s = 4 To 26
            Cells(i, s).Value = Cells(i, s).Value + Cells(i + 1, s).Value
        Next
        For s = 30 To 35
            Cells(i, s).Value = Cells(i, s).Value + Cells(i + 1, s).Value
        Next
        Cells(i, 39).Value = Cells(i, 39).Value + Cells(i + 1, 39).Value
        Rows(i + 1).Delete
        row = row - 1
        i = i - 1
    End If
    i = i + 1
   Debug.Print i
Loop
```

End Sub

\_\_\_\_\_

Sub identitycheck2()

Dim lastrow As Integer, i As Integer

lastrow = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row

For i = 2 To lastrow

If Worksheets(1).Cells(i, 3).Value <> Worksheets(1).Cells(i, 29).Value \_
And Worksheets(1).Cells(i, 29).Value <> "" \_
Or Worksheets(1).Cells(i, 3).Value <> Worksheets(1).Cells(i, 38).Value \_
And Worksheets(1).Cells(i, 2).Value <> Worksheets(1).Cells(i, 28).Value \_
And Worksheets(1).Cells(i, 28).Value <> "" \_
Or Worksheets(1).Cells(i, 2).Value <> Worksheets(1).Cells(i, 37).Value \_
And Worksheets(1).Cells(i, 37).Value <> Worksheets(1).Cells(i, 37).Value \_
And Worksheets(1).Cells(i, 1).Value <> Worksheets(1).Cells(i, 27).Value \_
And Worksheets(1).Cells(i, 1).Value <> Worksheets(1).Cells(i, 36).Value \_
And Worksheets(1).Cells(i, 1).Value <> "" \_
Or Worksheets(1).Cells(i, 1).Value <> Worksheets(1).Cells(i, 36).Value \_
And Worksheets(1).Cells(i, 1).Value <> "" \_
Or Worksheets(1).Cells(i, 36).Value <> "" \_

Debug.Print i,

End If

Next

End Sub

\_\_\_\_\_

Sub cellformat()

Dim lastrow As Integer

Dim s As Integer, i As Integer

lastrow = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row

For s = 4 To 26

```
For i = 2 To lastrow
```

Worksheets(1).Cells(i, s).Value = CDbl(Worksheets(1).Cells(i, s).Value) / 100

Next

Next

For i = 2 To lastrow

```
Worksheets(1).Cells(i, 39).Value = CDbl(Worksheets(1).Cells(i, 39).Value) / 100
Next
```

End Sub

```
-----
```

Sub create\_ws()

For i = 4 To 26

Worksheets.Add after:=Worksheets(Worksheets.Count)

```
Worksheets(Worksheets.Count).name = Worksheets(1).Cells(1, i).Value
```

Next

For i = 30 To 36

Worksheets.Add after:=Worksheets(Worksheets.Count)

```
Worksheets(Worksheets.Count).name = Worksheets(1).Cells(1, i).Value
```

Next

```
Worksheets.Add after:=Worksheets(Worksheets.Count)
Worksheets(Worksheets.Count).name = Worksheets(1).Cells(1, 39).Value
```

End Sub

\_\_\_\_\_

```
Sub singlesheets_financial()
```

Dim i As Integer, c As Integer, s As Integer, quarter As Integer Dim name As String

```
For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row - 1
   quarter = (Worksheets(1).Cells(i, 1).Value - 1990) * 4 + Worksheets(1).Cells(i, 2).Value
   If Worksheets(1).Cells(i, 3).Value = "American Airlines Inc." Then
        c = 2
   ElseIf Worksheets(1).Cells(i, 3).Value = "Continental Air Lines Inc." Then
        c = 3
   ElseIf Worksheets(1).Cells(i, 3).Value = "Delta Air Lines Inc." Then
        c = 4
   ElseIf Worksheets(1).Cells(i, 3).Value = "Northwest Airlines Inc." Then
        c = 5
   ElseIf Worksheets(1).Cells(i, 3).Value = "Southwest Airlines Co." Then
        c = 6
   ElseIf Worksheets(1).Cells(i, 3).Value = "United Air Lines Inc." Then
        c = 7
   ElseIf Worksheets(1).Cells(i, 3).Value = "US Airways Inc." Then
        c = 8
   Else
        c = 0
```

End If

If c <> 0 Then

```
For s = 4 To 26
name = Worksheets(1).Cells(1, s).Value
Worksheets(name).Cells(quarter + 1, c).Value = Worksheets(1).Cells(i, s).Value
Next
```

```
For s = 30 To 35
name = Worksheets(1).Cells(1, s).Value
Worksheets(name).Cells(quarter + 1, c).Value = Worksheets(1).Cells(i, s).Value
Next
```

```
Worksheets("ACCR_SALARIES").Cells(quarter + 1, c).Value = _
Worksheets(1).Cells(i, 39).Value
```

End If

Next

End Sub

\_\_\_\_\_

```
Sub inflate_financial()
Dim w As Integer, i As Integer, s As Integer
Dim quarter As Integer, row As Integer
w = 3
Do Until Worksheets(w).name = "GENERAL_MANAGE"
For i = 2 To 68
quarter = Worksheets(w).Cells(i, 1)
row = 2 + (3 * (quarter - 1))
For s = 2 To 8
Worksheets(w).Cells(i, s) = Worksheets(w).Cells(i, s).Value * _
Worksheets("Inflation").Cells(row, 8)
Next
Next
w = w + 1
Worksheets(w).Activate
```

Loop

End Sub

\_\_\_\_\_

Sub delete1990()

```
For w = 3 To Worksheets.Count
```

Worksheets(w).Range("B2:H13").Delete Shift:=xlUp

Worksheets(w).Range("A69:A80").ClearContents

Next

End Sub

```
Sub quarterize_employees()
```

Dim w As Worksheet Dim i As Integer, s As Integer, z As Integer

Dim a As Integer

```
Set w = Worksheets("TOTAL")
i = 3
```

w.Columns(2).Insert

w.Cells(1, 2).Value = "QUARTER"

```
Do Until w.Cells(i, 1).Value = ""
```

```
If w.Cells(i, 1).Value <> w.Cells(i + 1, 1).Value Then
        w.Rows(i).Insert
       w.Rows(i).Insert
        w.Rows(i).Insert
       For s = 3 To 9
            a = (w.Cells(i + 3, s).Value - w.Cells(i - 1, s).Value) / 4
            For z = 0 To 2
                w.Cells(i + z, s).Value = w.Cells(i - 1, s).Value + (z + 1) * a
            Next
        Next
       For z = 0 To 2
            w.Cells(i + z, 1).Value = w.Cells(i - 1, 1).Value
            w.Cells(i + z, 2).Value = z + 2
        Next
        w.Cells(i - 1, 2).Value = 1
   End If
   i = i + 4
Loop
```

End Sub

\_\_\_\_\_

```
Sub quarterize_pilots()
```

Dim w As Worksheet

Dim i As Integer, s As Integer, z As Integer

Dim a As Integer

```
Set w = Worksheets("PILOTS_COPILOTS")
```

i = 3

```
w.Columns(2).Insert
w.Cells(1, 2).Value = "QUARTER"
```

Do Until w.Cells(i, 1).Value = ""

```
If w.Cells(i, 1).Value <> w.Cells(i + 1, 1).Value Then
w.Rows(i).Insert
w.Rows(i).Insert
For s = 3 To 9
a = (w.Cells(i + 3, s).Value - w.Cells(i - 1, s).Value) / 4
For z = 0 To 2
w.Cells(i + z, s).Value = w.Cells(i - 1, s).Value + (z + 1) * a
```

```
Next
       For z = 0 To 2
           w.Cells(i + z, 1).Value = w.Cells(i - 1, 1).Value
           w.Cells(i + z, 2).Value = z + 2
       Next
       w.Cells(i - 1, 2).Value = 1
   End If
   i = i + 4
Loop
End Sub
-----
Sub fueldatain1()
Dim breite As Integer, hoehe As Integer
For w = 2 To Worksheets.Count
       breite = 1
       hoehe = 1
       Do While Worksheets(w).Cells(1, breite).Value <> ""
```

breite = breite + 1

Next

Loop

```
hoehe = Worksheets(w).Cells(Rows.Count, 1).End(xlUp).row
```

```
Worksheets(w).Range(Worksheets(w).Cells(2, 1), _
```

Worksheets(w).Cells(hoehe, breite - 1)).Cut \_

```
Destination:=Worksheets(1).Cells(Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row + 1, 1)
Next
```

End Sub

```
-----
```

Sub monthtoquarter()

Dim i As Integer, s As Integer Dim row As Integer

```
row = Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row
i = 2
```

```
Do Until i > row
If Cells(i, 1).Value = Cells(i + 1, 1).Value And _
Cells(i, 2).Value = Cells(i + 1, 2).Value _
And Cells(i, 4).Value = Cells(i + 1, 4).Value Then
For s = 6 To 13
```

```
Cells(i, s).Value = Cells(i, s).Value + _
           Cells(i + 1, s).Value
       Next
       Rows(i + 1).Delete
       row = row - 1
       i = i - 1
   End If
   i = i + 1
Loop
End Sub
-----
Sub zerotest()
Dim i As Integer, s As Integer
For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row
   Debug.Print i
   For s = 6 To 9
       If Right(Cells(i, s).Value, 2) <> "00" Then
           mbox = ("Zeile" & i & ", Spalte" & s)
       End If
   Next
```

End Sub

-----

Sub convertdbl()

Dim i As Integer, s As Integer

For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row
Debug.Print i
For s = 6 To 9
Cells(i, s).Value = CDbl(Cells(i, s).Value) / 100
Next

Next

End Sub

\_\_\_\_\_

```
Sub carriercodetest()
Dim i As Integer, s As Integer
For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row - 1
   Debug.Print i
   For s = 6 To 9
       If Cells(i, 4).Value = Cells(i + 1, 4).Value Then
          mbox = ("Zeile" & i & ", Spalte" & s)
       End If
   Next
Next
End Sub
-----
Sub inflate()
Dim year As Integer, month As Integer
Dim row As Integer
Dim i As Integer
```

For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row

```
year = Worksheets(1).Cells(i, 1).Value
month = Worksheets(1).Cells(i, 3).Value
row = (year - 1993) * 12 + month + 1
Worksheets(1).Cells(i, 10).Value = Worksheets(1).Cells(i, 8).Value * _
Worksheets("Inflation").Cells(row, 4)
Worksheets(1).Cells(i, 11).Value = Worksheets(1).Cells(i, 9).Value * _
Worksheets("Inflation").Cells(row, 4)
Worksheets(1).Cells(i, 12).Value = Worksheets(1).Cells(i, 8).Value * _
Worksheets("Inflation").Cells(row, 5)
Worksheets(1).Cells(i, 13).Value = Worksheets(1).Cells(i, 9).Value * _
Worksheets(1).Cells(i, 5)
```

End Sub

-----

Sub inflate2()

Dim year As Integer, quarter As Integer Dim row As Integer Dim i As Integer

For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row

```
year = Worksheets(1).Cells(i, 1).Value
quarter = Worksheets(1).Cells(i, 2).Value
row = (year - 1993) * 12 + (quarter - 1) * 3 + 2
Worksheets(1).Cells(i, 13).Value = Worksheets(1).Cells(i, 7).Value * _
Worksheets("Inflation").Cells(row, 8).Value
Worksheets(1).Cells(i, 14).Value = Worksheets(1).Cells(i, 8).Value * _
Worksheets("Inflation").Cells(row, 8).Value
```

End Sub

\_\_\_\_\_

Sub singlesheets()

Dim i As Integer, c As Integer, x As Integer, quarter As Integer

```
For i = 2 To Worksheets(1).Cells(Rows.Count, 1).End(xlUp).row - 1
quarter = Worksheets(1).Cells(i, 3).Value
If Worksheets(1).Cells(i, 4).Value = "AA" Then
    c = 2
ElseIf Worksheets(1).Cells(i, 4).Value = "CO" Then
    c = 3
ElseIf Worksheets(1).Cells(i, 4).Value = "DL" Then
    c = 4
```

```
ElseIf Worksheets(1).Cells(i, 4).Value = "NW" Then
    c = 5
ElseIf Worksheets(1).Cells(i, 4).Value = "WN" Then
    c = 6
ElseIf Worksheets(1).Cells(i, 4).Value = "UA" Then
    c = 7
ElseIf Worksheets(1).Cells(i, 4).Value = "US" Then
    c = 8
Else
    c = 0
End If
If c \iff 0 Then
    Worksheets("TDOMT_GALLONS").Cells(quarter - 27, c).Value = _
    Worksheets(1).Cells(i, 6).Value
    Worksheets("TOTAL_GALLONS").Cells(quarter - 27, c).Value = _
    Worksheets(1).Cells(i, 7).Value
    Worksheets("TDOMT_COST").Cells(quarter - 27, c).Value = _
    Worksheets(1).Cells(i, 10).Value
    Worksheets("TOTAL_COST").Cells(quarter - 27, c).Value = _
    Worksheets(1).Cells(i, 11).Value
```

```
End If
```

End Sub

## A.4 Python Code

The two extended Python programs for preliminary data treatment in this project were developed by Steve Lawford.

.....

Parse complete\_coupon dictionary to text.
(for project with Anthony/Maximilian)

Steve Lawford: 20 November 2009

.....

```
import cPickle,time
from safe_cPickle import *
```

# Set oneway\_flag=1 for one-way flights only (=0 for return flights)
oneway\_flag=0

if oneway\_flag:

data\_path='C:/Project/data/complete\_coupon\_oneway/'

filename='complete\_coupon\_oneway'

else:

data\_path='C:/Project/data/complete\_coupon/'

filename='complete\_coupon'

# cPickle load individual coupon\_full\_x\_x dictionaries

```
t0=time.time(); print 'Loading dictionary: '+filename
c_x_x=open(data_path+filename,'r')
dt=cPickle.load(c_x_x)
print str(time.time()-t0)+' seconds to load dictionary.'
# CPI data parse
print; print 'Parsing CPI data.'
t0=time.time()
f=open('C:/Project/data/us_cpi_index/us_cpi_monthly.txt','r')
cpi_index_monthly={}
for 1 in f:
    cpidata=l.strip().split()
    cpi_index_monthly[cpidata[0]+'_'+cpidata[1]]=eval(cpidata[2])
f.close()
cpi_index_quarterly={}
for m in cpi_index_monthly.keys():
    if m.split('_')[1]=='1':
        cpi_index_quarterly[m.split('_')[0]+'_1']=cpi_index_monthly[m]
    elif m.split('_')[1]=='4':
```

```
cpi_index_quarterly[m.split('_')[0]+'_2']=cpi_index_monthly[m]
```

```
elif m.split('_')[1]=='7':
```

```
cpi_index_quarterly[m.split('_')[0]+'_3']=cpi_index_monthly[m]
elif m.split('_')[1]=='10':
```

```
cpi_index_quarterly[m.split('_')[0]+'_4']=cpi_index_monthly[m]
else:
```

pass

# CPI deflator

```
# Hard-coded: 2009Q1 prices
```

```
cpi_deflator={}
```

```
for m in cpi_index_quarterly.keys():
```

cpi\_deflator[m]=cpi\_index\_quarterly['2009\_1']/cpi\_index\_quarterly[m]

print str(time.time()-t0)+' seconds to parse CPI data.'

```
length=len(dt[dt.keys()[0]])
```

#print; print 'Length of data file: '+str(length); print
#print 'Dictionary keys: ',dt.keys(); print

```
print; print 'Creating output file.'
t0=time.time()
```

```
routes_all={}; carriers_all={}; timeslot={}
```

```
for i in range(length):
```

```
if dt['OpCarrier'][i]!='TW':
    routes_all[dt['Origin'][i]+'_'+dt['Dest'][i]]=0
    carriers_all[dt['OpCarrier'][i]]=0
    timeslot[eval(dt['Year'][i]+dt['Quarter'][i])]=0
```

```
routes_all_list=routes_all.keys()
```

```
routes_all_list.sort()
```

```
route_codes={}; count=1
```

```
for j in routes_all_list:
    route_codes[j]=count
    count+=1
```

```
carriers_all_list=carriers_all.keys()
carriers_all_list.sort()
```

```
carrier_codes={}; count=1
for j in carriers_all_list:
    carrier_codes[j]=count
    count+=1
```

#print carrier\_codes

```
timet=timeslot.keys()
```

```
timet.sort()
timecode={}; count1=1
for k in timet:
    timecode[k]=count1
    count1+=1
```

```
output='Origin'+'\t'+'Dest'+'\t'+'Year'+'\t'+'Quarter'+'\t'+
'OpCarrier'+'\t'+'AvFare'+'\t'+'TotalPass'+'\t'+\
'Route'+'\t'+'Routecode'+'\t'+'Carriercode'+'\t'+'Time'+'\t'
+'CPIquarter'+'\t'+'CPIdeflator'+'\t'+'RealAvFare'+'\n'
```

```
for i in range(length):
```

```
if dt['0pCarrier'][i]!='TW':
    output+=dt['Origin'][i]+'\t'+dt['Dest'][i]+'\t'+dt['Year'][i]+
    '\t'+dt['Quarter'][i]+'\t'+dt['OpCarrier'][i]+\
    '\t'+str(dt['AvFare'][i])+'\t'+str(dt['TotalPass'][i])+'\t'+
    dt['Origin'][i]+'_'+dt['Dest'][i]+\
    '\t'+str(route_codes[dt['Origin'][i]+'_'+dt['Dest'][i]])+
    '\t'+str(carrier_codes[dt['OpCarrier'][i]])+\
    '\t'+str(timecode[eval(dt['Year'][i]+dt['Quarter'][i]])+'\t'+\
    str(cpi_index_quarterly[dt['Year'][i]+'_'+dt['Quarter'][i]])+'\t'+\
    str(cpi_deflator[dt['Year'][i]+'_'+dt['Quarter'][i]])+'\t'+\
    str(dt['AvFare'][i]*cpi_deflator[dt['Year'][i]+'_'+
    dt['Quarter'][i])+'\n'
```

```
print str(time.time()-t0)+' seconds to create output.'
print; print 'Saving file.'
t0=time.time()
```

```
f=open(data_path+filename+'_text.txt','w'); f.write(output); f.close()
```

```
print str(time.time()-t0)+' seconds to save file.'; print
print 'Done.'
```

-----

.....

Data parse for dynamic economic fare models, by route. (for project with Anthony/Maximilian)

Steve Lawford : 24 January 2010

.....

import os,sys
from scipy import \*
from airport\_location\_function\_modified\_return import \*
from route\_population\_geom\_mean\_function import \*
from route\_leisure\_function import leisure\_function

from route\_business\_function import business\_function
from airport\_gdp\_function import gdp\_function

```
module_dir=os.path.join('Project','code')
sys.path.insert(0,module_dir)
```

```
leisure_dict=leisure_function(0.05)
business_dict=business_function(0.10)
gdp_dict=gdp_function()
```

r\_sphere=6372.7974775959065 # km

def distance\_calculator(dest\_coords\_degrees,origin\_coords\_degrees):

distance=r\_sphere\*theta

```
return distance
```

```
for rr in range(1,8):
    filename='fares_route'+str(rr)+'.txt'
    filenameout=filename.split('.')[0]+'_out.txt'
    f=open('C:/Project/data/'+filename,'r')
    c=0
    for j in f:
        c+=1
        k=j.split('\t')
        if c==1:
            lencheck=len(k); dct={}
            for i in range(len(k)):
                if k[i]!='' and k[i]!='\n': dct[i]=[k[i].strip(),['']*65]
        else:
            for i in range(len(k)):
                if k[i]!='' and k[i]!='\n': dct[i][1][c-2]=eval(k[i].strip())
    f.close()
    dct2=\{\}
    for m in dct.keys():
        dct2[dct[m][0]]=dct[m][1]
    dct3={}
```

print

for n in dct2.keys():
 p=n.split('\_')

```
flag=0
```

#### try:

```
dest_coords_degrees=airport_location(p[0])[1]
origin_coords_degrees=airport_location(p[1])[1]
distance=distance_calculator(dest_coords_degrees,origin_coords_degrees)
distance=abs(distance)
```

except TypeError: flag=1

#### try:

```
popn=route_population(p[0],p[1])
leisure=max(leisure_dict[p[0]],leisure_dict[p[1]])
business=max(business_dict[p[0]],business_dict[p[1]])
gdp=(gdp_dict[p[0]]*gdp_dict[p[1]])**0.5
except KeyError: flag=1
```

```
if not flag and popn!=None:
    dct3[n]=[dct2[n],distance]
    dct3[n].append(eval(popn))
    dct3[n].append(leisure)
```

```
dct3[n].append(business)
        dct3[n].append(gdp)
    else: pass
output=''; lines=0
for s in dct3.keys():
   c=0
   for t in dct3[s][0]:
       c+=1
        if t!='':
            lines+=1
            output+=str(t)+'/t'+str(c)+'/t'+str(dct3[s][1])+'/t'+
            str(dct3[s][2])+'\t'
            output+=str(dct3[s][3])+'\t'+str(dct3[s][4])+'\t'+
            str(dct3[s][5])+'\t'
            if c>=35: output+=str(1)+'\n'
            elif c<35: output+=str(0)+'\n'
```

```
print str(lines)+' lines in file '+filenameout
f=open(filenameout,'w'); f.write(output); f.close()
```

# List of Figures

1	Domestic traffic of American Airlines from Fort Worth International Airport (ENAC	
	Air Transport Data).	7
2	Domestic traffic of Continental Airlines from George Bush Intercontinental Airport	
	(ENAC Air Transport Data).	9
3	Domestic traffic of Delta Air Lines from Hartsfield-Jackson Atlanta International	
	Airport (ENAC Air Transport Data).	10
4	Domestic traffic of Northwest Airlines from Detroit Metro Airport (ENAC Air Transport	
	Data)	11
5	Domestic traffic of United Airlines from Chicago O'Hare International Airport (ENAC	
	Air Transport Data)	12
6	Domestic traffic of US Airways from Charlotte Douglas International Airport (ENAC	
	Air Transport Data)	13
7	Domestic traffic of Southwest Airlines from Las Vegas McCarran International Airport	
	(ENAC Air Transport Data).	14
8	Excerpt from the DB1B Ticket database for 2009Q1, where FLL is Fort Lauderdale	
	Airport (IATA airport code), FL is Florida, WN is Southwest (IATA airline code),	
	the itinerary Fare is nominal (in U.S.\$), and distance is measured in miles. In the	
	text, we take a closer look at the 3 highlighted it ineraries	16
9	Coupons bought by passengers on an itinerary in 2008, for all U.S. reporting carriers.	
	We observe that the proportion of tickets with 2 or 4 itineraries represents more	
	than $66\%$ of all tickets sold. In fact, this graph does not give us the proportion of	
	round trips or changes of planes, so we cannot state whether the $4,250,000$ 4-coupon	
	itineraries are one-stop returns or one-way trips with 4 successive changes of plane.	17
10	Number of passengers per quarter in 2008	18

11	State of departure for 2008 itineraries	19
12	Number of passengers for 2008 itineraries as a percentage of the population estimates	
	by U.S. state.	20
13	Carrier reporting 2008 itineraries	21
14	Excerpt from the DB1B Coupon database for 2009Q1. As for the Ticket database,	
	the itinerary fare is nominal, in U.S.\$, and distance is measured in miles. We will	
	later take a closer look at the 3 highlighted itineraries	23
15	Fare class for coupons purchased in 2008. These fare class are defined by reporting	
	carriers.	24
16	U.S. Consumer Price Index between 1993 and 2009.	27
17	CPI deflators (dashed) and inflation estimates between 1993 and 2009	29
18	Illustrative Southwest ticket from Kansas City to Milwaukee.	30
19	Quarterly average fares for round trips (unit: real 2009 US\$). The data for the	
	airline Southwest in the DB1B database, for round trips, is given by the DOT only	
	from the third quarter of 1998. Before this quarter Southwest did not report round	
	trips	32
20	Number of passengers carried per quarter (round trips). As for the fares, data from	
	Southwest is only available from the third quarter of 2008	33
21	Quarterly average fares for American Airlines (\$ against time).	36
22	American Airlines - regression on quarterly average fares: @trend stands for the	
	regression of the results over time, and dummy stands for the dummy variable	
	previously presented	44
23	American Airlines - final regression on quarterly average fares.	45
24	American Airlines - final regression on quarterly average fares (non filtered data)	46
25	Continental Airlines - regression on quarterly average fares	47

26	Continental Airlines - residual correlograms of the regression in Figure 25	48
27	Quarterly average fares for Continental Airlines (\$ against time)	49
28	Number of passengers carried by Continental Airlines per quarter.	49
29	Continental Airlines - regression on quarterly average fares	50
30	Continental Airlines - residual correlograms of the regression in Figure 29	51
31	Continental Airlines - regression on quarterly average fares	52
32	Delta Airlines - regression on quarterly average fares	53
33	Quarterly average fares for Delta Airlines (\$ against time).	54
34	Delta Airlines - regression on quarterly average fares	55
35	Quarterly average fares for Northwest Airlines (\$ against time)	56
36	Northwest Airlines - regression on quarterly average fares	57
37	Quarterly average fares for United Airlines (\$ against time)	58
38	United Airlines - regression on quarterly average fares	59
39	Quarterly average fares for US Airways (\$ against time)	59
40	US Airways - regression on quarterly average fares	60
41	Quarterly average fares for Southwest Airlines (\$ against time)	60
42	Southwest Airlines - regression on quarterly average fares	61
43	In-sample dynamic forecasts of average fares from quarter 58 to quarter 65. Forecast	
	1 refers to American, forecast 2 refers to Continental, 3 refers to Delta, 4 refers to	
	Northwest, 5 refers to United, 6 refers to US Airways and 7 refers to Southwest. $\ . \ .$	66
44	Out-of-sample dynamic forecasts of average fares from quarter 65 to quarter 73.	
	Forecast 1 refers to American, forecast 2 refers to Continental, 3 refers to Delta,	
	4 refers to Northwest, 5 refers to United, 6 refers to US Airways and 7 refers to	
	Southwest	67

45	Number of passengers carried per quarter (on round trips) from $1993$ (quarter 1) to	
	2009 (quarter 65)	68
46	Quarterly number of passengers carried by American Airlines on round trips	70
47	American Airlines - regression on the quarterly number of passengers (filtered data).	71
48	American Airlines - regression on the quarterly number of passengers (filtered data).	72
49	American Airlines - regression on the quarterly number of passengers (filtered data).	73
50	American Airlines - regression on the quarterly number of passengers (filtered data).	74
51	American Airlines - regression on the quarterly number of passengers (non-filtered	
	data)	75
52	Number of passengers carried by Continental Airlines per quarter.	76
53	Continental Airlines - regression on the quarterly number of passengers (non-filtered	
	data)	77
54	Number of passengers carried by Delta Air Lines per quarter	78
55	Delta Air Lines - regression on the quarterly number of passengers (filtered data).	78
56	Delta Air Lines - regression on the quarterly number of passengers (non-filtered data).	79
57	Number of passengers carried by Northwest Airlines per quarter.	80
58	Northwest Airlines - regression on the quarterly number of passengers (non-filtered	
	data)	81
59	Number of passengers carried by United Airlines per quarter	82
60	United Airlines - regression on the quarterly number of passengers (filtered data)	82
61	United Airlines - regression on the quarterly number of passengers (non-filtered data).	83
62	Number of passengers carried by US Airways per quarter	84
63	US Airways - regression on the quarterly number of passengers (filtered data)	84
64	US Airways - regression on the quarterly number of passengers (non-filtered data).	85
65	Number of passengers carried by Southwest Airlines per quarter.	86

66	Southwest Airlines - regression on the quarterly number of passengers (filtered data).	86
67	Southwest Airlines - correlograms of the residuals for the regression in Figure 66	87
68	Southwest Airlines - regression on the quarterly number of passengers (filtered data).	87
69	In-sample dynamic forecasts of the number of passengers carried from quarter 58 to	
	quarter 65. Forecast 1 refers to American, forecast 2 refers to Continental, 3 refers	
	to Delta, 4 refers to Northwest, 5 refers to United, 6 refers to US Airways and 7	
	refers to Southwest.	91
70	Out-of-sample dynamic forecasts of the number of passengers carried from quarter	
	65 to quarter 73. Forecast 1 refers to American, forecast 2 refers to Continental, 3	
	refers to Delta, 4 refers to Northwest, 5 refers to United, 6 refers to US Airways and	
	7 refers to Southwest.	92
71	Accrued Salaries of the 7 airlines between 1993 and 2006, i.e. quarter no. $1$ is $1993$ Q1	
	and quarter no. 55 is 2006Q4	94
72	Number of pilots and co-pilots in the original yearly format	96
73	Total number of employees in the original yearly format	96
74	Total number of employees after the expansion to quarterly data through linear	
	regression.	97
75	Aircraft and traffic servicing expenses.	100
76	Expenses for depreciation and amortization.	101
77	Flying operations expenses.	102
78	General and administrative expenses	103
79	Income before income tax	104
80	Income tax.	105
81	Other interest expense	106
82	Interest on long-term debt and capital leases.	107

### 

83	Aircraft maintenance
84	Net income
85	Nonoperating income and expenses
86	Total Operating Expenses
87	Operating profit or loss
88	Total operating revenues
89	Passenger service
90	Expenses for promotion and sales
91	Passenger transport revenues
92	Transport related expenses
93	Transport related revenues
94	Domestic fuel consumption
95	Total fuel consumption
96	Domestic fuel expenses
97	Total fuel expenses
98	Real Gross Domestic Product (GDPCA) (% of annual variation against time) 117
99	GDPCA (scaled to appear with the average fares of the airlines), and the quarterly
	average fares of the airlines (fare1 is for American, 2 is for Continental, 3 for Delta,
	4 for Northwest, 5 for United, 6 for US Airways, 7 for Southwest)
100	American Airlines - regression on quarterly average fares. ecol_13 stands for the
	variable of Operational Expenses
101	Continental Airlines - regression on quarterly average fares. eco2_21 stands for the
	variable of the total number of employees
102	Continental Airlines - regression on quarterly average fares. eco2_24 stands for the
	variable of Transport Expenses

103	Delta Air Lines - regression on quarterly average fares. $eco3_16$ stands for the variable
	of Passenger Services
104	Northwest Airlines - regression on quarterly average fares. eco4_4 stands for the
	variable of Flying Operations
105	United Airlines - regression on quarterly average fares. $eco5_16$ stands for the variable
	of Passenger Services
106	US Airways - regression on quarterly average fares. eco6_24 stands for the variable
	of Transport Expenses
107	Southwest Airlines - regression on quarterly average fares. $eco7_26$ stands for the
	variable of Transport Revenue
108	Quarterly average fares between Chicago (ORD) and Atlanta (ATL) (\$ against time).130
109	American Airlines - regression on quarterly average fares
110	Delta Air Lines - regression on quarterly average fares
111	United Airlines - regression on quarterly average fares
112	American Airlines - regression on the number of passengers per quarter
113	Delta Air Lines - regression on the number of passengers per quarter
114	United Airlines - regression on the number of passengers per quarter
115	Delta Air Lines - regression on the number of passengers per quarter
116	Quarterly average fares between Los Angeles (LAX) and New-York (JFK) ( $\$ against
	time)
117	American Airlines - regression on quarterly average fares
118	Delta Air Lines - regression on quarterly average fares
119	United Airlines - regression on quarterly average fares
120	American Airlines - regression on the number of passengers per quarter
121	Delta Air Lines - regression on the number of passengers per quarter

122	United Airlines - regression on the number of passengers per quarter
123	Quarterly average fares between Baltimore (BWI) and Seattle (SEA) (\$ against time).145
124	Northwest Airlines - regression on quarterly average fares
125	United Airlines - regression on quarterly average fares
126	Southwest Airlines - regression on quarterly average fares
127	American Airlines - economic regression on quarterly average fares
128	Continental Airlines - economic regression on quarterly average fares
129	Delta Air Lines - economic regression on quarterly average fares
130	Northwest Airlines - economic regression on quarterly average fares
131	United Airlines - economic regression on quarterly average fares
132	US Airways - economic regression on quarterly average fares
133	Southwest Airlines - economic regression on quarterly average fares
134	Best ARMA models for filtered data
135	Best ARMA models for non filtered data
136	Best ARMA models for non filtered data
137	Best ARMA models for filtered data with the use of a trend variable
138	Best ARMA models for filtered data with the use of a dummy variable at period 35. 165
139	Best ARMA models for filtered data (allowing 5 lags for p,q in $\operatorname{ARMA}(p,q)).$ 166
140	Best ARMA models for differentiated dependant variable (i.e. best $ARIMA(p,1,q)$
	models) in filtered data
141	Best ARIMA models for filtered data (with possible use of a trend variable and a
	dummy variable)
142	Best ARIMA models for non-filtered data (with possible use of a trend variable and
	a dummy variable)

## List of Tables

1	The carriers are denoted by their IATA airline codes. " $se(\alpha_i)$ " stands for the	
	standard error of the coefficient $\alpha_i$ , and " $t - stat(\alpha_i)$ " stands for the Student's	
	t-statistic, which asymptotically follows a standard normal distribution. " $R^2$ " is the	
	coefficient of determination of the regression, which is a measure of the global fit of	
	the model	34
2	The carriers are reported with their IATA airline codes	63
3	The carriers are reported with their IATA airline codes.	89